



ФОНД
ДМИТРИЯ ЗИМИНА

Династия

Летняя школа

«Нанофизика низких температур»

20-30 августа 2007

Superconductivity on the Localization Threshold

&

Superconductor-Insulator quantum phase transition

Experiment

Tatyana Baturina

Concrete address

✓ Superconducting

✓ Disordered

$$T\tau \ll 1$$

✓ Two-dimensional systems

quasi-2D → electronic spectrum is 3D

$$l, \lambda_F < d < \xi, l_T$$

✓ Disordered Superconducting
Ultra-thin Films

Evolution

weak disorder

strong disorder

metal

Drude conductivity
+
quantum corrections

insulator

thermally activated
or Mott-Efros-Shklovskii-like
behavior of conductivity

+

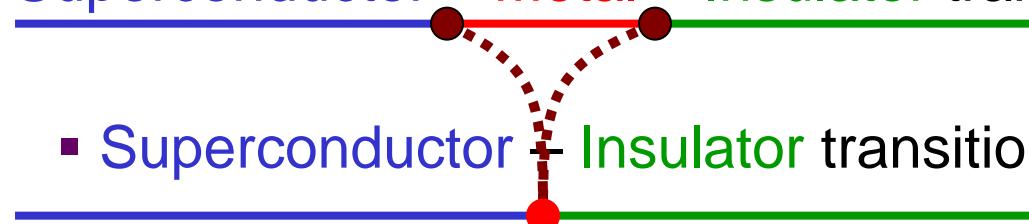
superconductivity
Cooper pairing
attractive interaction

Outline

- ✓ Quantum corrections to conductivity at $T > T_c$
- ✓ Fermionic and Bosonic Models

✓ Suppression of Superconductivity by Disorder

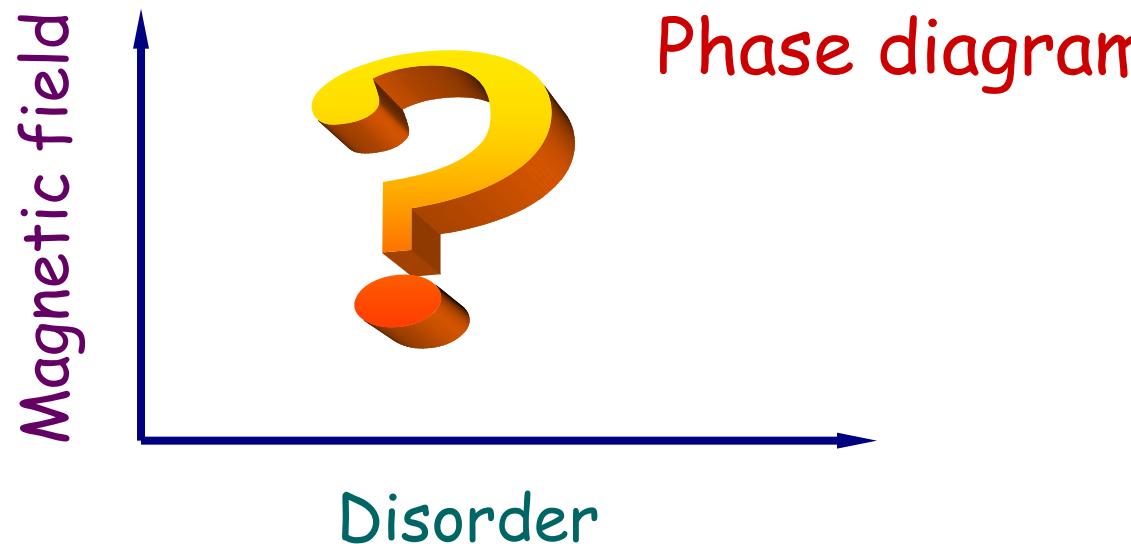
- Superconductor – Metal – Insulator transition (**SMIT**)



- Superconductor – Insulator transition (**SIT**)

✓ Suppression of Superconductivity by Magnetic field

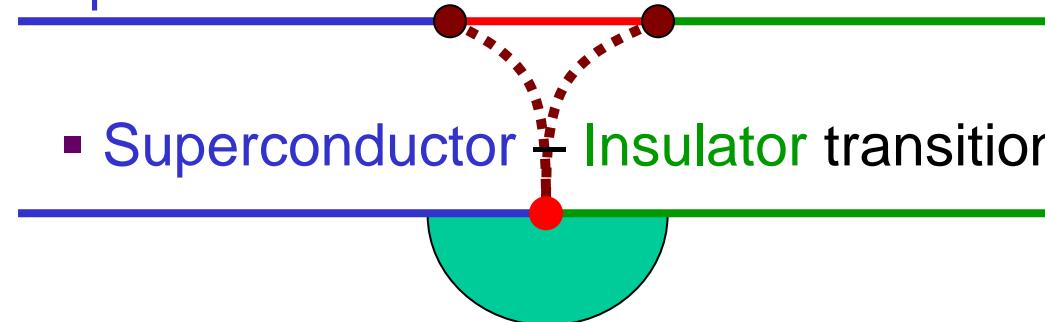
- Evolution from Superconductor – Metal transition (**SMT**)
to Superconductor – Insulator transition (**SIT**)





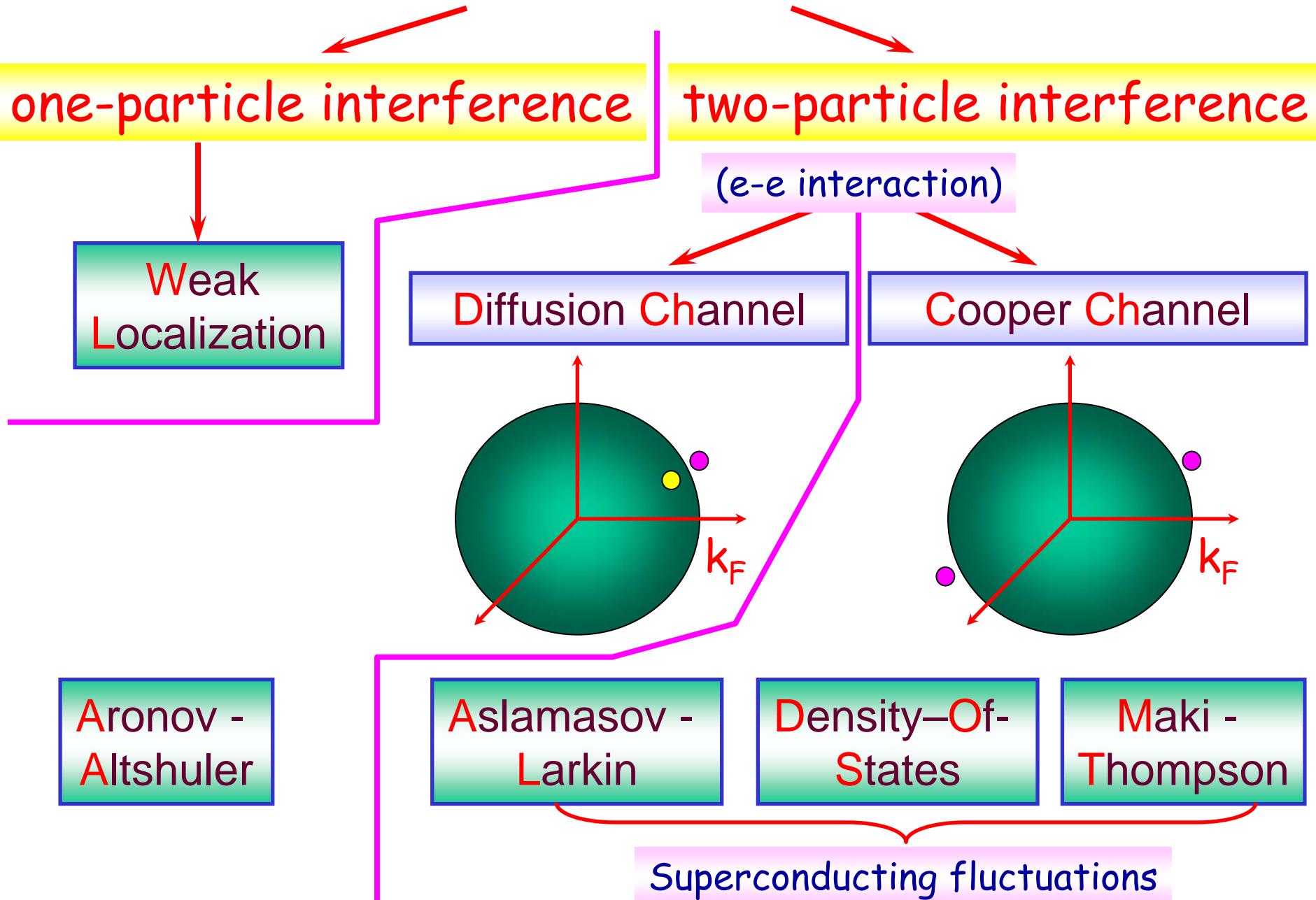
Suppression of Superconductivity by Disorder

- Superconductor – Metal – Insulator transition (SMIT)

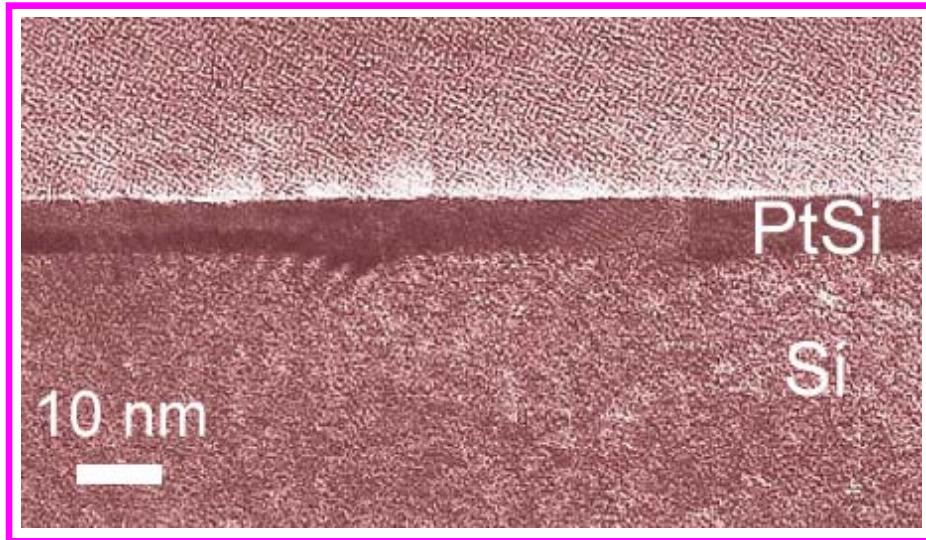


Critical Region
of the Disorder-Driven
Superconductor-Insulator
quantum phase transition

Quantum corrections to conductivity



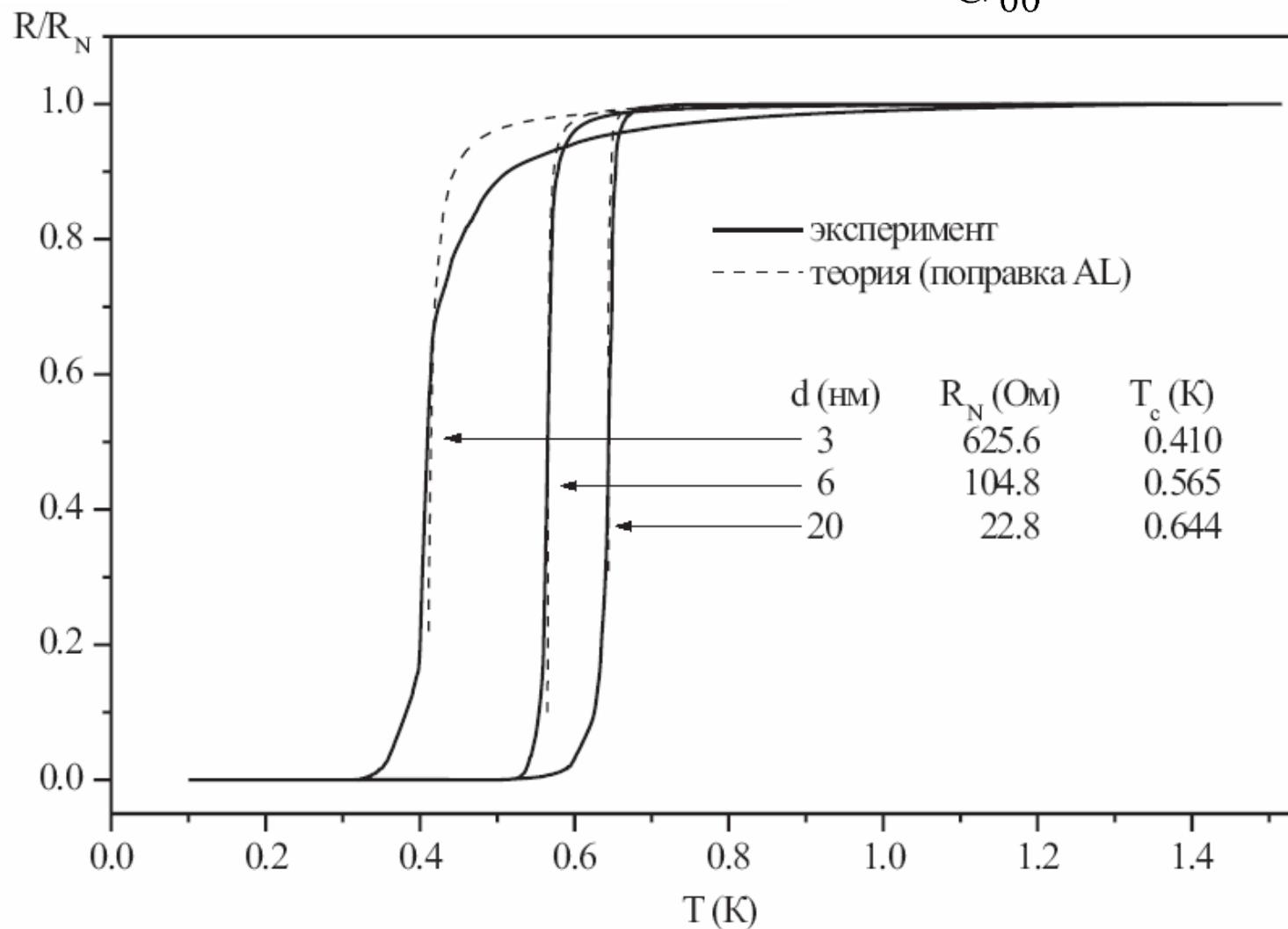
The basic parameters of the PtSi films



d нм	R_{\square} Ом	n 10^{22} см $^{-3}$	k_F 10^8 см $^{-1}$	E_F эВ	$\rho(E_F)$ 10^{46} Дж $^{-1}$ м $^{-3}$	τ 10^{-16} с	$k_F l$	l нм	D см 2 /с
3	625.6	3.6	1.0	4.0	8.5	5.3	6.4	0.6	2.5
6	104.8	7.0	1.3	6.1	10.7	8.2	15.4	1.2	5.9
20	22.8	9.4	1.4	7.5	11.7	8.2	18.7	1.3	7.2

$R(T)$ at $B = 0$

$$\frac{\Delta G^{AL}(T)|_{T \rightarrow T_c}}{G_{00}} = \frac{\pi^2}{8} \frac{T}{T - T_c}$$

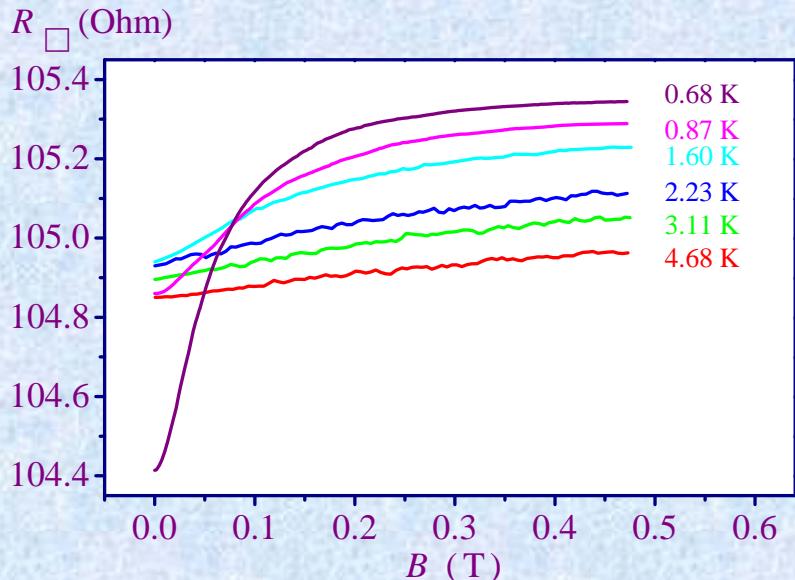


$$G_{00} = e^2 / (2\pi^2 \hbar)$$

$$\Delta R(T) \approx R^2 \Delta G(T)$$

Magnetoresistance

$R(B, T = T_i)$



WL

$$\frac{\Delta G^{WL}(B)}{G_{00}} = \alpha \cdot Y\left(\frac{4eB}{\hbar} l_\varphi^2\right)$$

$$G_{00} = e^2 / 2\pi^2 \hbar$$

$$Y(x) = \ln(x) + \Psi\left(\frac{1}{2} + \frac{1}{x}\right)$$

where $\Psi(z)$ is the digamma function

$\alpha = 1$, if $\tau_\varphi \ll \tau_{so}$ → negative MR
 $\alpha = -1/2$, if $\tau_\varphi \gg \tau_{so}$ → positive MR

MT

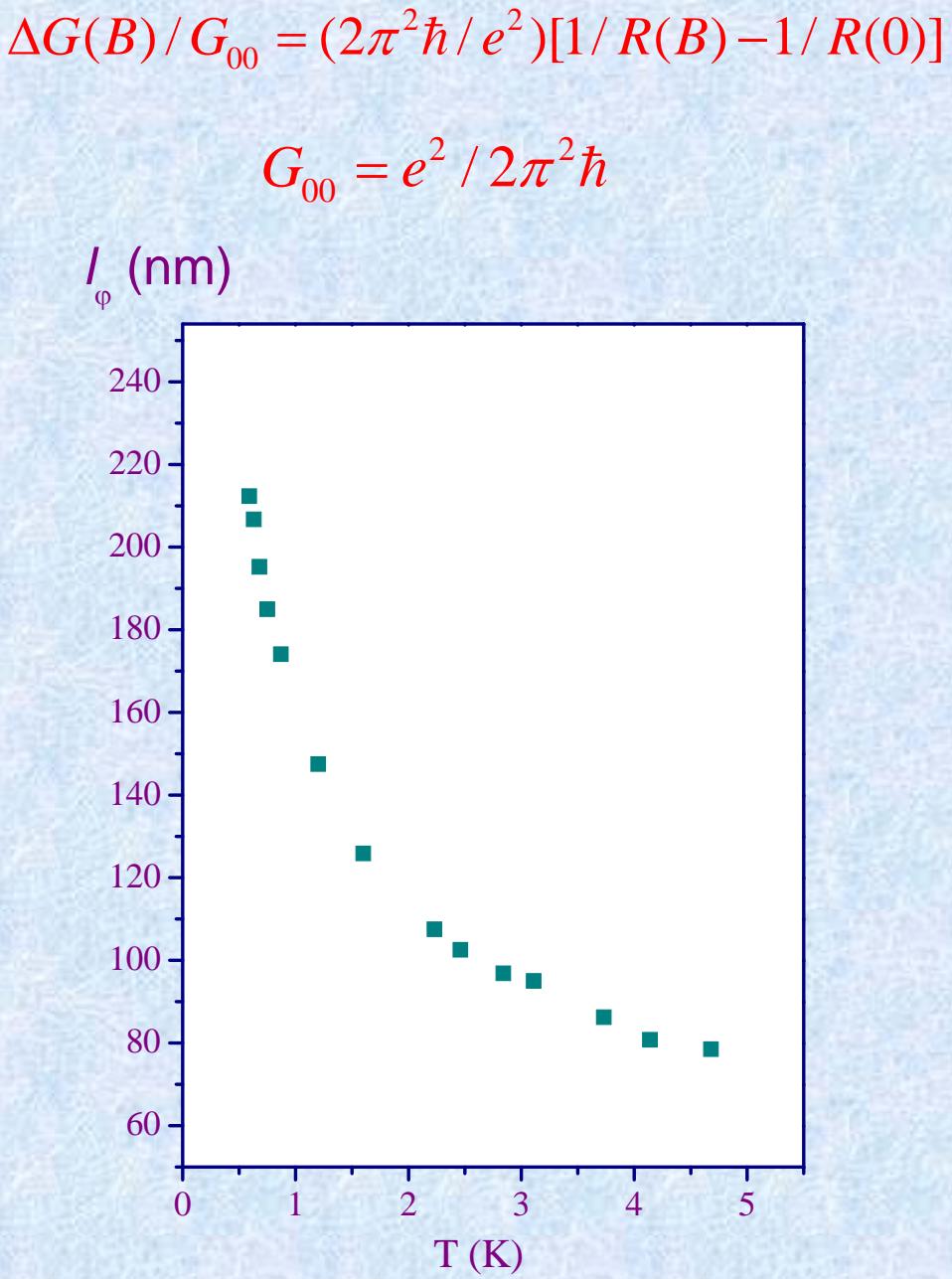
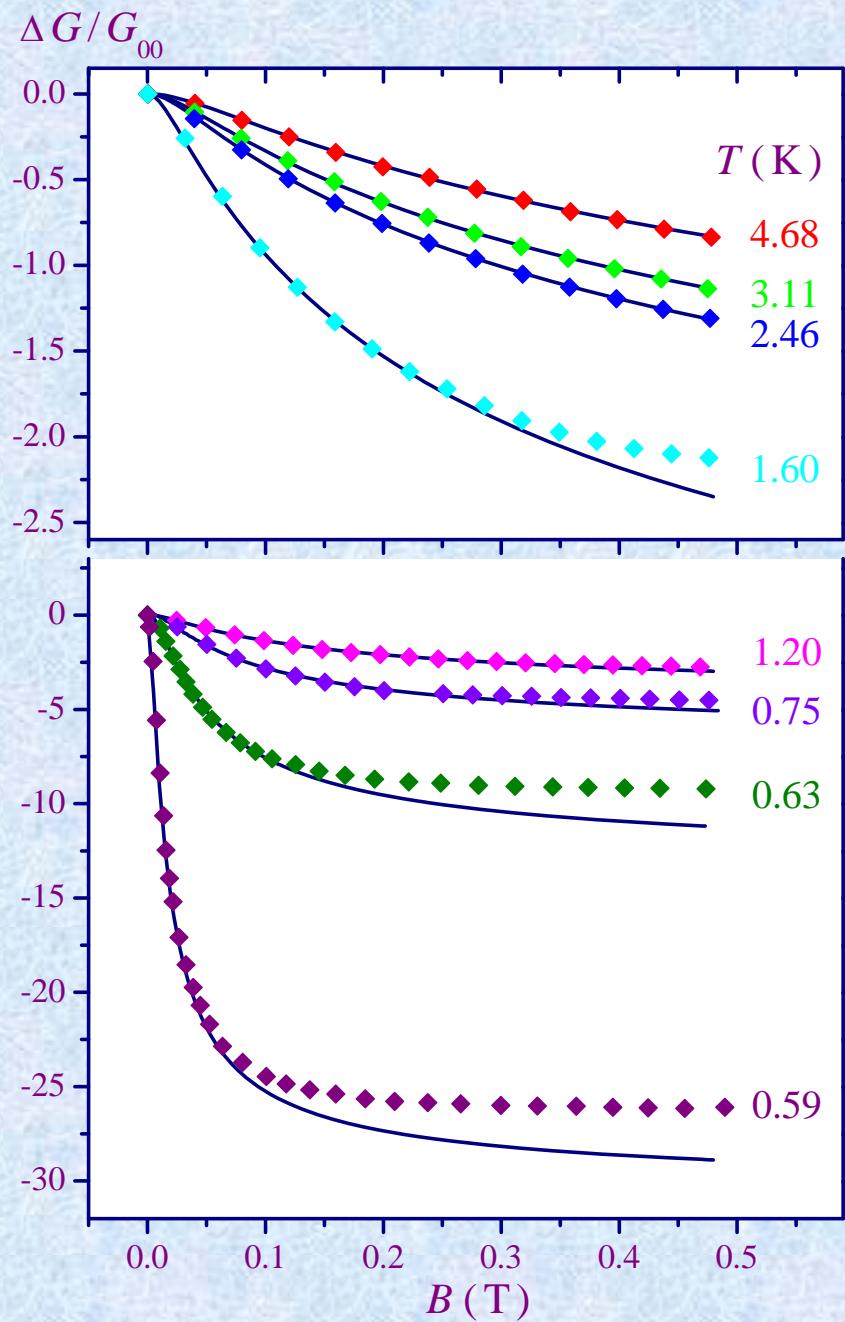
A.I. Larkin (1980)

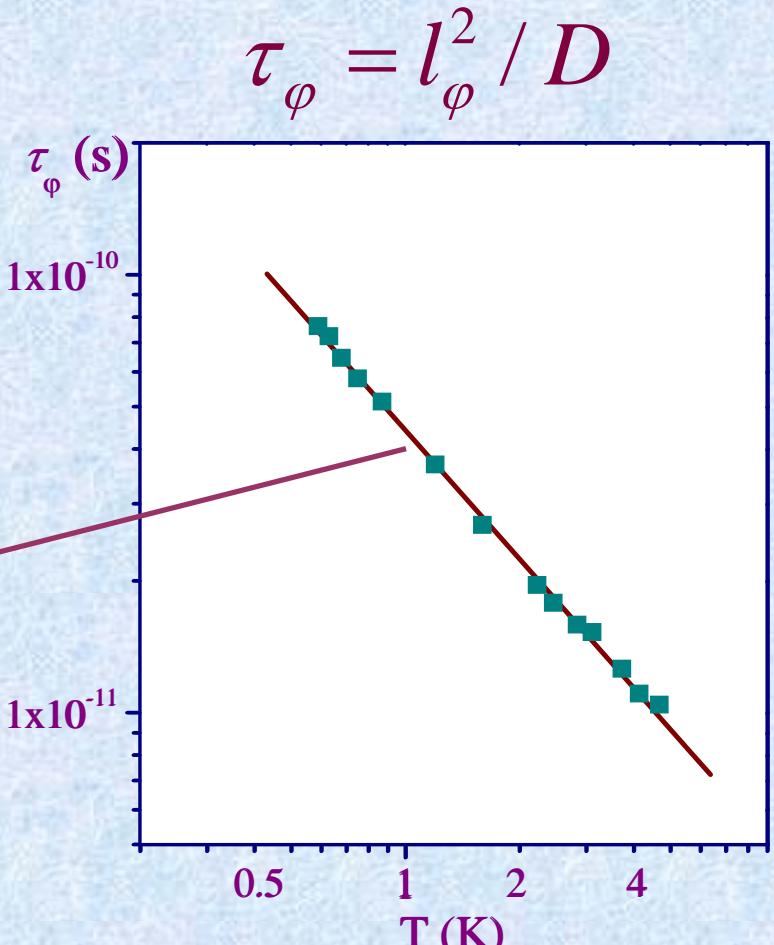
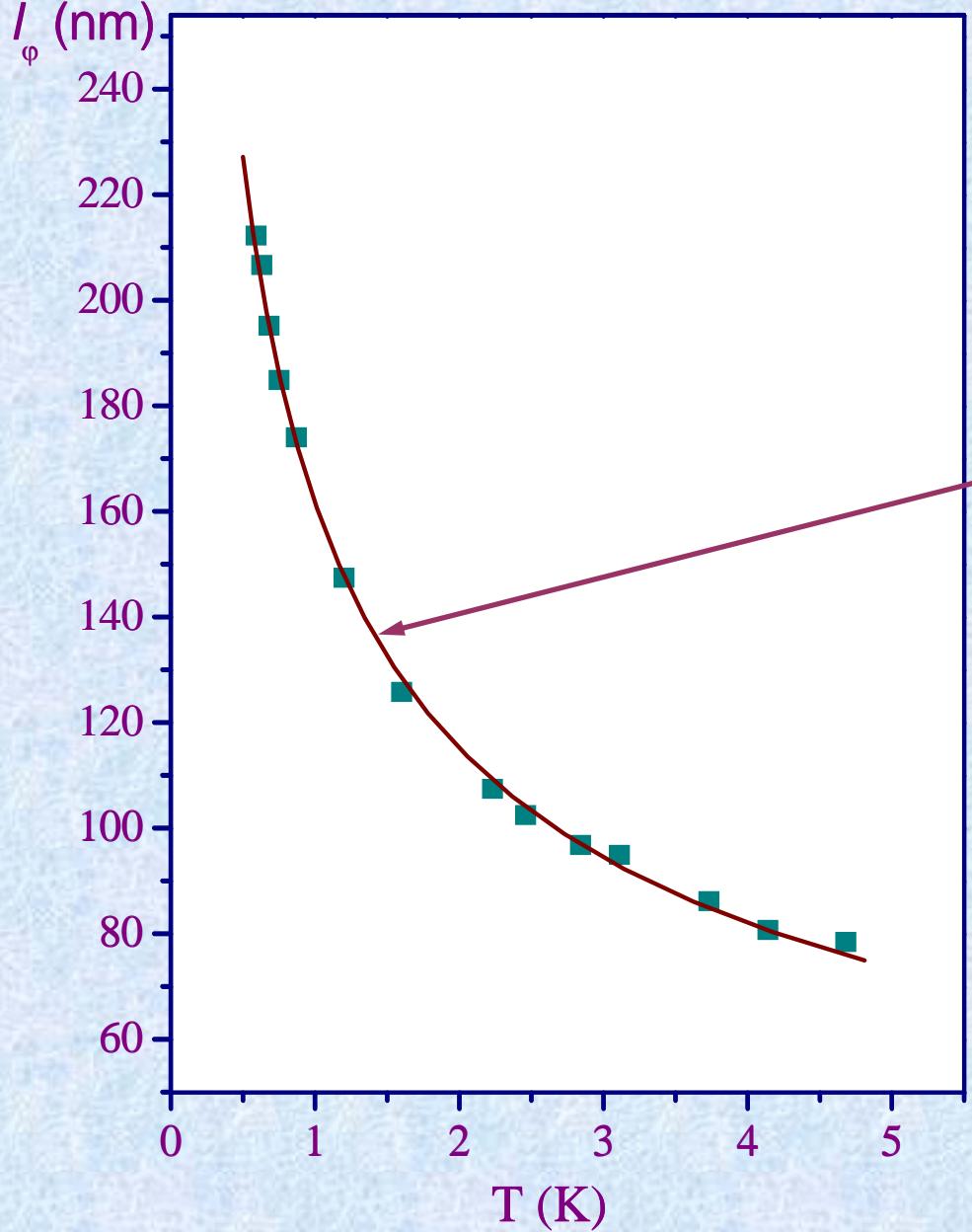
$$\frac{\Delta G^{MT}(B)}{G_{00}} = -\beta(T) \cdot Y\left(\frac{4eB}{\hbar} l_\varphi^2\right)$$

Restrictions: $\ln \frac{T}{T_c} \gg \frac{\hbar}{k_B T \tau_\varphi}$, $B \ll \frac{k_B T}{4De} \ln \frac{T}{T_c}$

Lopes dos Santos and Abrahams (1985)

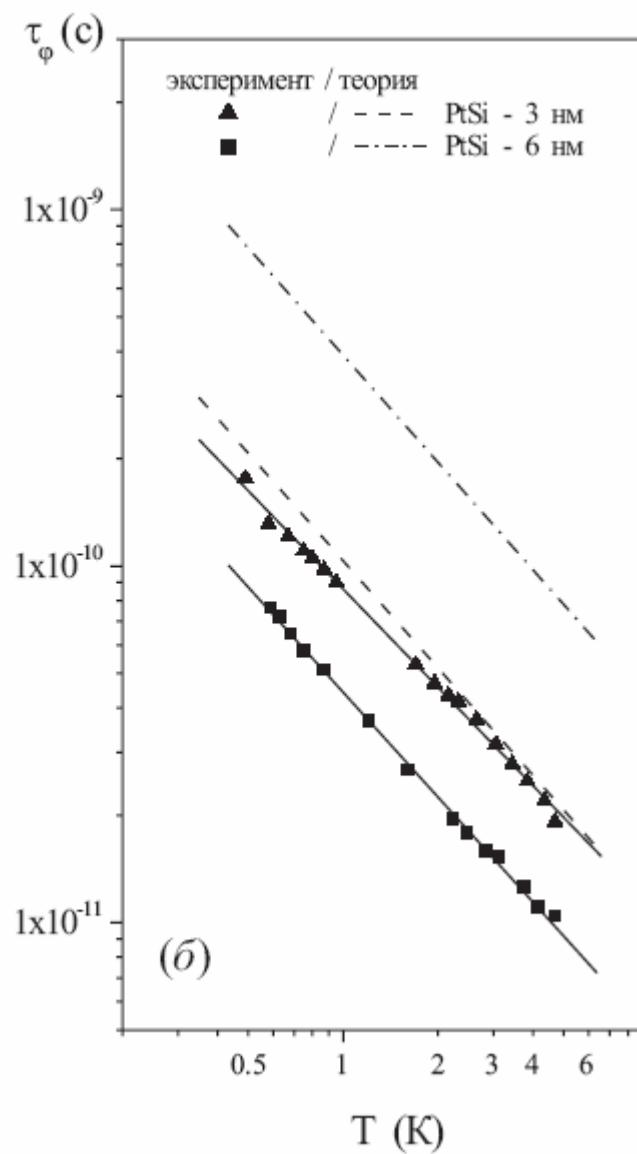
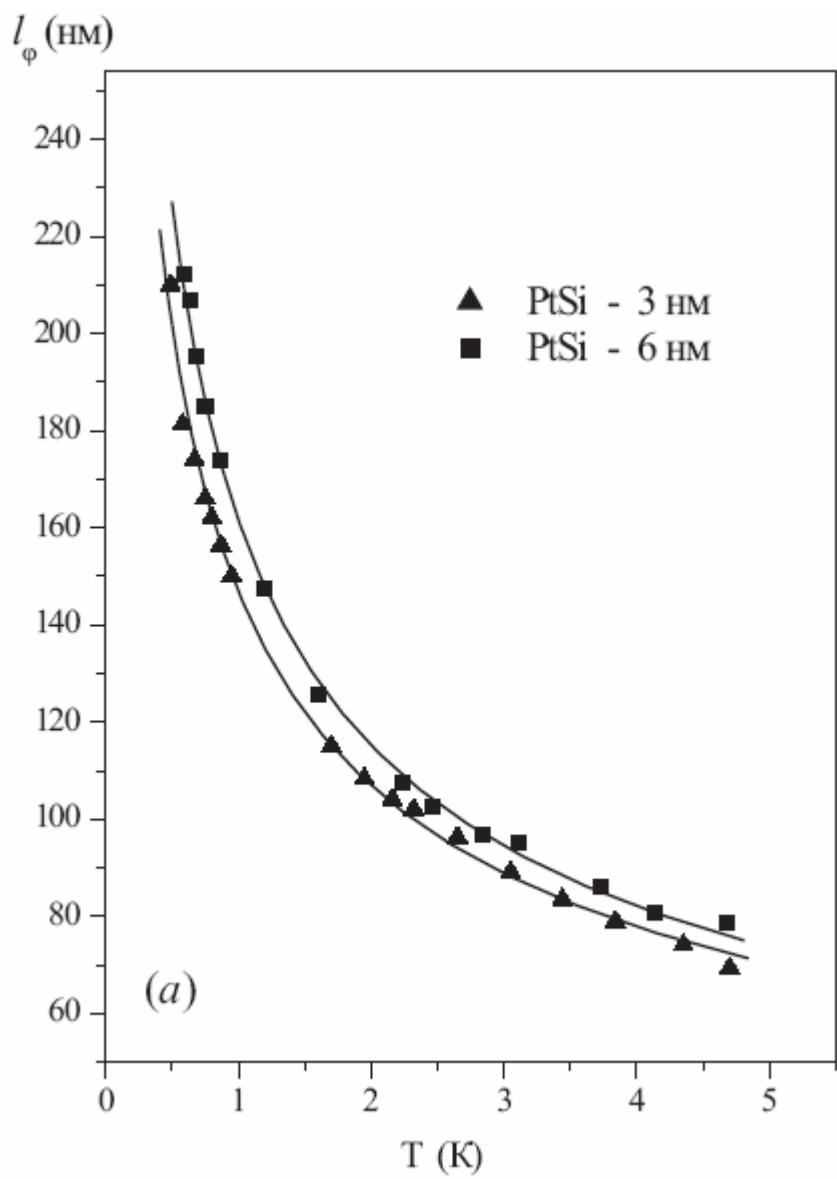
$$\frac{\Delta G^{MT}(B)}{G_{00}} = -\beta(T, \tau_\varphi) \cdot \left[Y\left(\frac{4eB}{\hbar} l_\varphi^2\right) - Y\left(\frac{\pi DeB}{2k_B T \ln(T/T_c)}\right) \right]$$





$$\tau_\varphi \propto T^{-p} \longrightarrow p = 0.98$$

$$\tau_\varphi^{-1} = \frac{\pi k T}{\hbar} \frac{e^2 R_\square}{2\pi^2 \hbar} \ln \frac{\pi \hbar}{e^2 R_\square}$$



$R(T)$ at $B = 0$

$$G_{00} = e^2/(2\pi^2 \hbar)$$

$$\frac{\Delta G^{WL}(T)}{G_{00}} = \alpha p \ln \left(\frac{kT\tau}{\hbar} \right)$$

$$\frac{\Delta G^{ID}(T)}{G_{00}} = \left[4 - 3 \frac{2+F}{F} \ln \left(1 + \frac{F}{2} \right) \right] \ln \left(\frac{kT\tau}{\hbar} \right)$$

$$\frac{\Delta G^{WL+ID}(T)}{G_{00}} = A \ln \left(\frac{kT\tau}{\hbar} \right)$$

$$\frac{\Delta G^{DOS}(T)}{G_{00}} = \ln \left[\frac{\ln(T_c/T)}{\ln(kT_c\tau/\hbar)} \right]$$

$$\frac{\Delta G^{AL}(T)|_{T \rightarrow T_c}}{G_{00}} = \frac{\pi^2}{8} \frac{T}{T - T_c}$$

$$\frac{\Delta G^{MT}(T)|_{T \gg T_c}}{G_{00}} = \beta(T) \ln \left(\frac{kT\tau_\varphi}{\hbar} \right)$$

$$\frac{\Delta G^{MT}(T)}{G_{00}} = \beta(T, \tau_\varphi) \ln \left(\frac{\ln(T/T_c)}{\delta} \right)$$

$$\delta = \frac{\pi \hbar}{8kT\tau_\varphi}$$

$$T_c < T < \hbar(k\tau_\varphi)^{-1}$$

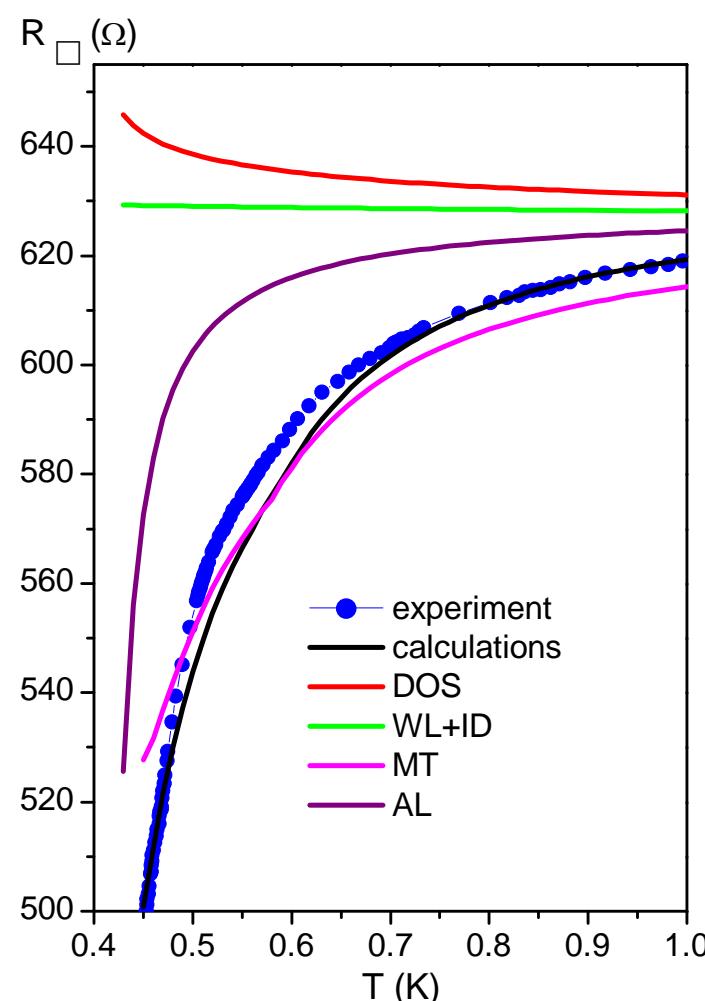
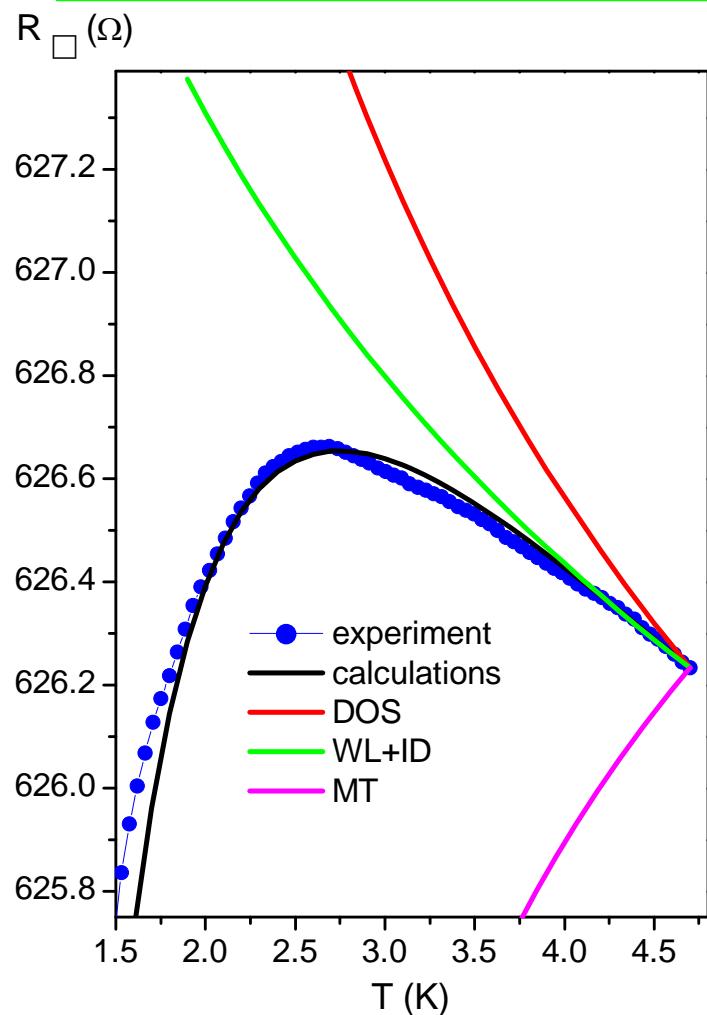
AL

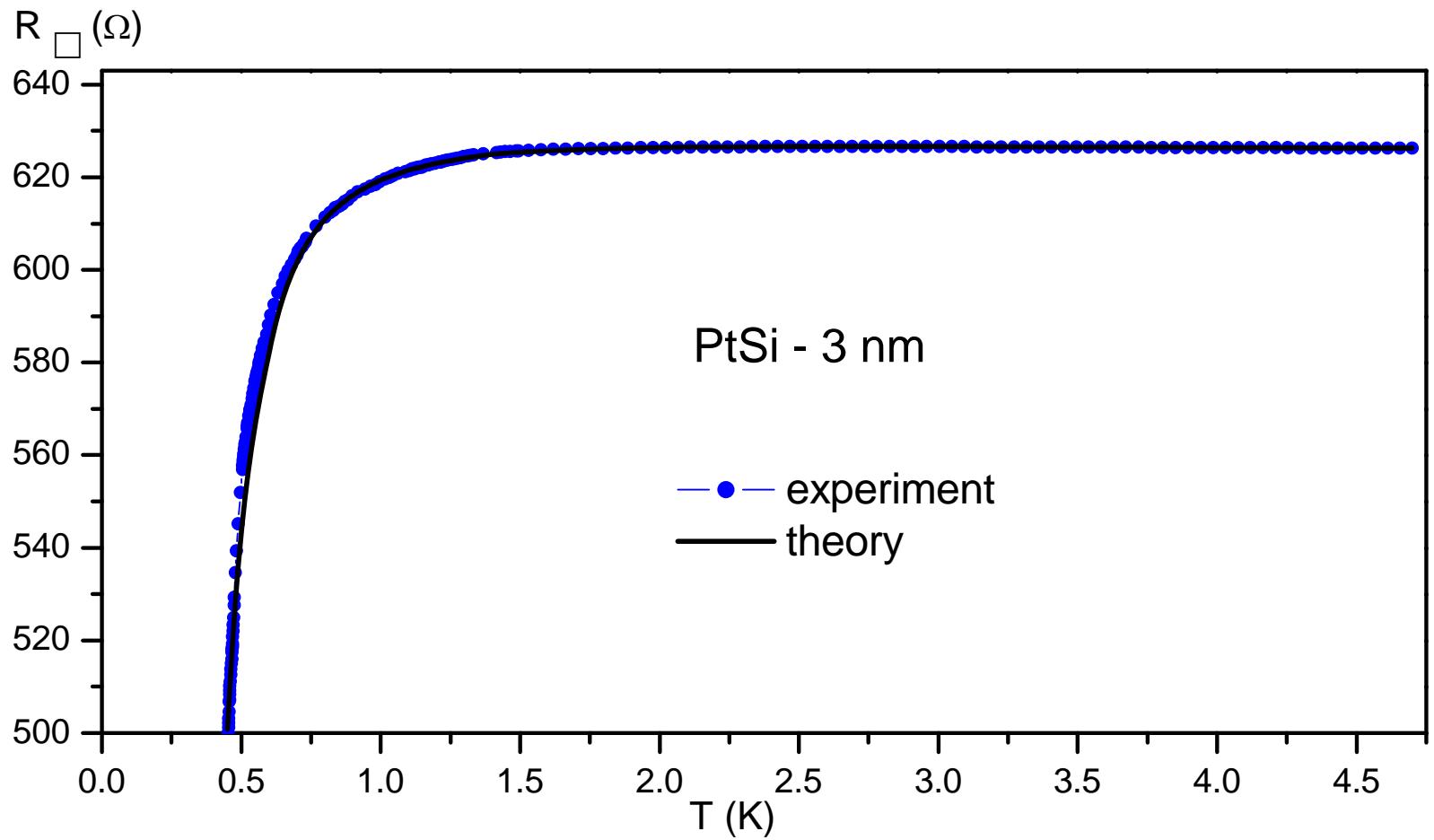
$$\hbar(k\tau_\varphi)^{-1} < T < 2T_c$$

MT, AL, DOS, ID, WL

$$T > 2T_c$$

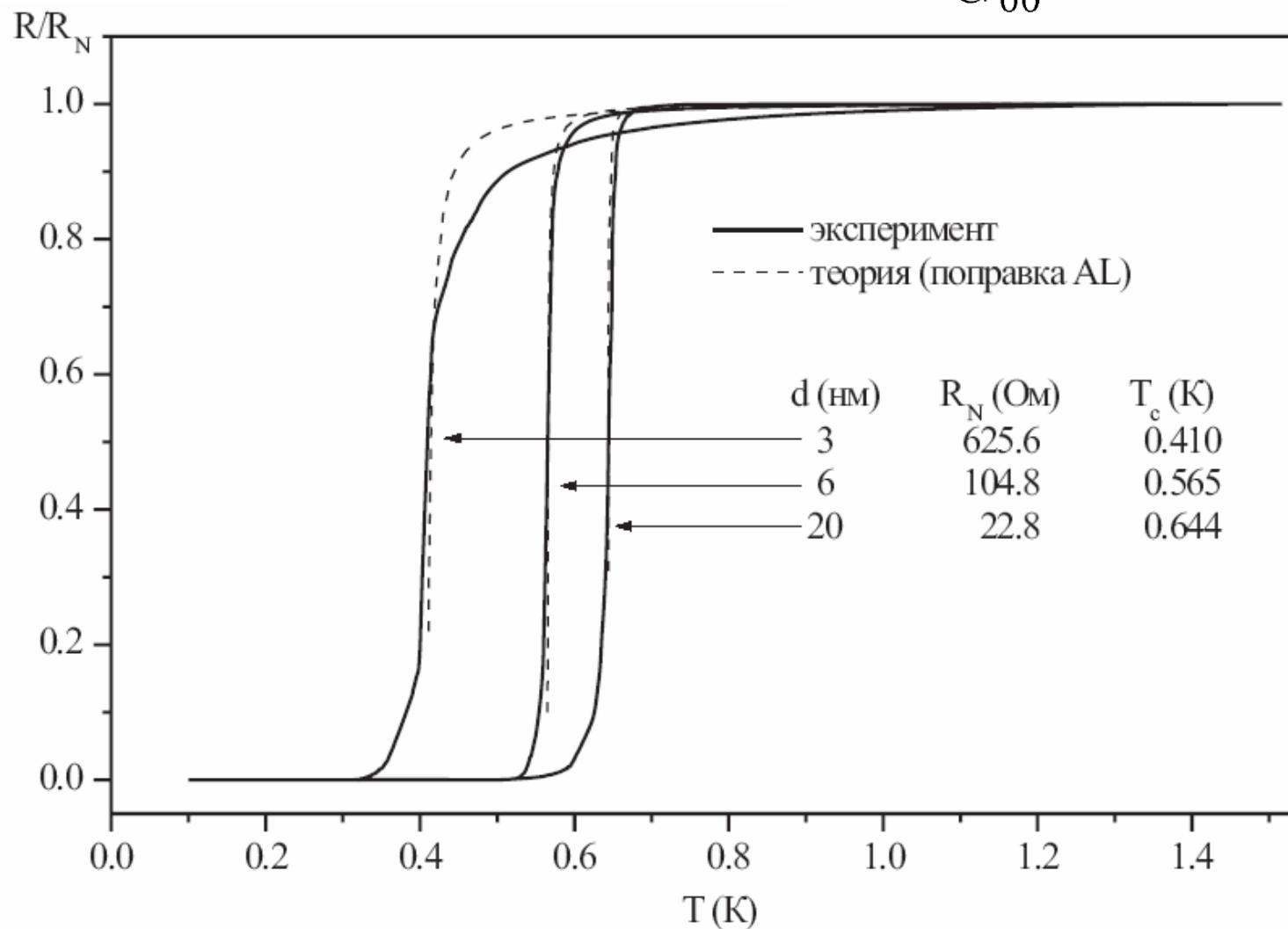
$ID, WL, DOS, MT.$

$T_c < T < \hbar(k\tau_\varphi)^{-1}$ AL $\hbar(k\tau_\varphi)^{-1} < T < 2T_c$ MT, AL, DOS, ID, WL $T > 2T_c$ $ID, WL, DOS, MT.$ 



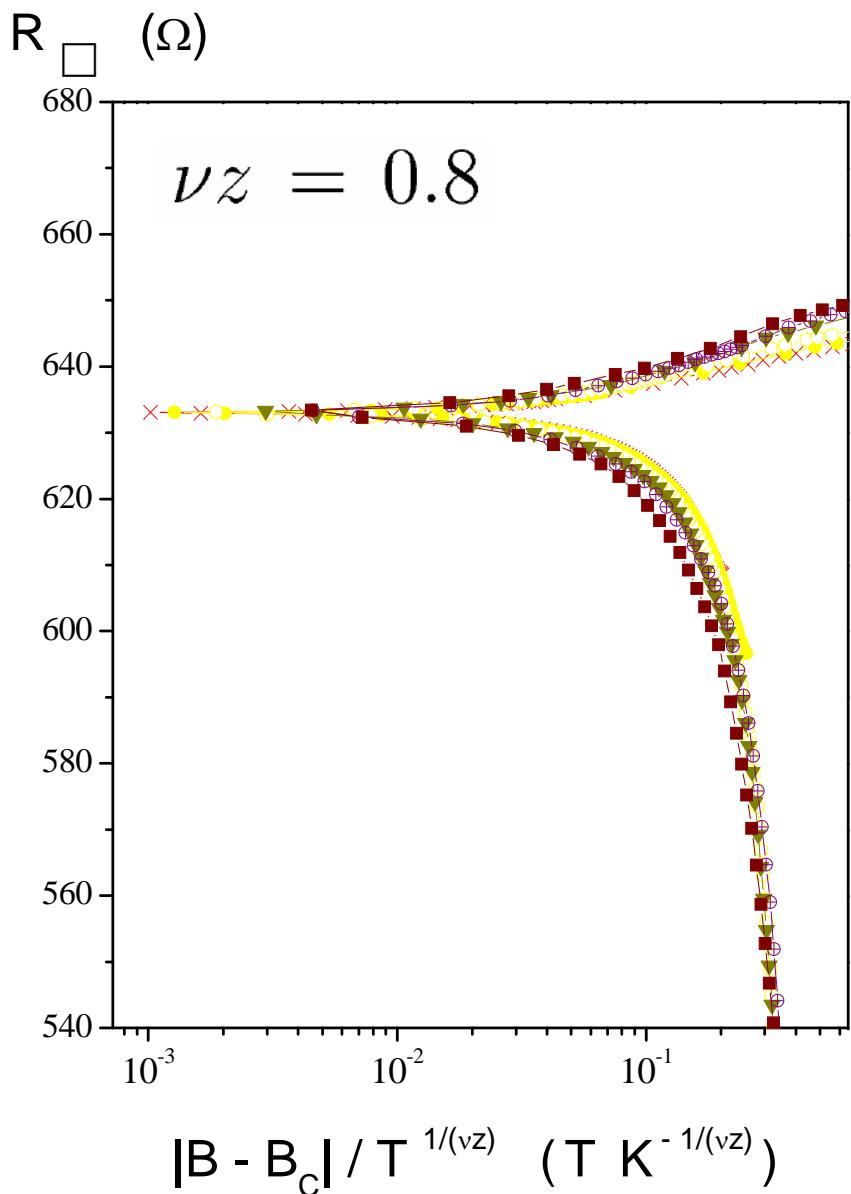
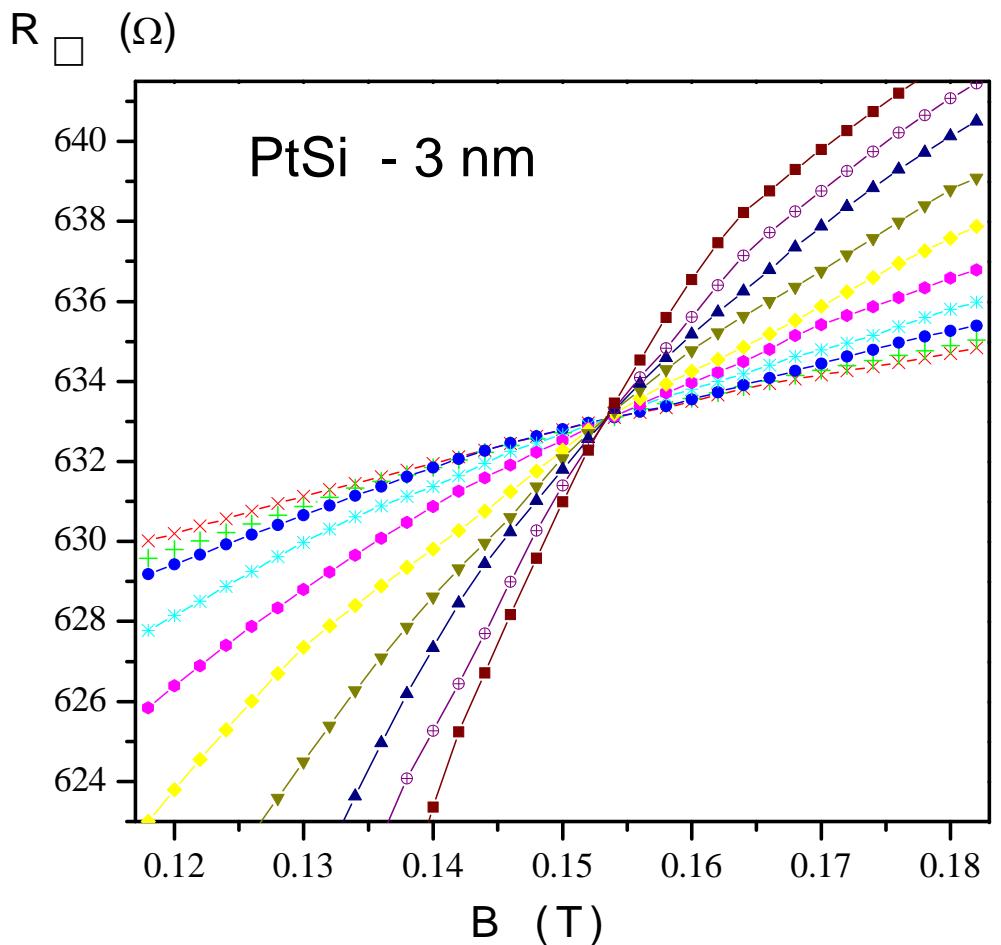
$R(T)$ at $B = 0$

$$\frac{\Delta G^{AL}(T)|_{T \rightarrow T_c}}{G_{00}} = \frac{\pi^2}{8} \frac{T}{T - T_c}$$



$$G_{00} = e^2 / (2\pi^2 \hbar)$$

$$\Delta R(T) \approx R^2 \Delta G(T)$$



$$R(T, B) = R_c \cdot f \left(\frac{|B - B_c|}{T^{1/\nu z}} \right)$$



Suppression of Superconductivity by Disorder

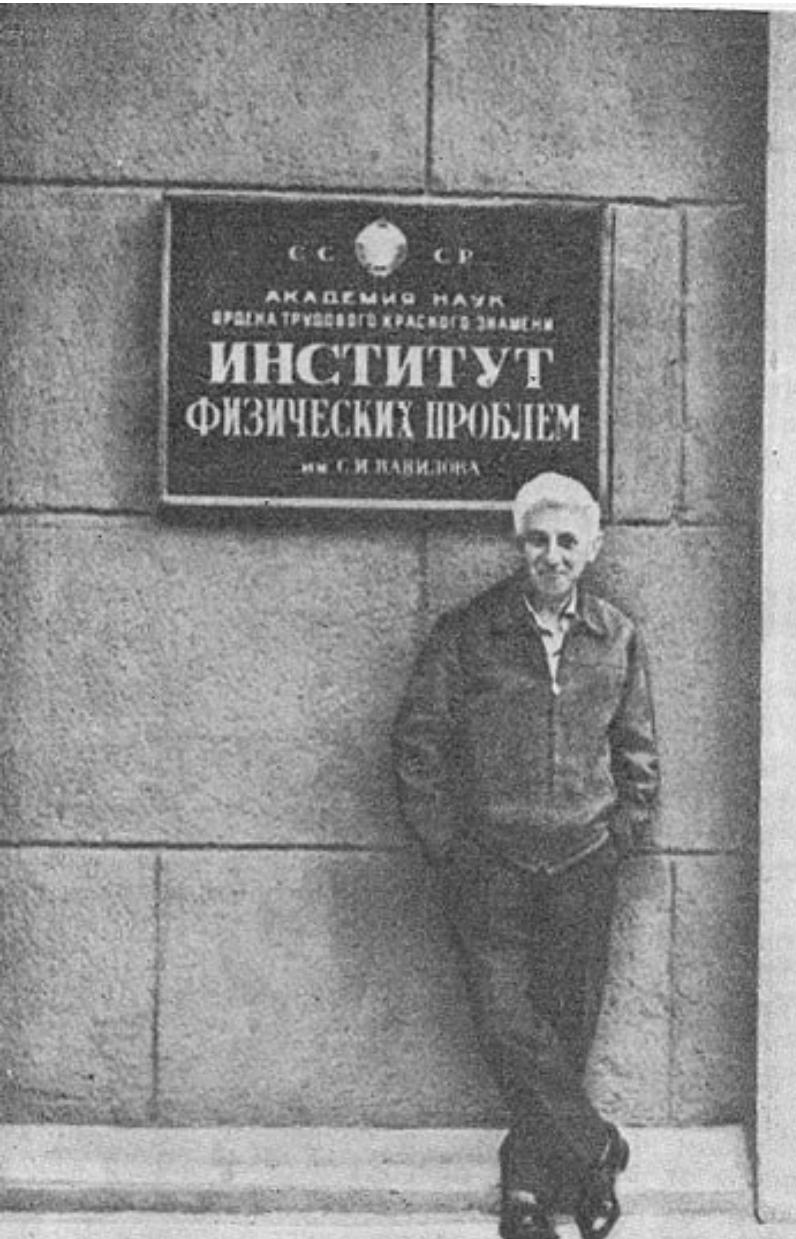
- Superconductor – Metal – Insulator transition (**SMIT**)



- Superconductor – Insulator transition (**SIT**)



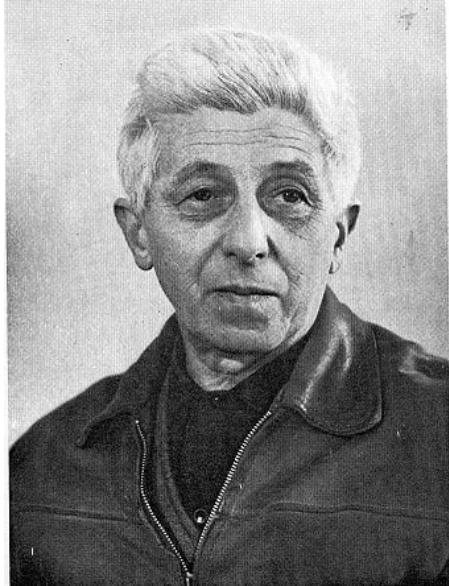
Suppression of Superconductivity by Disorder



The first studies of superconductivity in the presence of disorder were performed by A.I. Shalnikov (Institute for Physical Problems, Russia).

A. Shalnikov, Nature **142**, 74 (1938).
A.I. Shalnikov, ZhETF **10**, 630 (1940).

Suppression of Superconductivity by Disorder

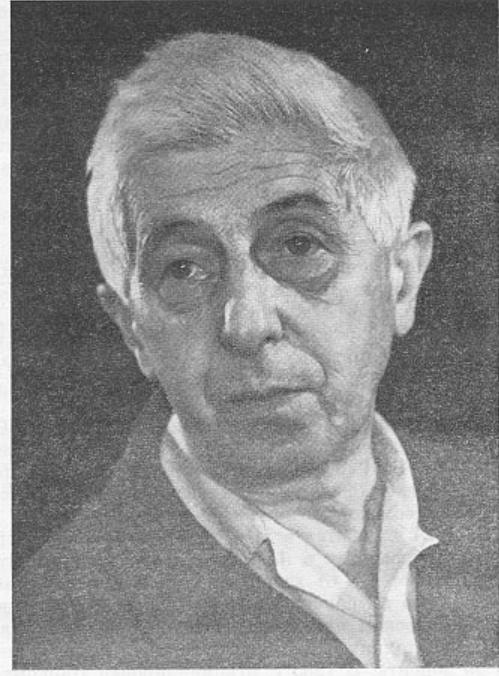


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A. Shalnikov, Nature **142**, 74 (1938).
A.I. Shalnikov, ZhETF **10**, 630 (1940).

Amorphous metals:
lead (**Pb**), tin (**Sn**) and thallium (**Tl**) films
with thickness between 1 (!) and 200 nanometers

This was the first observation of suppression of T_c with decreasing thickness in thin superconducting films



Suppression of Superconductivity by Disorder

The first studies of superconductivity in the presence of disorder were performed by A.I. Shalnikov
(Institute for Physical Problems, Russia).

A. Shalnikov, Nature **142**, 74 (1938)
A.I. Shalnikov, ZhETF **10**, 630 (1940)

Мы не можем привести зависимости, характеризующей влияние толщины пленки на критическую температуру перехода. Нами были сделаны качественные эксперименты, в которых мы получали пленки различных толщин, последовательно испаряя все новые и новые количества металла в одном и том же приборе. Первая, самая тонкая пленка ($d \sim 10^{-7}$ см) оказалась сверхпроводящей при $\sim 4.1^\circ\text{K}$. Следующая, более толстая ($d = 10^{-6}$ см) при 4.5°K и, наконец, пленка толщиной около $3 \cdot 10^{-5}$ см при 4.9°K .

Anderson's theorem

predicts that nonmagnetic impurities
have **no effect** on superconductivity

A.A. Abrikosov and L.P. Gorkov, Sov. Phys. JETP 8, 1090 (1958).

P.W. Anderson, J. Phys. Chem. Solid 11, 26 (1959).

at relatively weak disorder $l \gg v_F/\omega_D$

This theorem does not consider

the strengthening
of electron-electron
interaction
with increasing disorder

the effect
of Anderson localization

weak disorder

strong disorder

Suppression of Superconductivity by Disorder

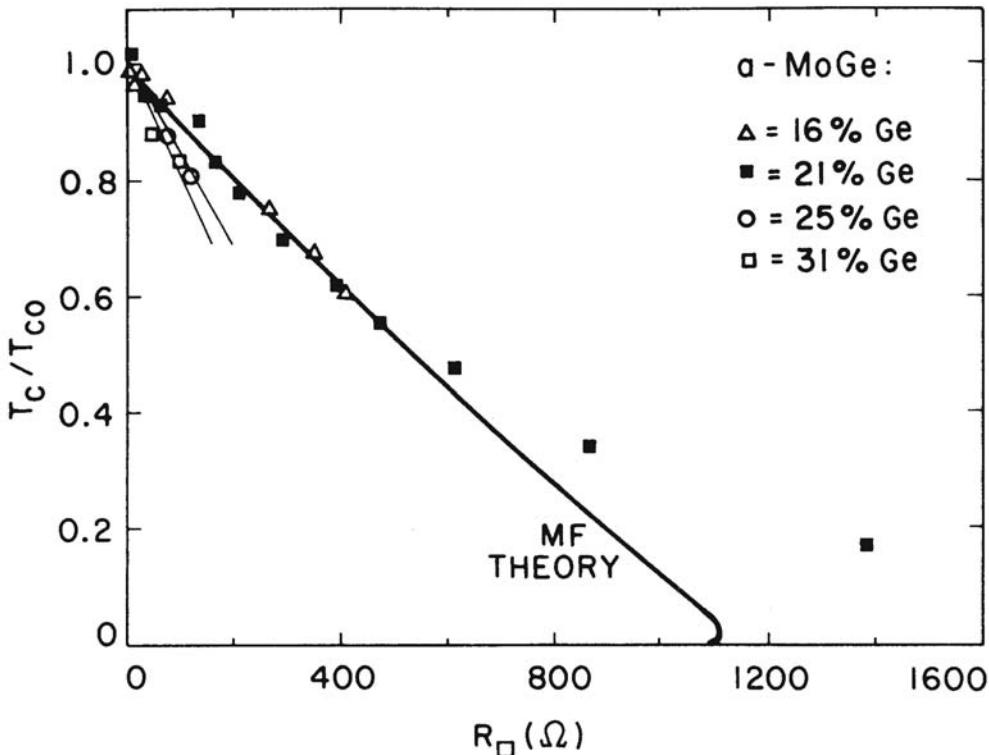
weak disorder

Theory

- S. Maekawa, H. Fukuyama,
J. Phys. Soc. Jpn. **51**, 1380 (1982).
S. Maekawa, H. Ebisawa, H. Fukuyama,
J. Phys. Soc. Jpn. **52**, 1352 (1983).
H. Takagi and Y. Kuroda,
Solid State Comm. **41**, 643 (1982).

Experiment

- J.M. Graybeal and M.R. Beasley,
PRB **29**, 4167 (1984).



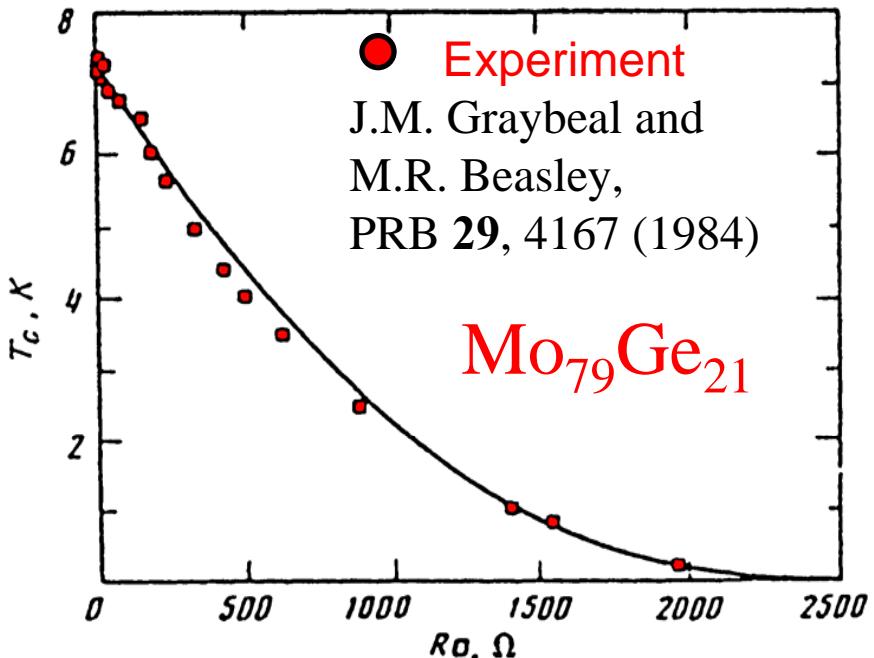
$$\ln\left(\frac{T_c}{T_{c0}}\right) = -\frac{1}{2}gr \left[\ln\left(\frac{\hbar}{kT_c\tau}\right) \right]^2 - \frac{1}{3}gr \left[\ln\left(\frac{\hbar}{kT_c\tau}\right) \right]^3$$

$$r = G_{00} \cdot R_\square \quad G_{00} = e^2 / (2\pi^2 \hbar)$$

weak disorder

Theory

A.M. Finkel'stein, JETP Lett. 45, 46 (1987).



The physical mechanism:

the decrease of the dynamical screening of the Coulomb repulsion between electrons because of the diffusive character of their motion in dirty systems

=> the decrease of the net attraction between electrons

=> the decrease of the transition temperature

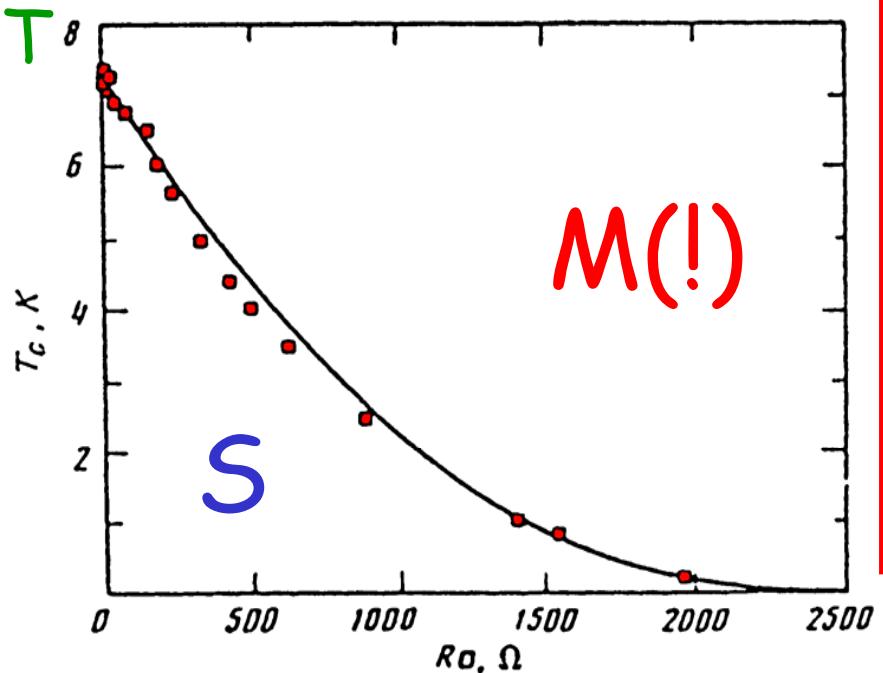
$$\ln \left(\frac{T_c}{T_{c0}} \right) = \frac{1}{|\gamma|} - \frac{1}{\sqrt{2r}} \ln \left(\frac{\gamma - r/4 - \sqrt{r/2}}{\gamma - r/4 + \sqrt{r/2}} \right)$$

$$m^* \propto \hbar/D$$

$$r = G_{00} \cdot R_\square$$

$$G_{00} = e^2 / (2\pi^2 \hbar) \quad \gamma = 1 / \ln(kT_{c0}\tau/\hbar)$$

weak disorder



Theory

A.M. Finkel'stein, JETP Lett. 45, 46 (1987).

Fermionic mechanism

Vanishing of T_c is accompanied by vanishing of the amplitude of the superconductive order parameter Δ (!)

Phase diagram

There is no Cooper pairs at the transition.

Review: A.M. Finkel'stein, Physica B 197, 636 (1994).

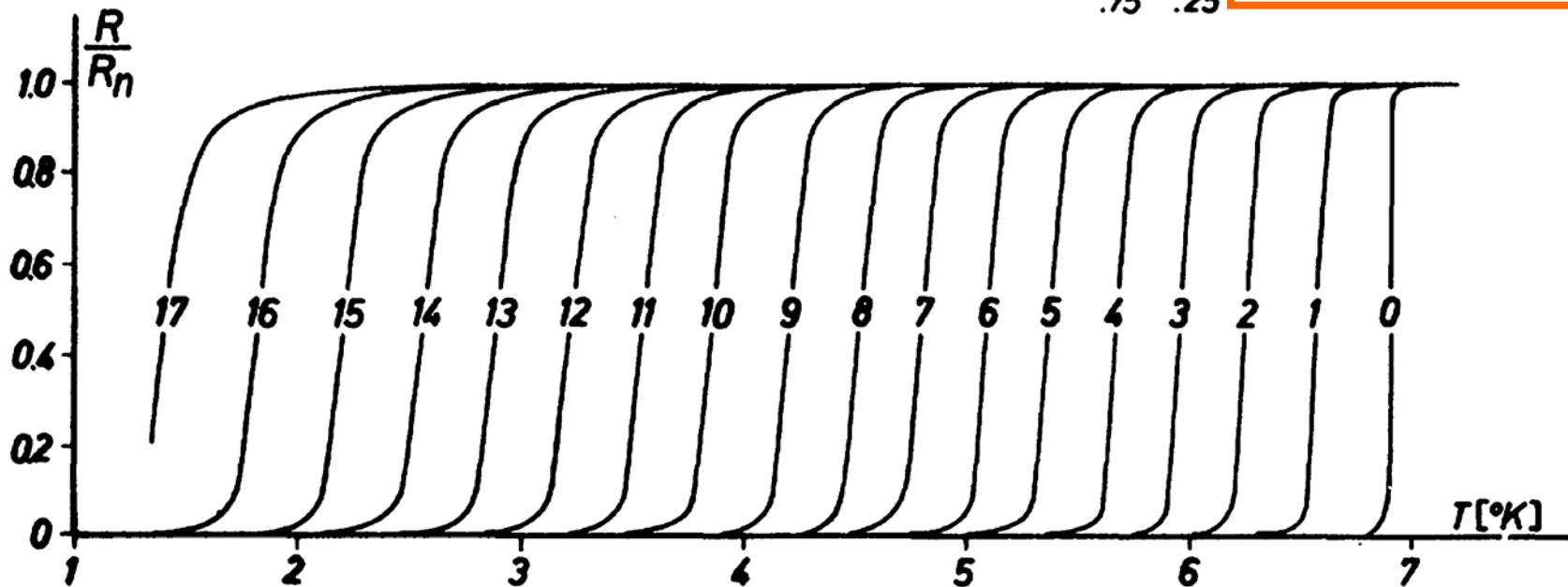
Suppression of Superconductivity by Magnetic field

Field-induced

*superconductor – normal metal
transition*

$Pb_{.75}Bi_{.25}$

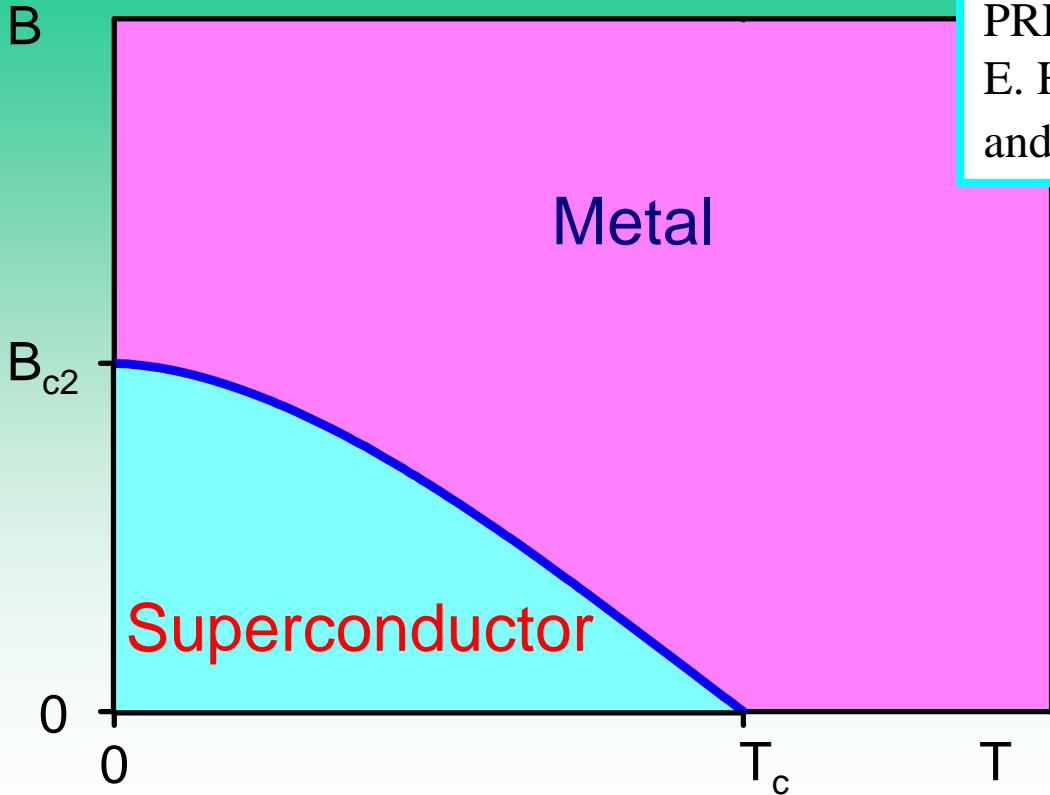
G. Bergmann,
PRB 7, 4850 (1973)



Field-induced

superconductor – normal metal transition

Phase diagram



Temperature dependence of the superconducting critical field, B_{c2}

E. Helfand and N.R. Werthamer,
PRL 13, 686 (1964); PR 147, 288 (1964);
E. Helfand, N.R. Werthamer,
and C. Hohenberg, PR 147, 295 (1964).

$$B_{c2}(0) = \frac{\pi}{2\gamma} \cdot \frac{kT_c}{eD}$$

$$\gamma = 1.781$$

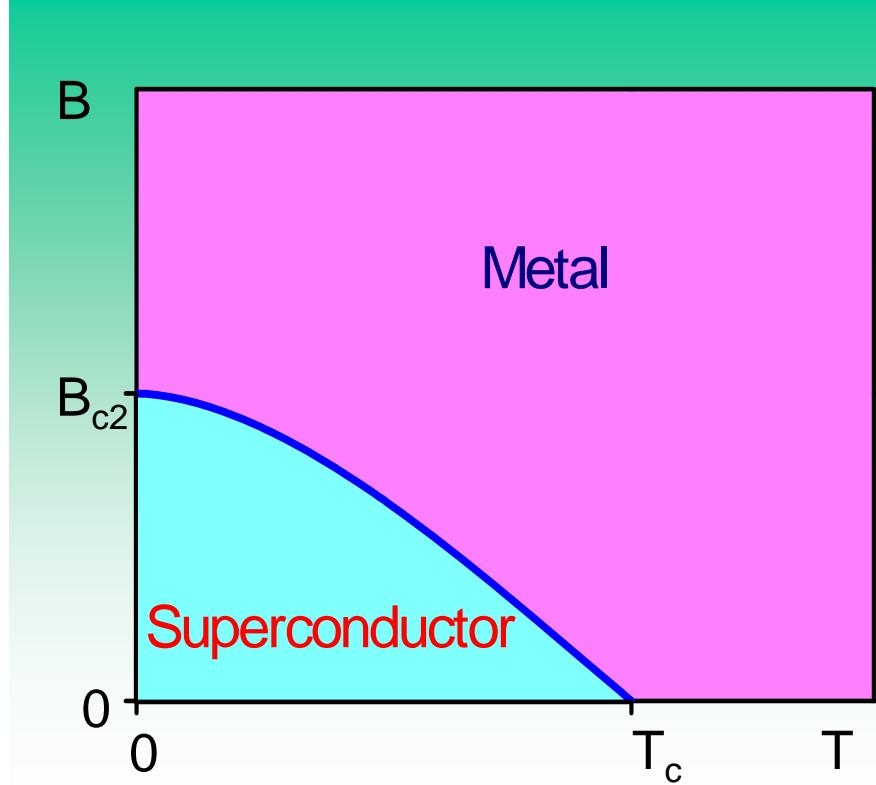
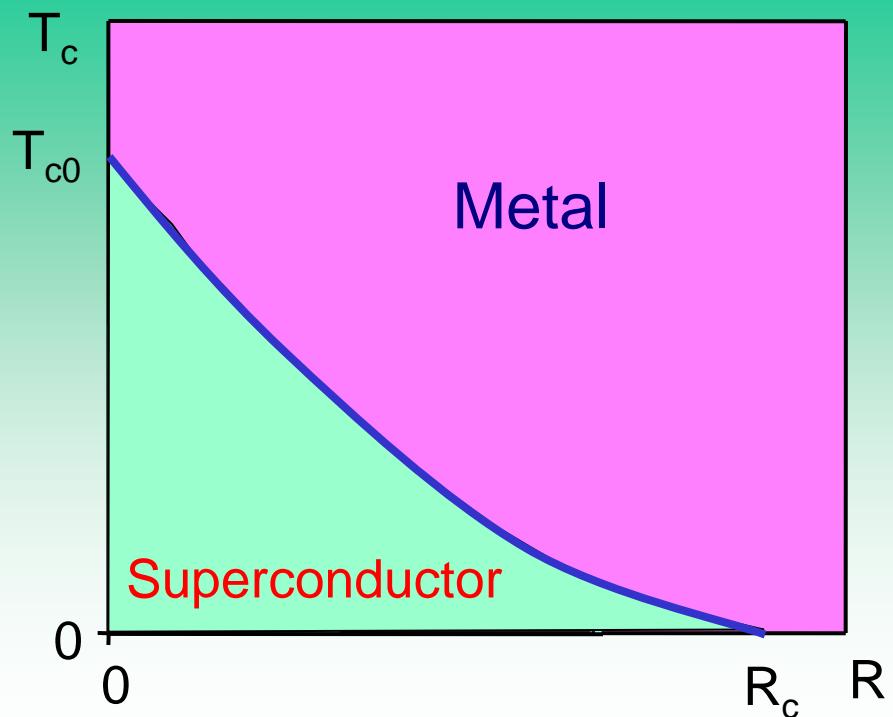
$$-\left. \frac{dB_{c2}}{dT} \right|_{T=T_c} = \frac{4k}{\pi e D}$$

Suppression of Superconductivity by Disorder & Magnetic field

superconductor – normal metal transition

A.M. Finkel'stein,
JETP Lett. 45, 46 (1987).

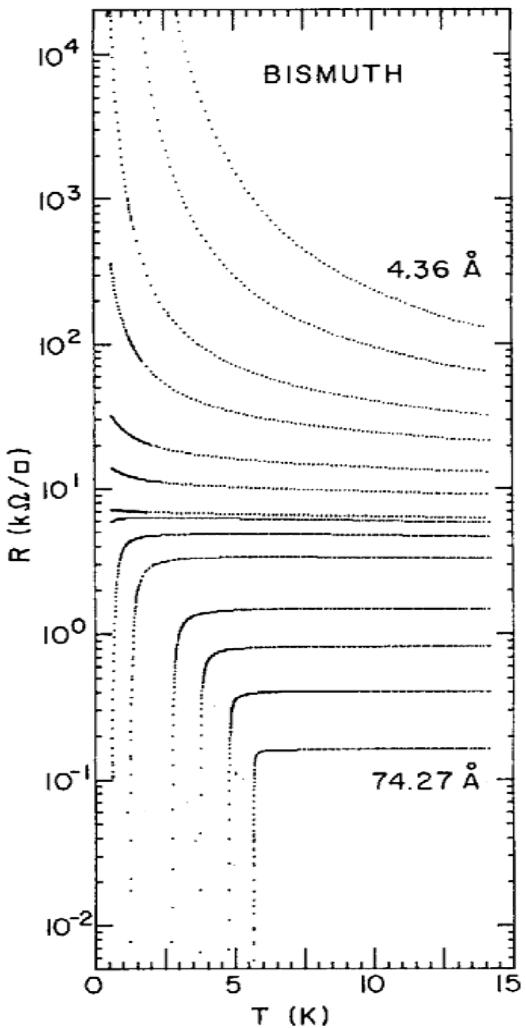
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PRL 13, 686 (1964); PR 147, 288 (1964);
E. Helfand, N.R. Werthamer,
and C. Hohenberg, PR 147, 295 (1964).



New era!!!

Suppression of Superconductivity by Disorder

strong disorder



D.V. Haviland, Y. Liu, A.M. Goldman,
PRL **62**, 2180 (1989).

Superconductor-insulator transition

$d < d_c$ Insulator

d_c Metal

$d > d_c$ Superconductor

Bi films
 $R_c = 6.45 \text{ k}\Omega$

$R_c = h/(2e)^2$

Fan-shaped curves

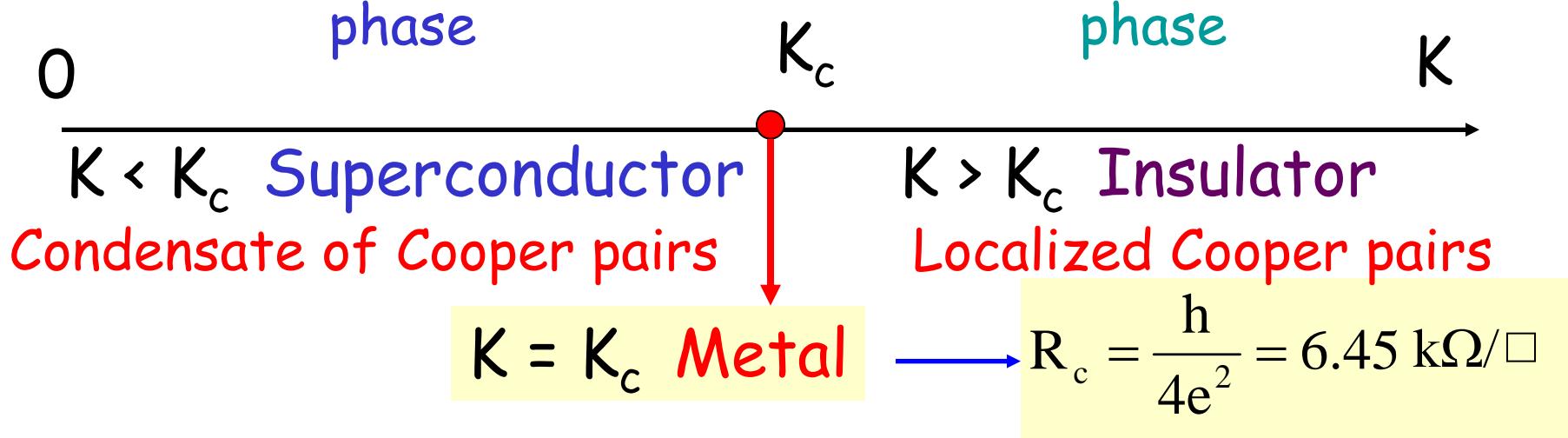
Bosonic mechanism

*** Quantum phase transition ***

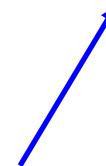
Theory

Matthew P.A. Fisher, G. Grinstein, S.M. Girvin , PRL **64**, 587 (1990).

Continuous zero-temperature phase transition

Quantum ordered
phaseQuantum disordered
phase

The system behaves like a normal metal right at the transition.

The resistance has a finite, nonzero value at $T = 0$.This value is *universal* - independent of all microscopic details.

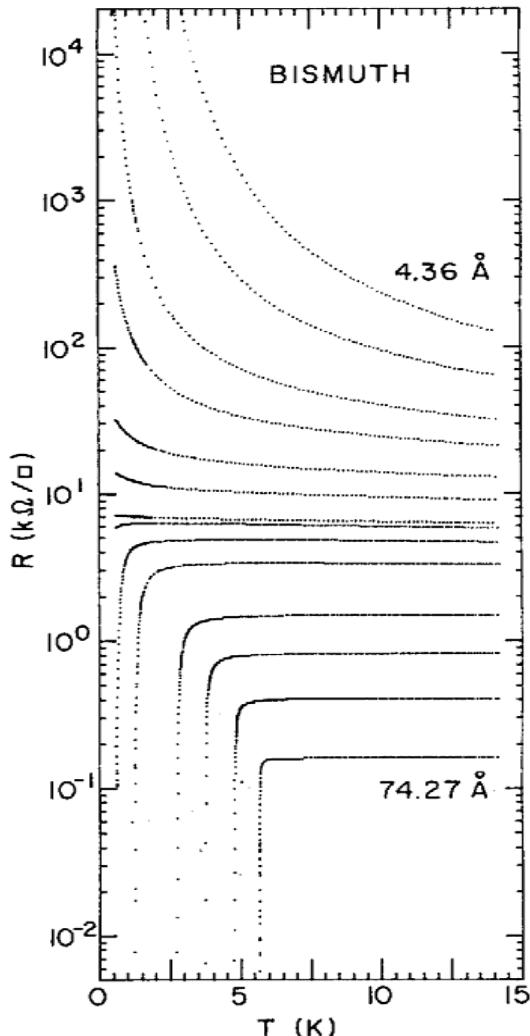
picture-gallery

“In search of disorder-driven
superconductor-insulator
transition”

*** collection ***

Suppression of Superconductivity by Disorder

D.V. Haviland, Y. Liu, and A.M. Goldman,
PRL 62, 2180 (1989).



$d < d_c$ Insulator

d_c Metal

$d > d_c$ Superconductor

Bi films
 $R_c = 6.45 \text{ k}\Omega$

$$R_c = h/(2e)^2$$

Fan-shaped curves

The onset of superconductivity in homogeneous ultrathin films is found to occur when their normal-state sheet resistance falls below a value close to $h/4e^2$, the quantum resistance for pairs. The data fur-

Suppression of Superconductivity by Disorder

Bi films $R_c = 6.45 \text{ k}\Omega$

Y. Liu, D.V. Haviland, B. Nease, and A.M. Goldman,
PRB **47**, 5931 (1993).

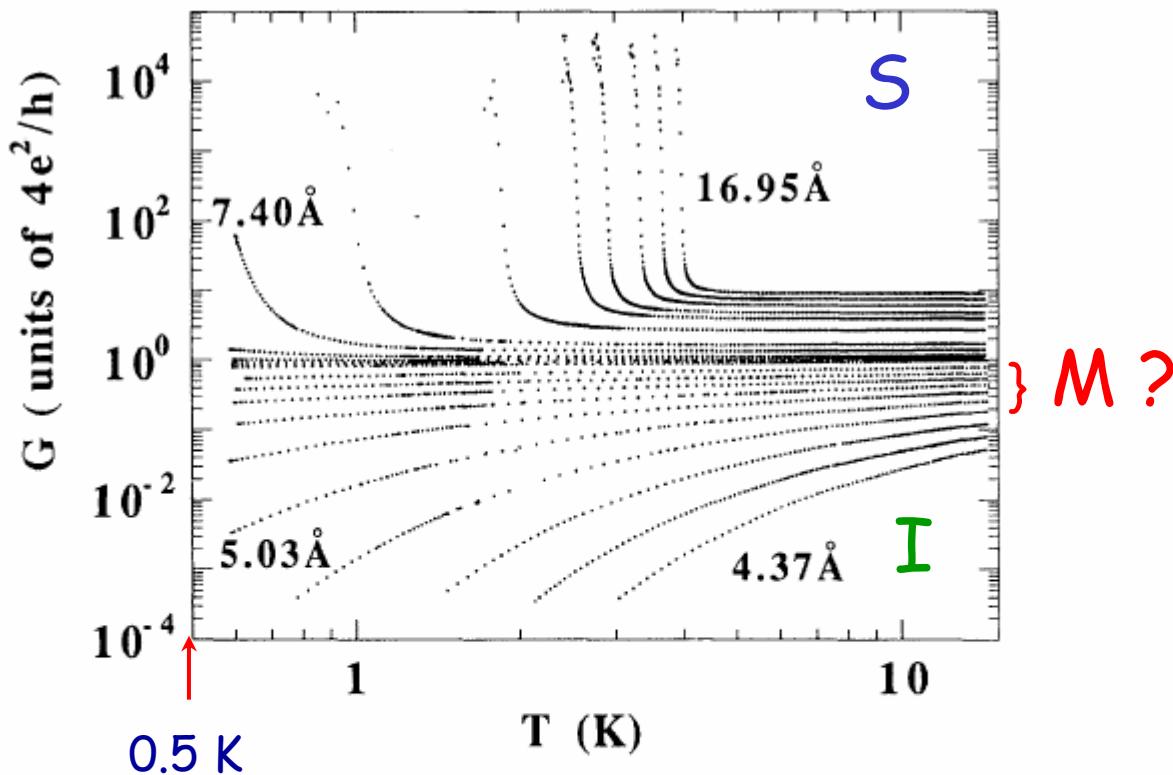
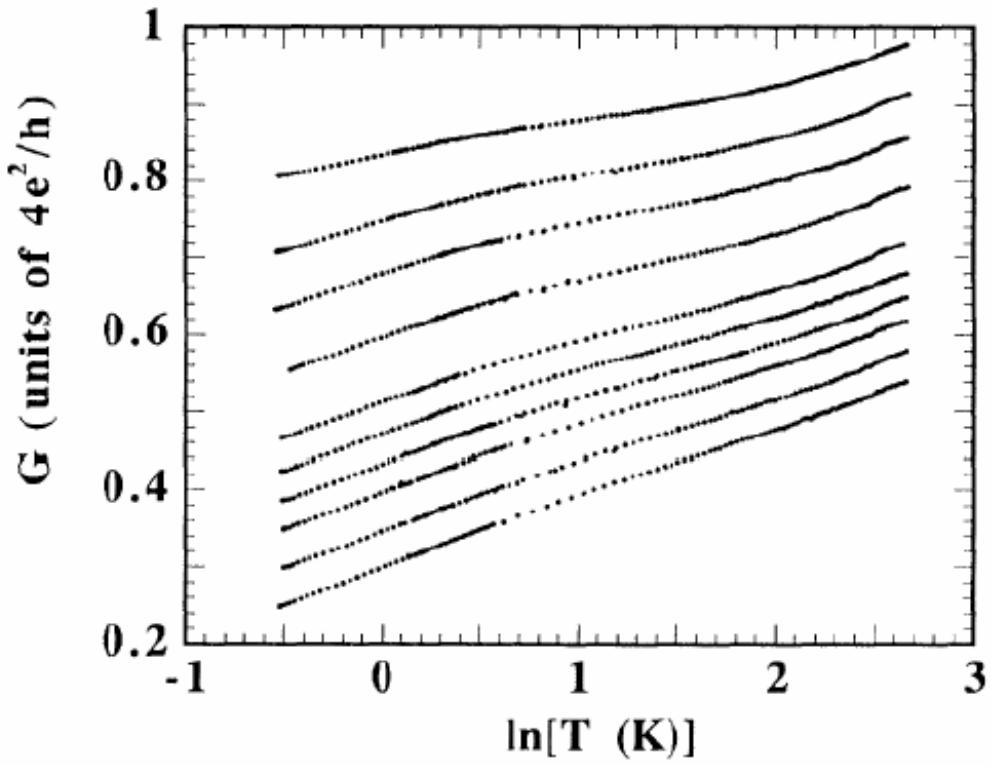


FIG. 2. Evolution for Bi films of the electrical conductance G in units of $4e^2/h$ as a function of temperature T . The thicknesses of a few selected films are indicated. Note that conductance and conductivity are identical in two dimensions. Only some of the data of the sequence of films is shown to avoid too high a density of data points.

Suppression of Superconductivity by Disorder

Bi films

Y. Liu, D.V. Haviland, B. Nease, and A.M. Goldman,
PRB **47**, 5931 (1993).



$$G \propto \ln T$$

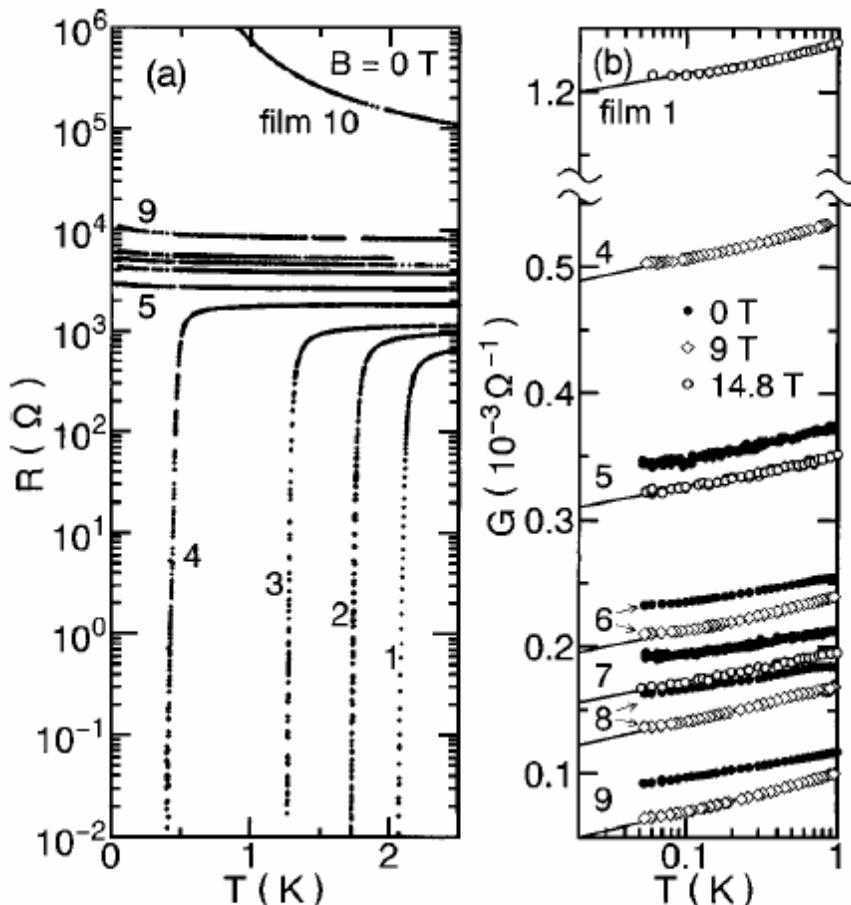
} M?

metal
Drude conductivity
+
quantum corrections

FIG. 6. Conductance G vs $\ln T$ of last ten insulating Bi films.
(The 22nd to 31st films of the Bi sequence.) The temperature dependences of the conductances are approximately logarithmic. Notice that in the low-temperature limit, the slope of the logarithm decreases as the onset of superconductivity is approached.

SMIT

Suppression of Superconductivity by Disorder



Mo_xSi_{1-x} films

S. Okuma, T. Terashima, and N. Kokubo,
PRB 58, 2816 (1998).

$$G \propto \ln T$$

metal
Drude conductivity
+
quantum corrections

Figure 1(a) illustrates the temperature dependence of the sheet resistance $R(T)$ in $B=0$ for ten selected films. Films with $R_n(10 \text{ K})$ smaller than $1.8 \text{ k}\Omega$ (films 1–4) achieve global superconductivity, while those with $R_n(10 \text{ K})$ larger than $2.5 \text{ k}\Omega$ (films 5–10) behave like an insulator, showing an increase in R at low temperatures.

SMIT

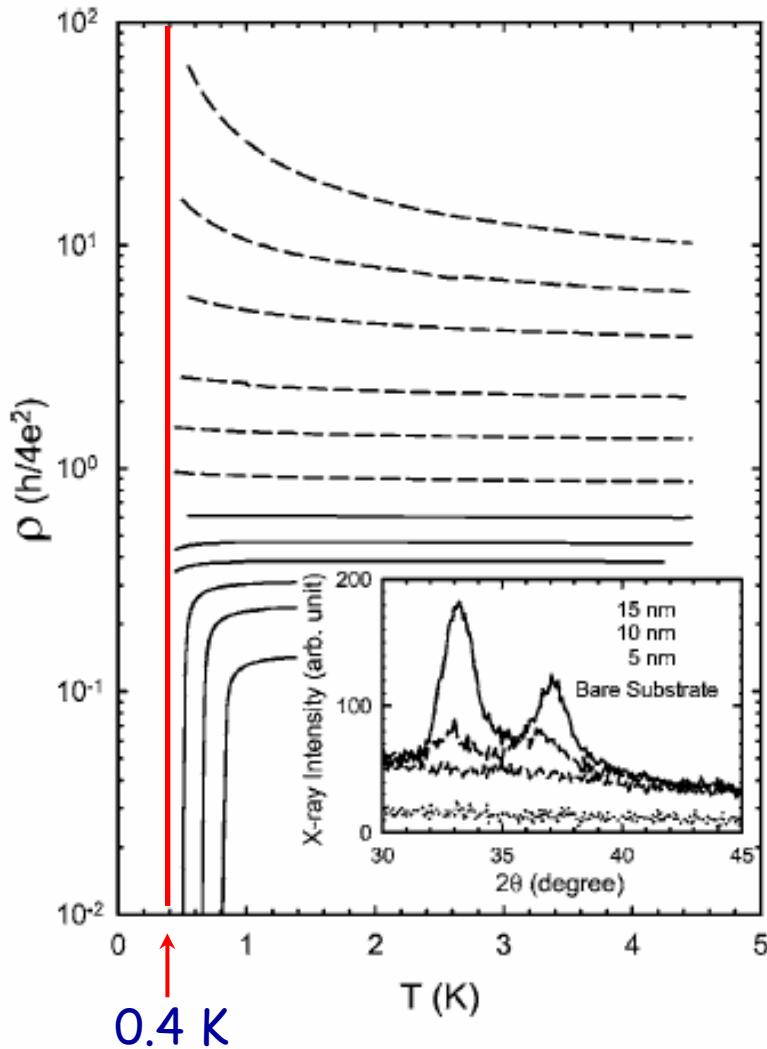


FIG. 1. The resistance is measured at $B=0$ with a dc current in the range 1–10 nA that is within the linear response regime. The thicknesses of the films are, from the top, 1.9, 2.0, 2.1, 2.3, 2.5, 2.8, 3.1, 3.4, 3.7, 4.0, 4.5, and 5.5 nm. The dashed lines are for the insulating phase and the solid lines are for the superconducting phase. Inset: x-ray diffraction patterns of 15, 10, 5 nm thick Ta films, and a bare Si substrate.

Ta films

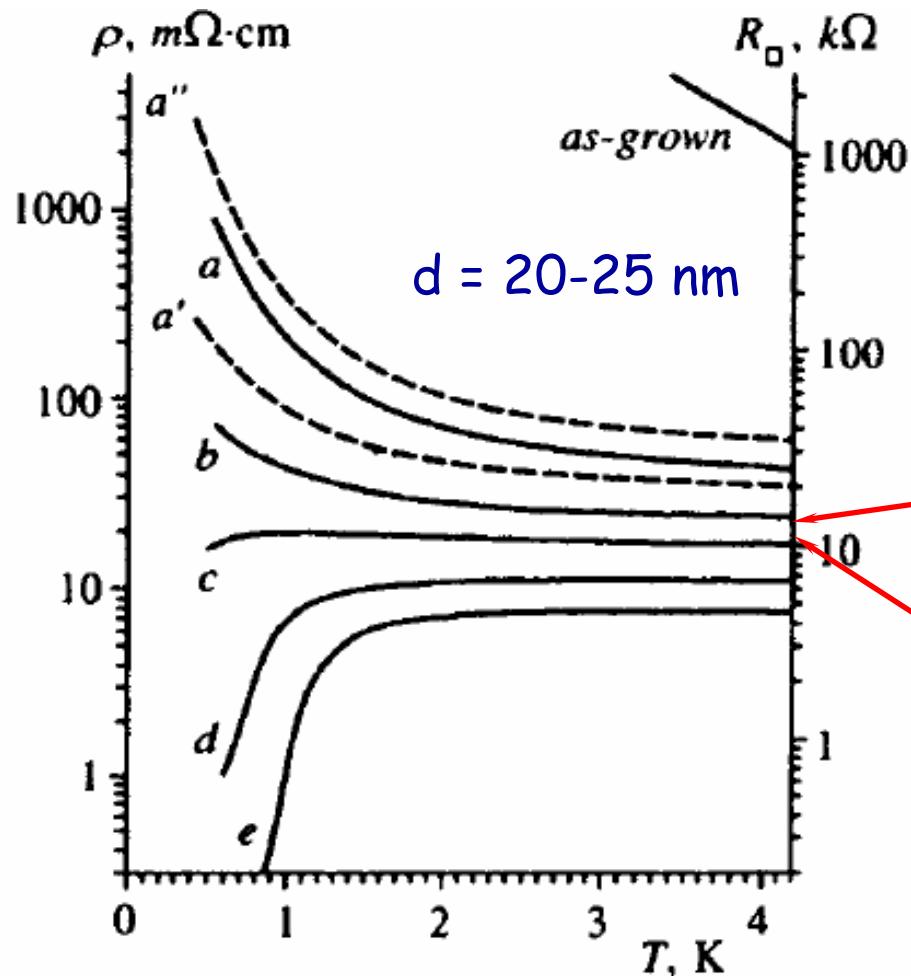
Y. Qin, C.L. Vicente, J. Yoon,
PRB 73, 100505(R) (2006).

← 6.45 kΩ

SMIT ?

or
additional study
at lower temperature
is needed

InO_x films



V.F. Gantmakher *et al.*,
JETP 82, 951 (1996).

$\sim 14 \text{ k}\Omega - \text{l}$

$\sim 10 \text{ k}\Omega - \text{s}$

FIG. 2. Evolution of the temperature dependence of the resistance of a -In₂O_x films in zero magnetic field after different treatments. Film No. 1: states a (initial)– e , film No. 2: states a' (initial) and a'' . A part of the dependence $R(T)$ for the as-grown film from the inset of Fig. 1 is also plotted.

Be films

E. Bielejec, J. Ruan, and W. Wu
PRL 87, 36801 (2001).

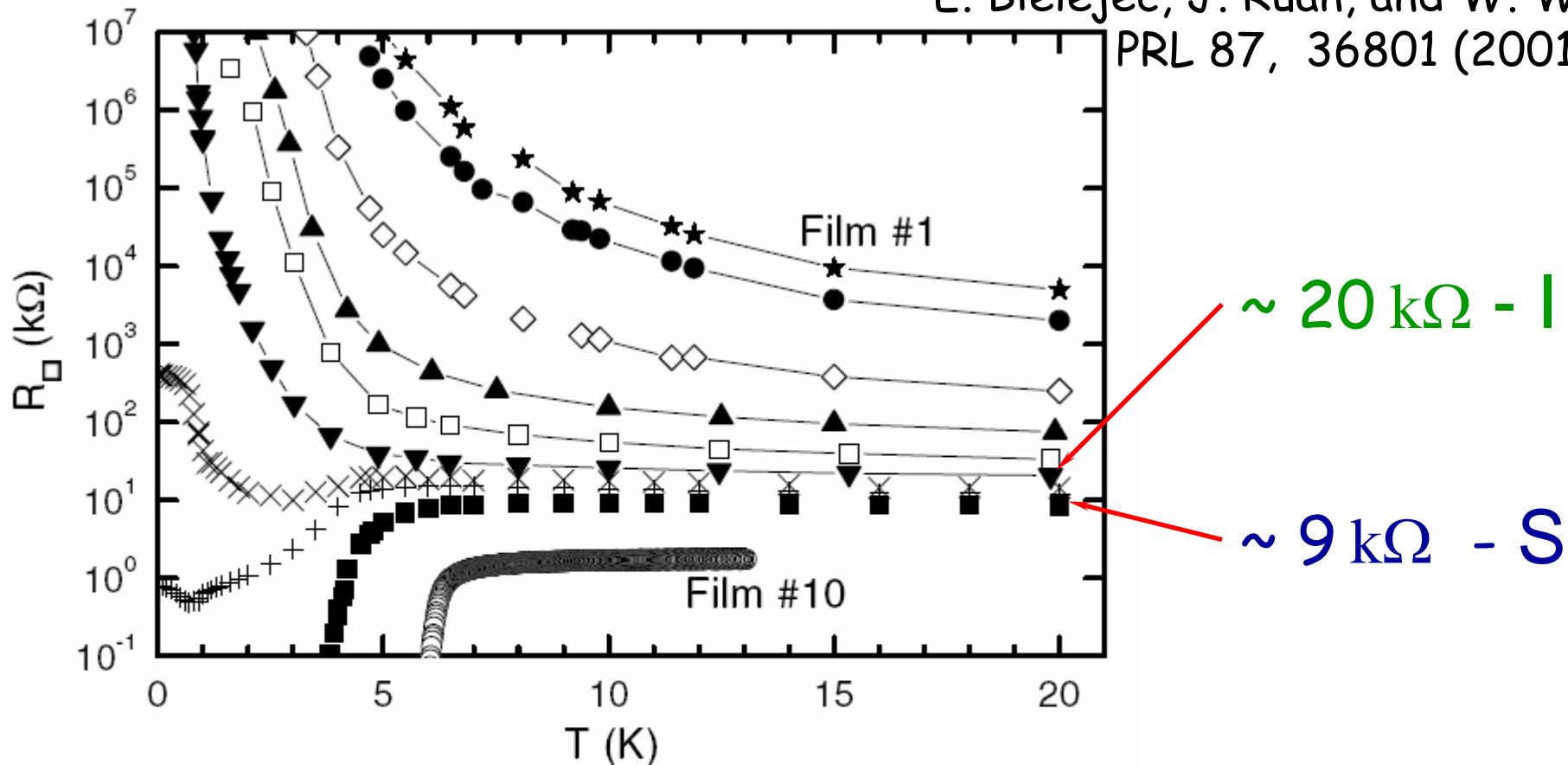
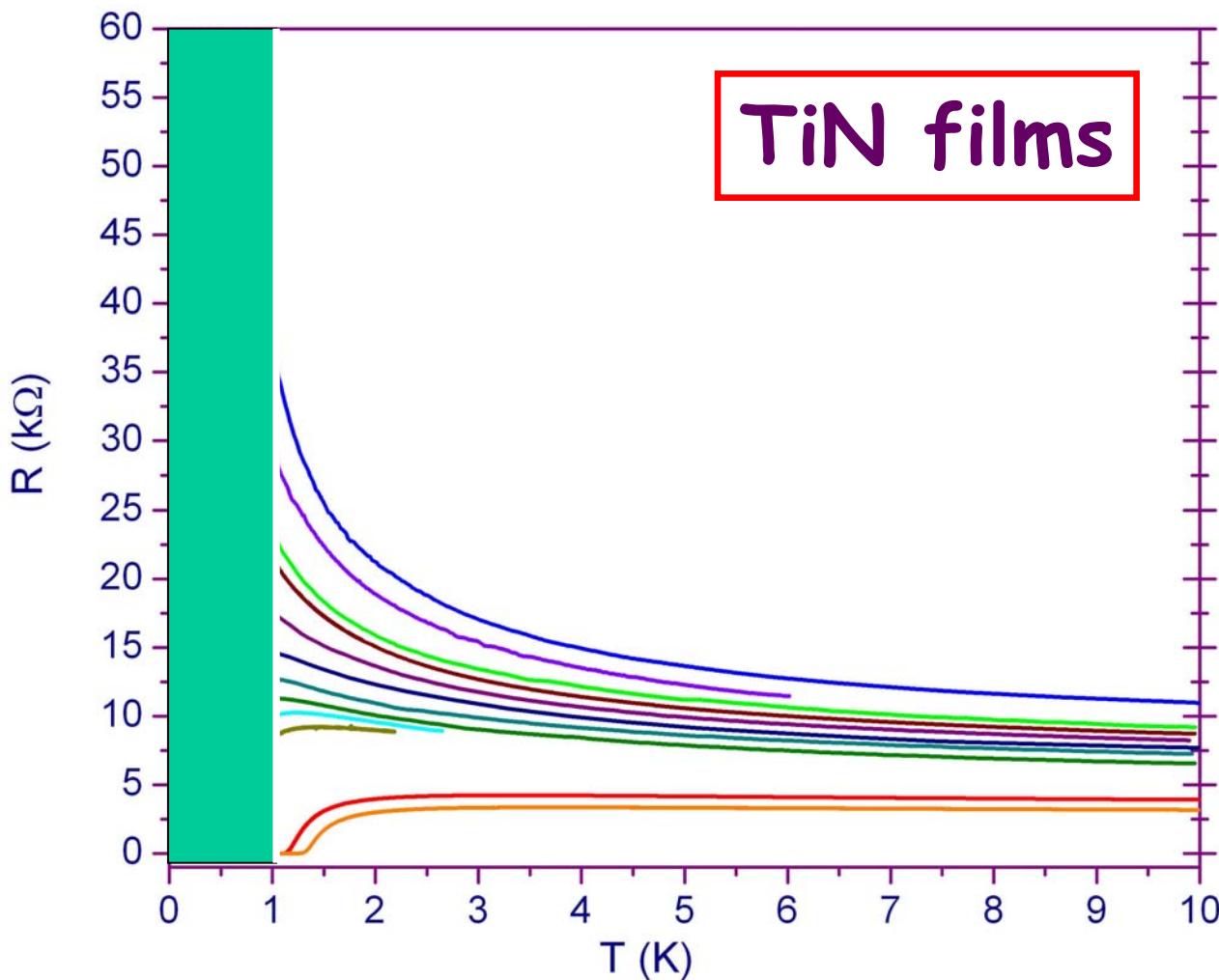


FIG. 1. Curves of film sheet resistance as a function of temperature measured on one film section following a series of deposition steps to increase film thickness. For curves from top to bottom, we label them as Film #1 to Film #10, respectively. The thickness for these films changed from 4.6 to 15.5 Å.

T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

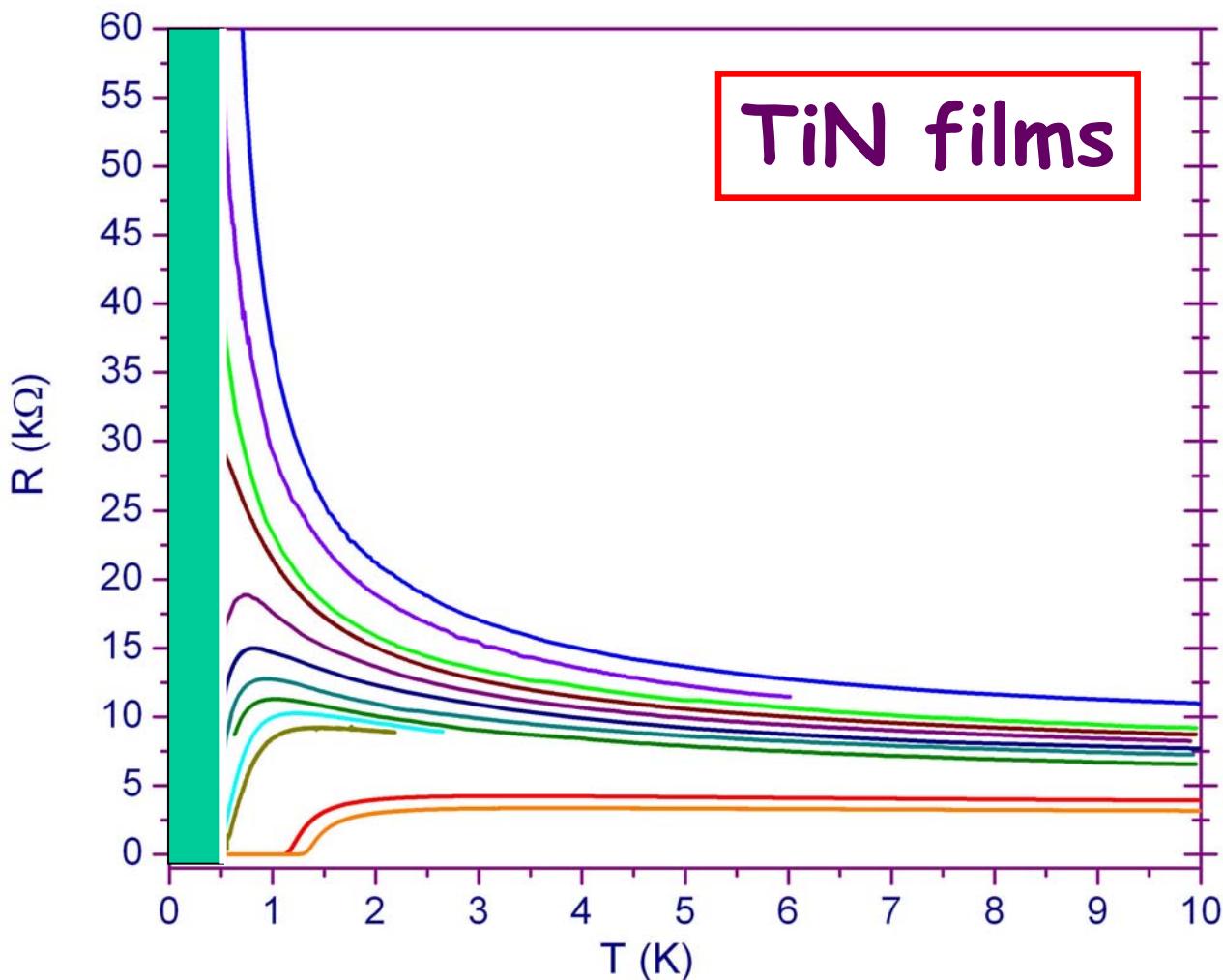
T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

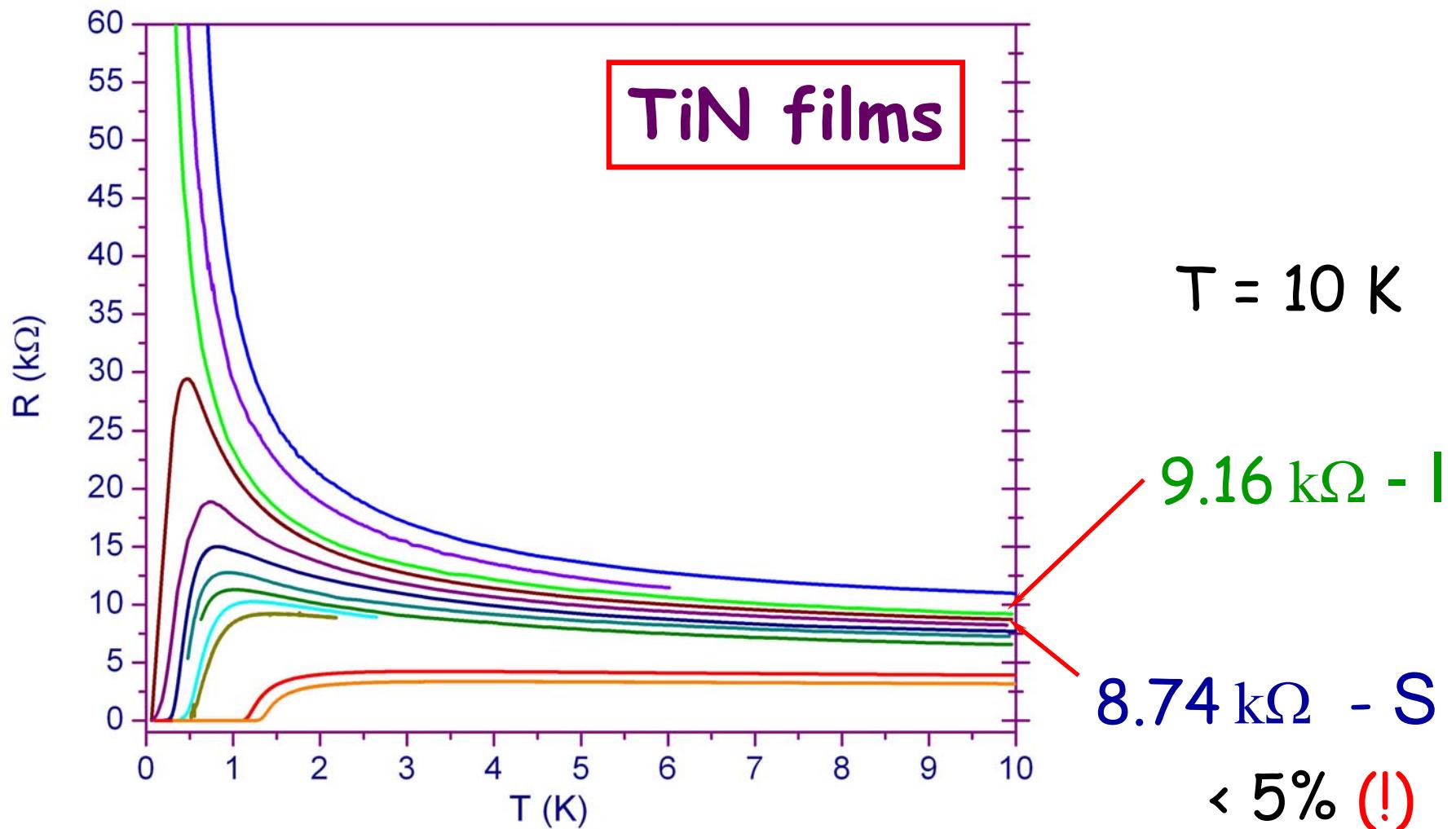
T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

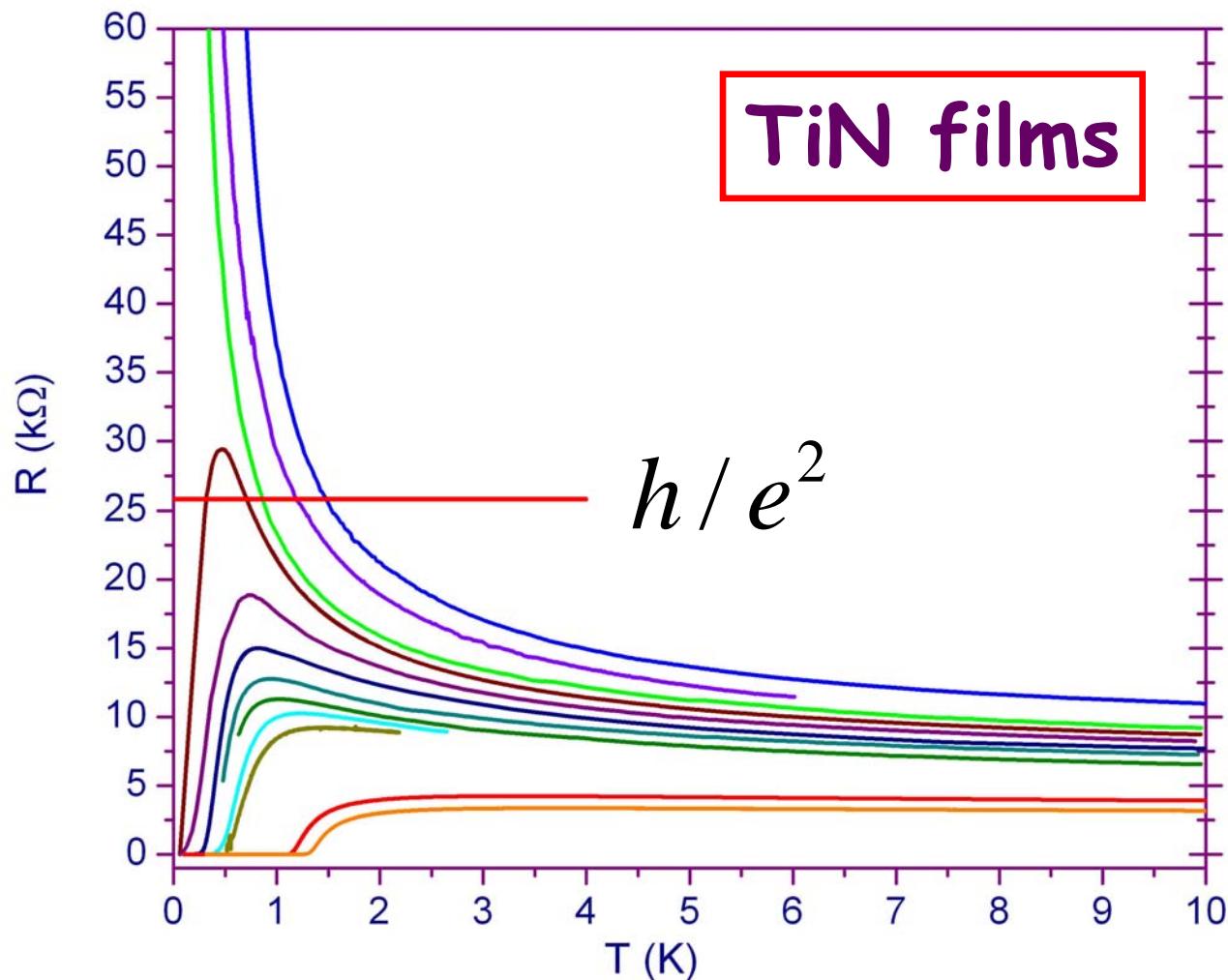
T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

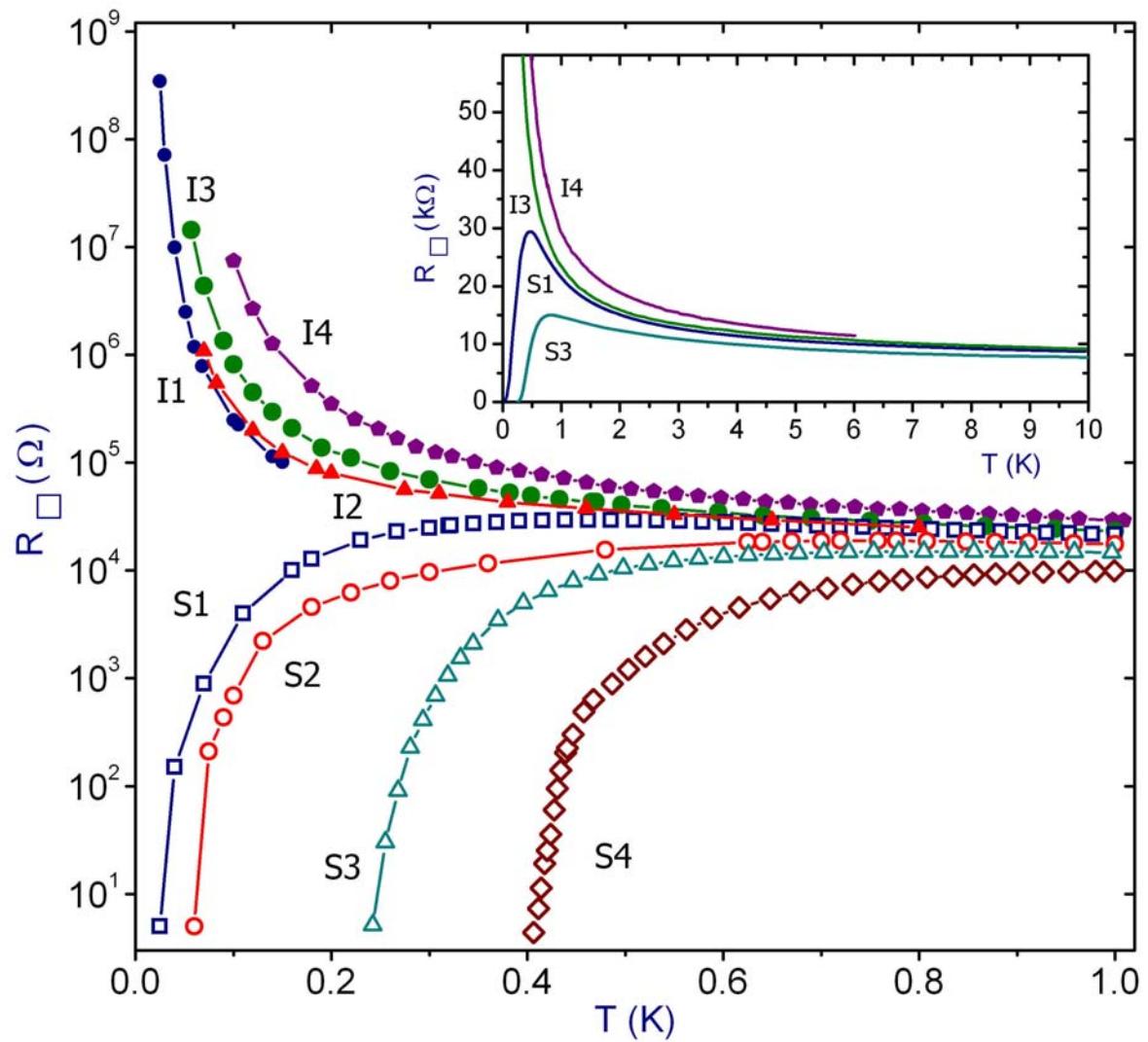
T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



TiN films

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur,
M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



SMIT or SIT

The search for a disorder-driven superconductor-insulator transition has included many materials, e.g.,

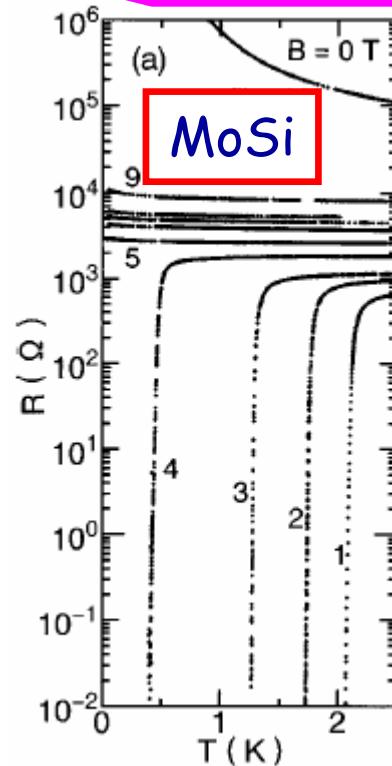
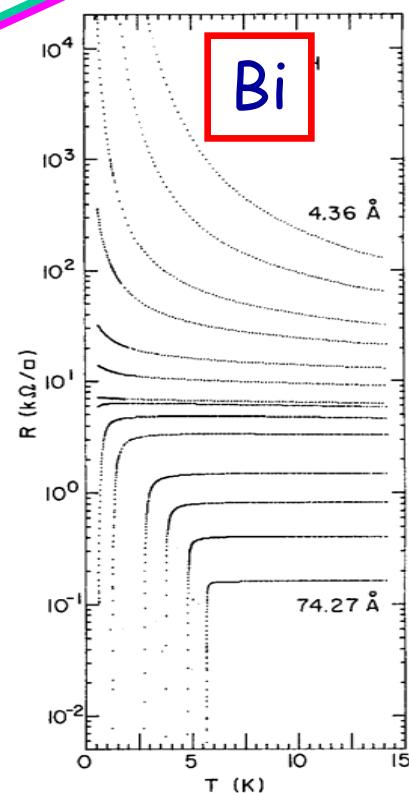
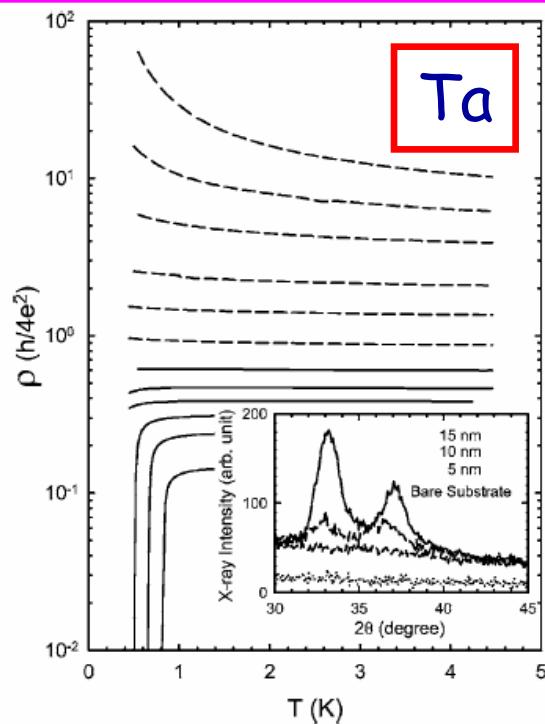
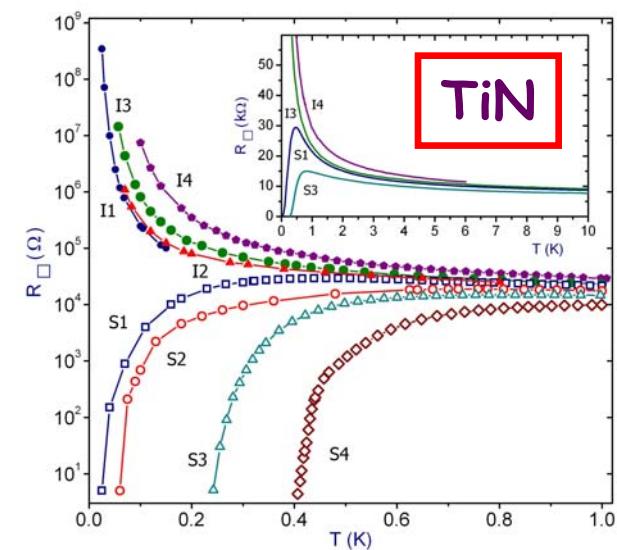
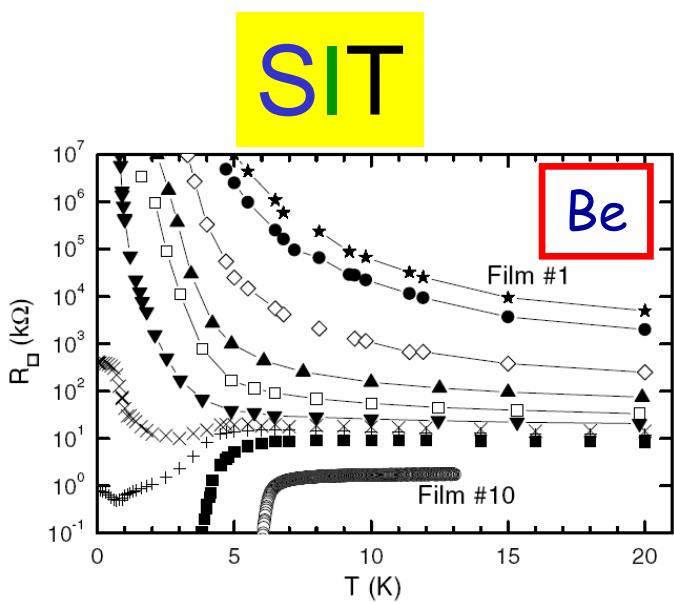
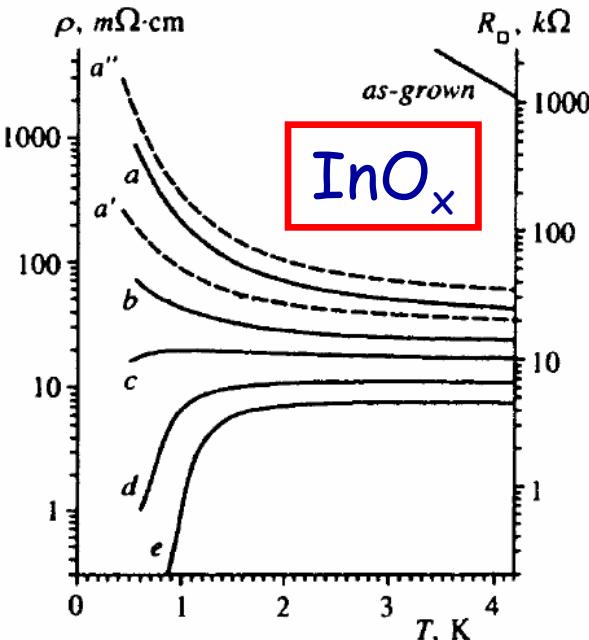
Bi, MoSi, Ta, InO_x, Be, TiN.

The immediate onset of exponential temperature dependence of the resistance, which conclusively evidences
the direct transition into an insulator,

was found so far only in **InO_x, Be, and TiN** films.

For **Bi, MoSi**, and **Ta**-compounds a weak logarithmic temperature dependence of the resistance was observed on the nonsuperconducting side in the vicinity of the transition.

- ✓ This possibly indicates an intermediate **metallic phase**
- ✓ More studies at even lower temperatures are needed to obtain conclusive evidences on which films fall into a superconducting state and which become insulating state

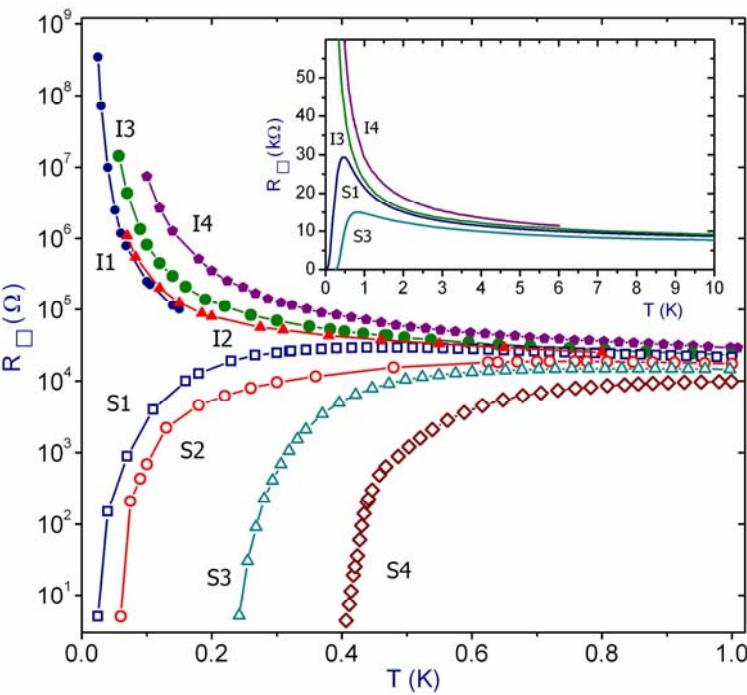
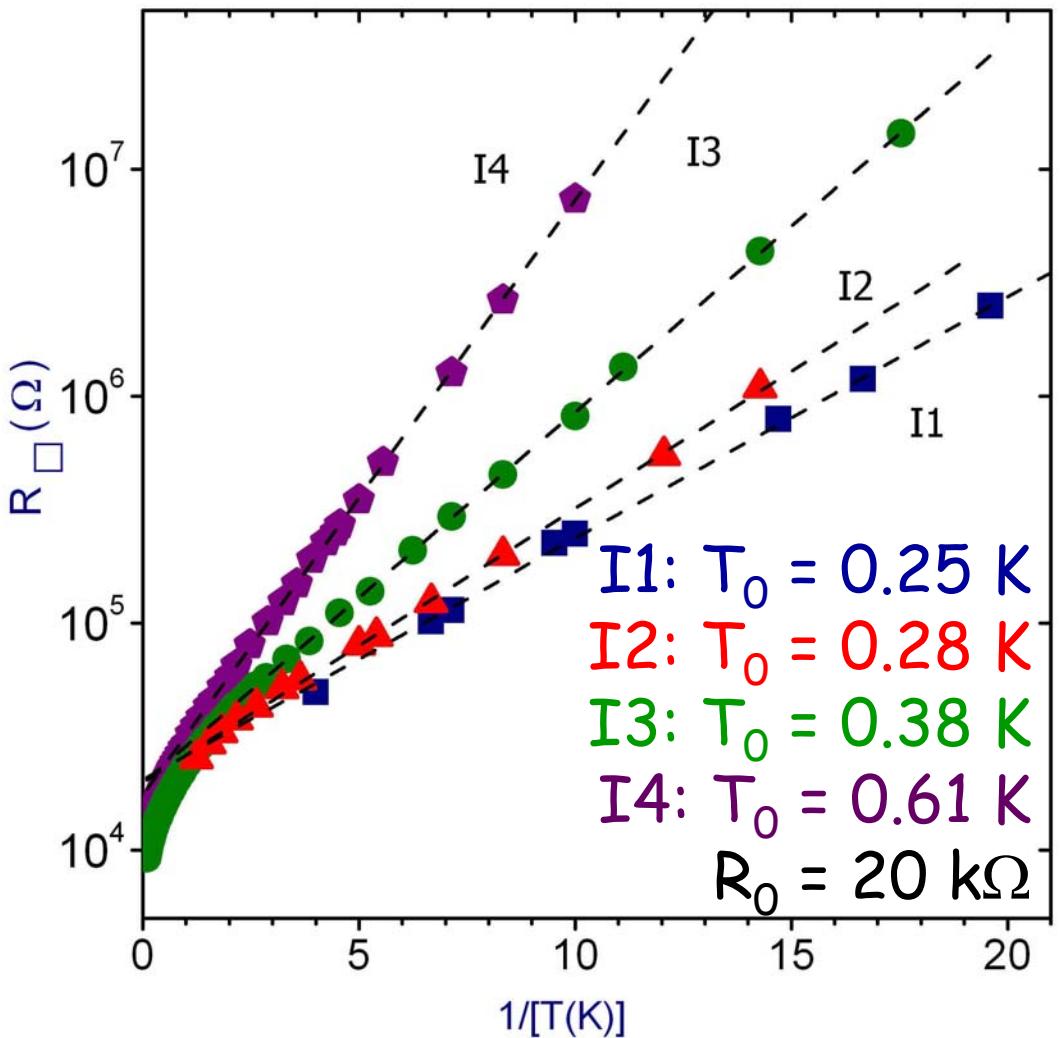


The immediate onset of exponential temperature dependence of the resistance, which conclusively evidences **the direct transition into an insulator**, was found so far only in **InO_x**, **Be**, and **TiN** films.

Insulating side of the transition
InO_x, **Be**, and **TiN** films

TiN films

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur,
M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602

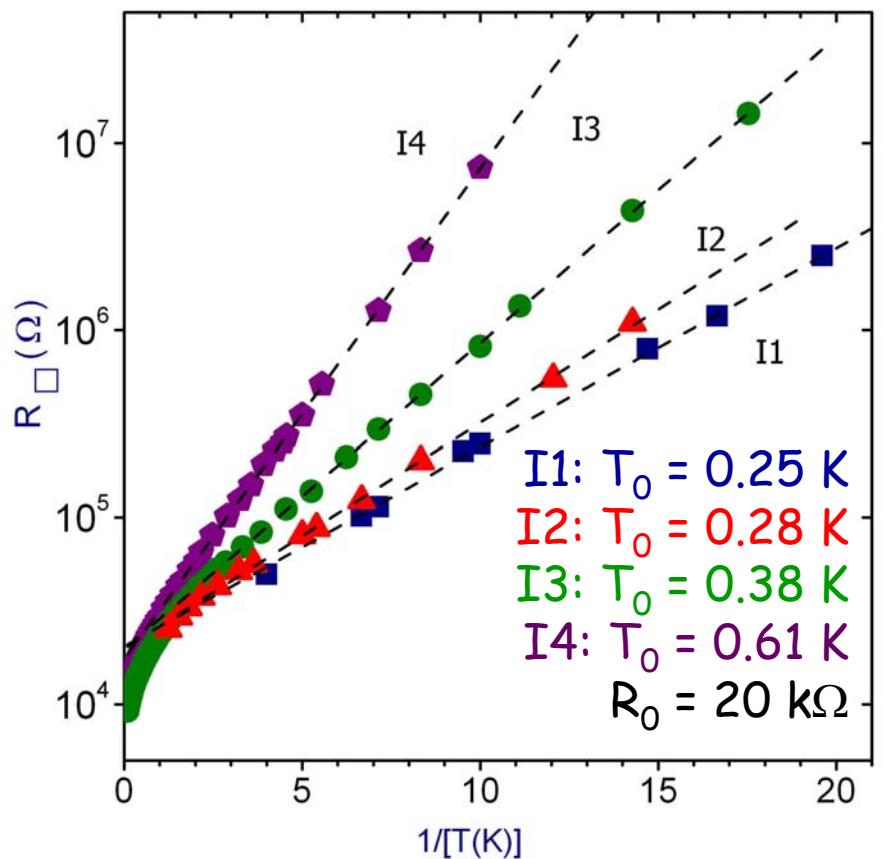


$$R = R_0 \exp(T_0/T)$$

At low temperatures we observe an Arrhenius behavior of the resistance

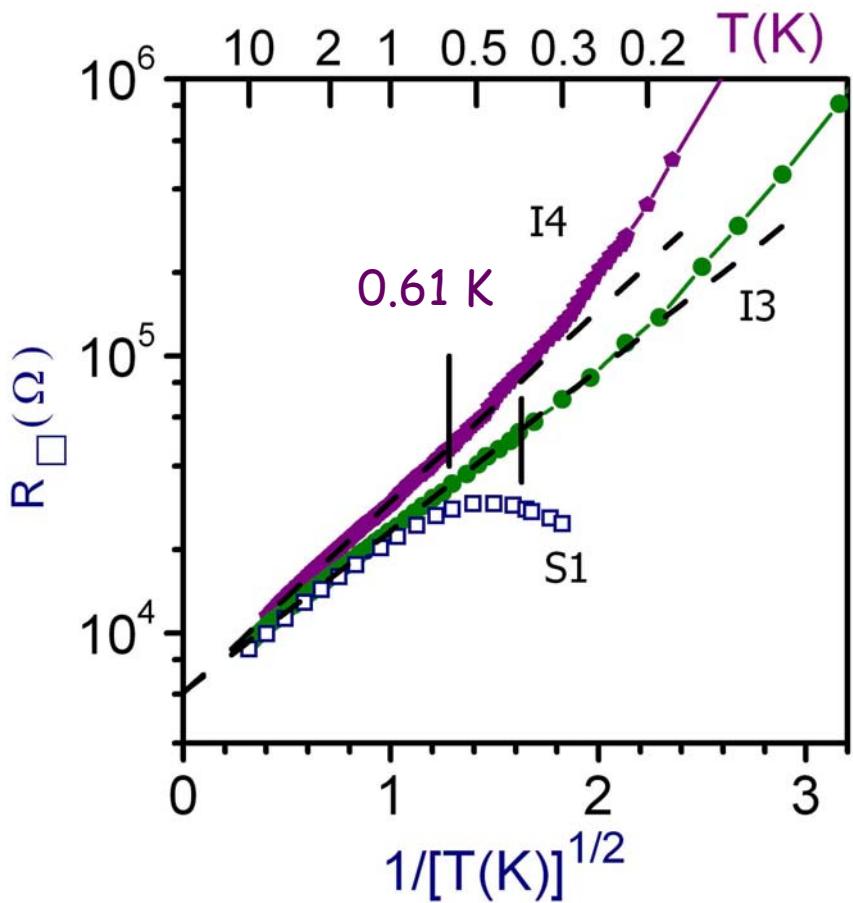
TiN films

T. B., A.Yu. Mironov, V.M. Vinokur,
M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



$$R = R_0 \exp(T_0/T)$$

At low temperatures we observe
an Arrhenius behavior
of the resistance



$$R = R_1 \exp(T_1/T)^{1/2}$$

Be films

W. Wu and E. Bielejec,
cond-mat/051121.

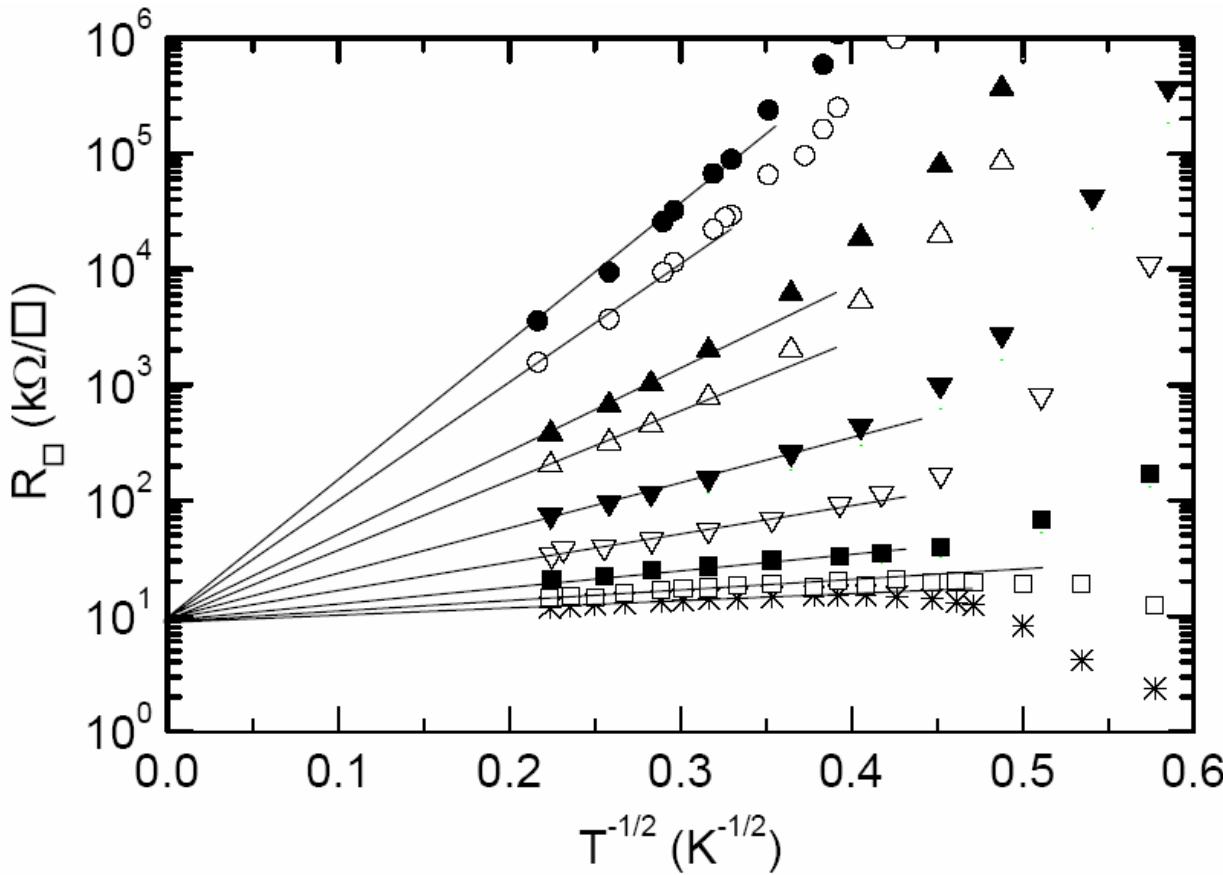
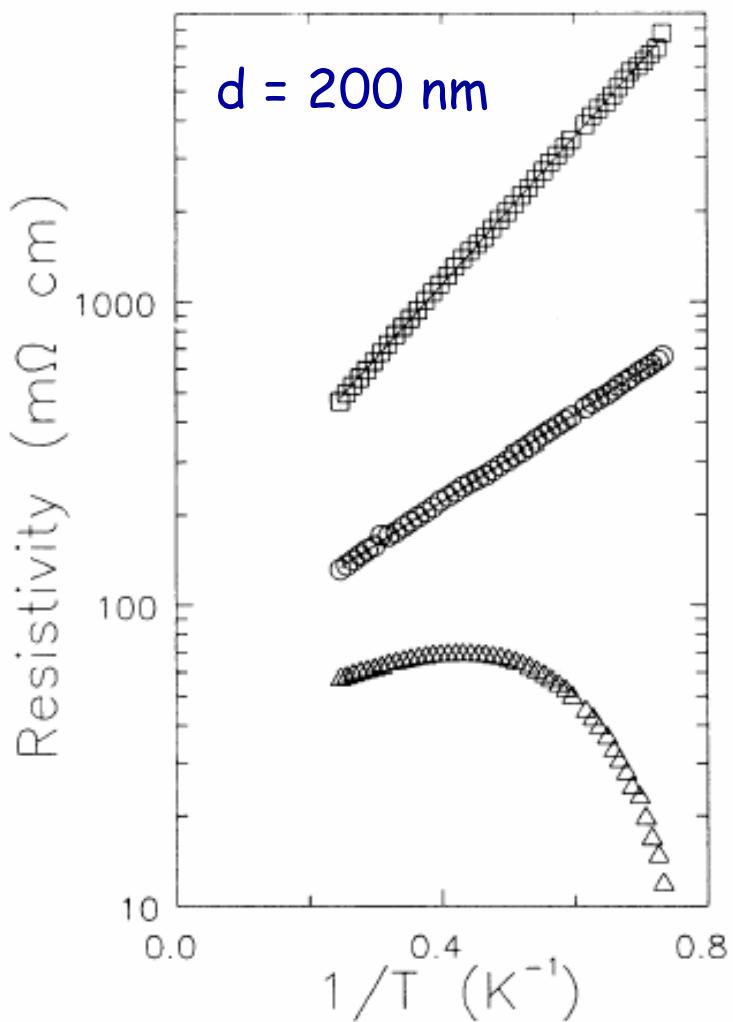


Fig. 1 Selected curves of R_{\square} versus $1/T^{1/2}$ for one Be film section following deposition steps to increase film thickness (from top to bottom). The thickness for these films changed from 4.6 \AA to about 10 \AA . The straight lines are drawn as a guide for eye, showing that in the high-T regime all the curves follow straight lines that converge to about $10 \text{ k}\Omega/\square$ in the $T \rightarrow \infty$ limit. The films for bottom curve is superconducting at low temperatures.



InO_x films

D. Shahar and Z. Ovadyahu,
PRB 46, 10917 (1992).

FIG. 2. Resistivity vs temperature of a typical batch of indium-oxide samples measured between 1.3 and 4.11 K. The upper curve is for the as-deposited film. The lower curves depict the $R(T)$ of the same sample after thermal annealing. The solid lines for the top two curves are fits to an Arrhenius behavior from which the various T_0 values were extracted. k_Fl values of these samples are 0.177 (\square), 0.21 (\circ), and 0.272 (\triangle). The sample thickness is 2000 Å and $n = 4 \times 10^{21}$.

InO_x film

D. Kowal and Z. Ovadyahu
Solid State Comm. 90,
783 (1994).

TiN film

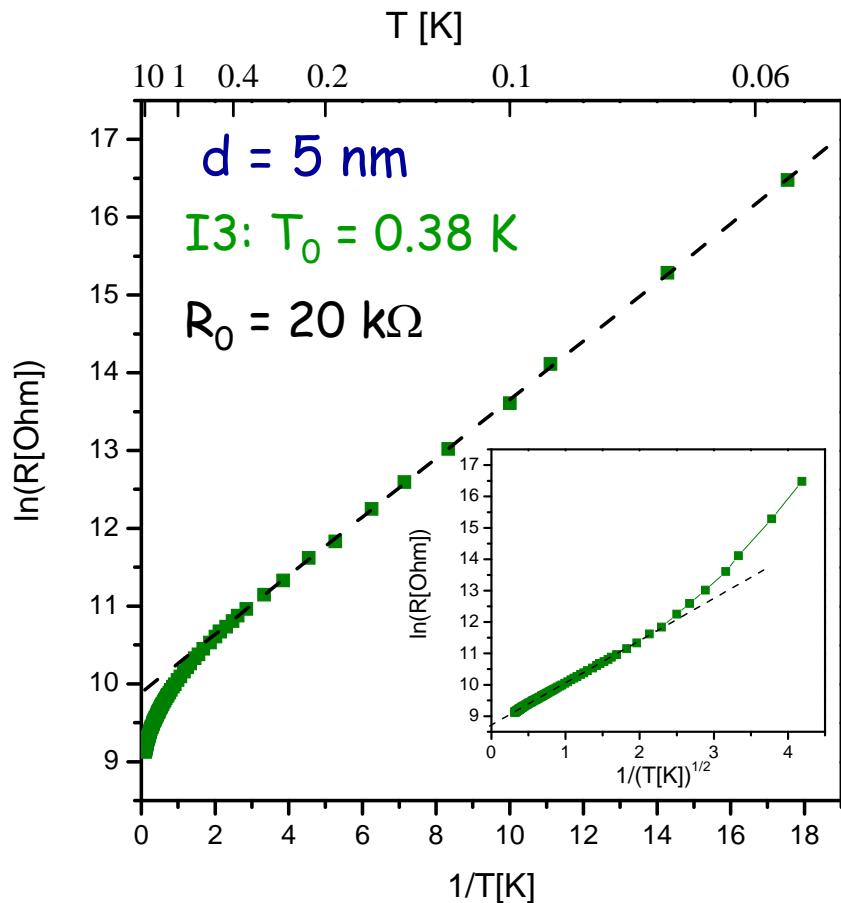
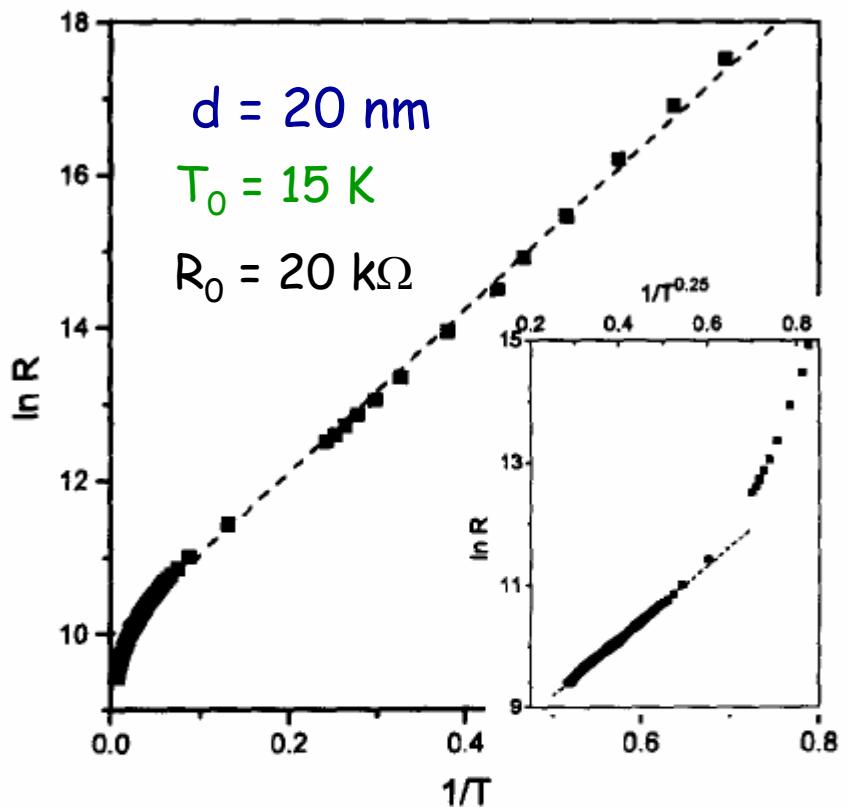


Fig. 1. The temperature dependence of the resistance for a 200\AA thick sample in the range $1.4\text{K}-200\text{K}$. Below 4.1K simple activation is observed with $T_0=15\text{K}$. Inset: The same data plotted against $T^{1/4}$ exhibits 3D VRH above 10K . The localization length determined from the slope and the known density of electrons is 12\AA .

Insulating side of the transition

InO_x, Be, and TiN films

- ❖ at low temperatures
- ❖ activation law

$$R = R_0 \exp(T_0/T)$$

- ❖ at temperatures higher than T₀

InO_x films

- ❖ 3D Mott's VRH

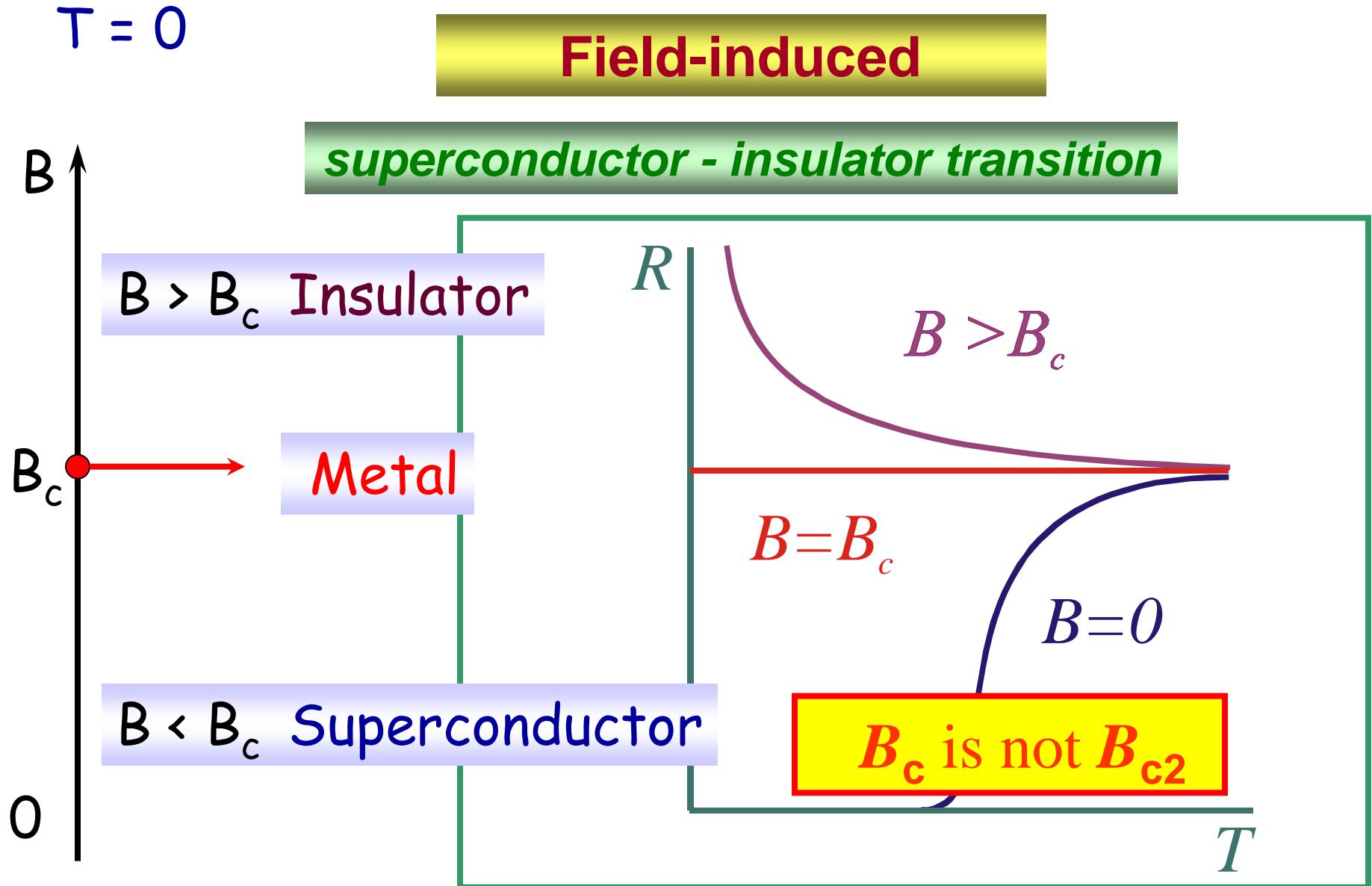
$$R = R_1 \exp(T_1/T)^{1/4}$$

Be and TiN films

- ❖ the ES hopping

$$R = R_1 \exp(T_1/T)^{1/2}$$

Suppression of Superconductivity by Magnetic field



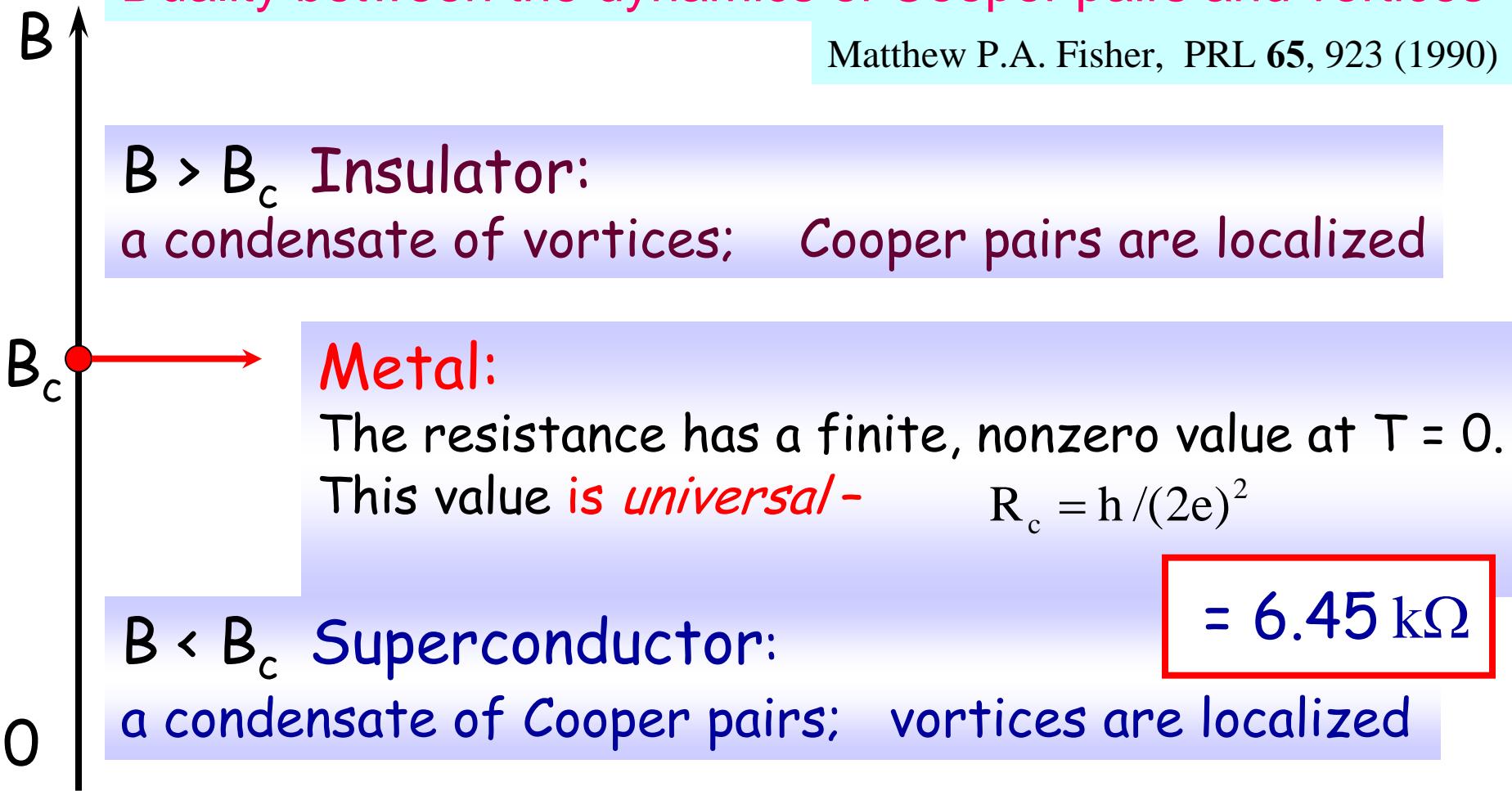
Field-induced superconductor – insulator transition

$T = 0$

*** Quantum phase transition ***

Duality between the dynamics of Cooper pairs and vortices

Matthew P.A. Fisher, PRL 65, 923 (1990)



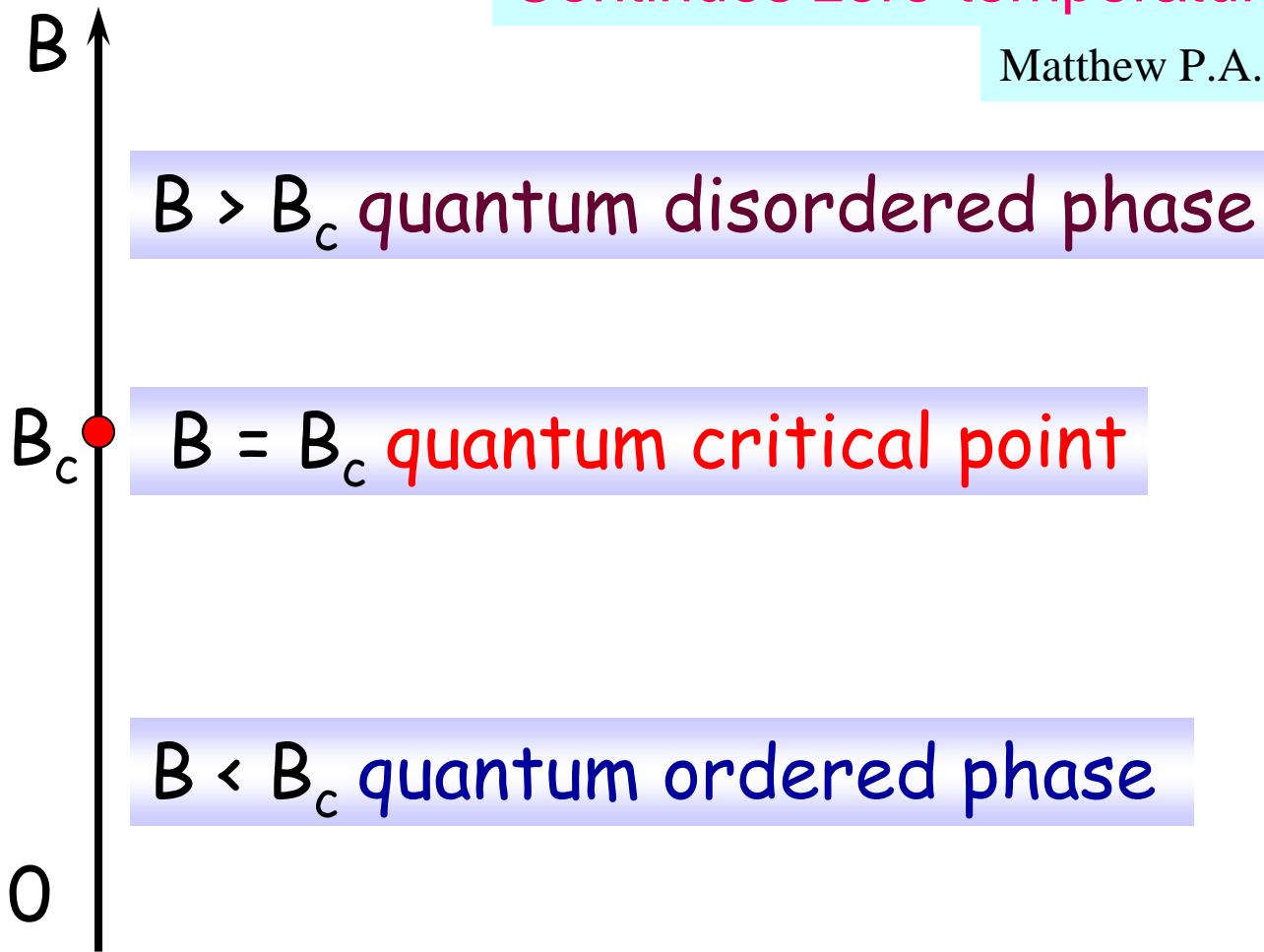
Field-induced superconductor – insulator transition

$T = 0$

*** Quantum phase transition ***

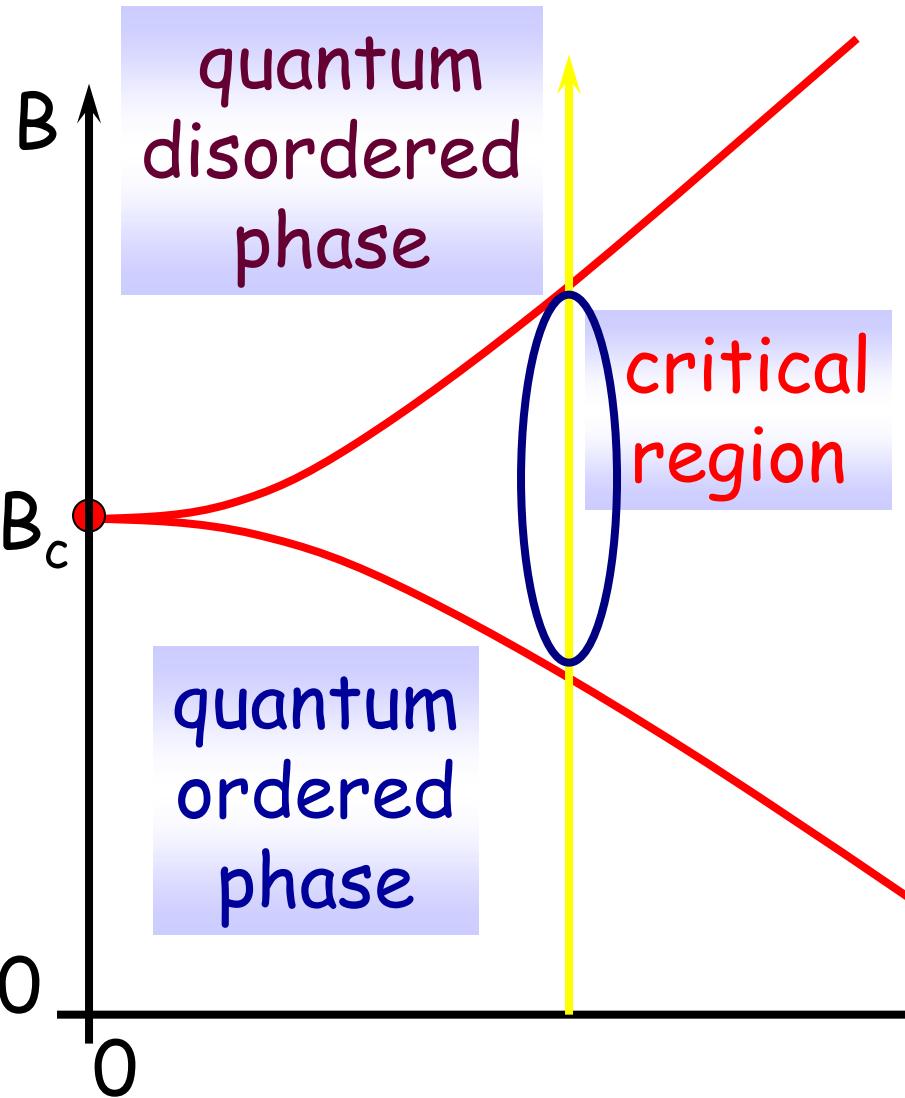
Continuous zero-temperature phase transition

Matthew P.A. Fisher, PRL **65**, 923 (1990)



Field-induced superconductor – insulator transition

$T > 0$



*** Quantum phase transition ***

Matthew P.A. Fisher, PRL **65**, 923 (1990)

$$\xi \propto \delta^{-\nu}$$

the correlation length

$$\delta = |B - B_c|$$

$$\varepsilon_{fl} \propto \xi^{-z}$$

the characteristic energy

at finite temperature

$$\frac{\varepsilon_{fl}}{T} \propto \frac{\delta^{-\nu z}}{T}$$

Scaling

$$R = R_c f\left(\frac{\delta}{T^{1/\nu z}}\right)$$

Field-induced superconductor – insulator transition

*** Quantum phase transition ***

EXPERIMENT

✓ Fan-shaped curves

$$\begin{aligned} dR/dT > 0 \text{ at } B < B_c \\ dR/dT < 0 \text{ at } B > B_c \end{aligned}$$

✓ Scaling

$$R = R_c f(|B - B_c| / T^{1/\nu z})$$

✓ Negative magnetoresistance

at high magnetic fields

(as result of the break up of the localized Cooper pairs)

V.F. Gantmakher, et. al. JETP Lett. 68, 363 (1998)

picture-gallery

“In search of
Magnetic-field-driven
superconductor-insulator
transition”

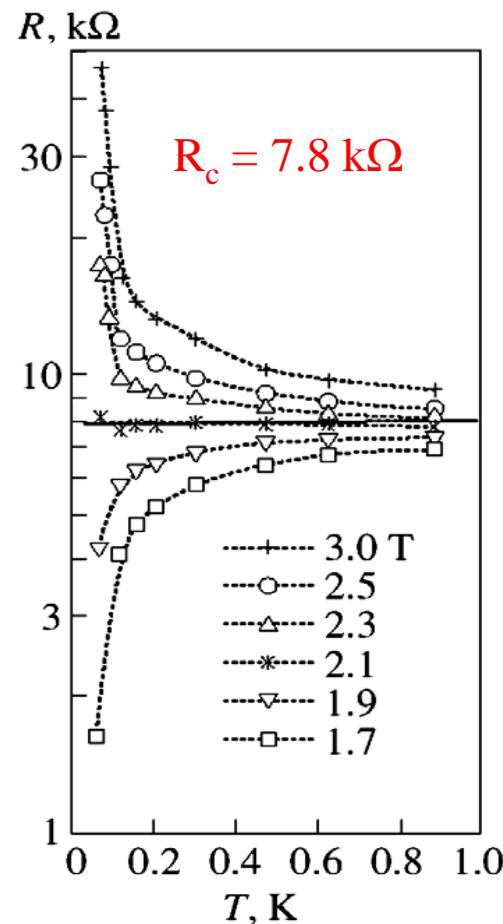
*** collection ***

Bi, MoSi, MoGe, Ta, InO_x, Be, TiN

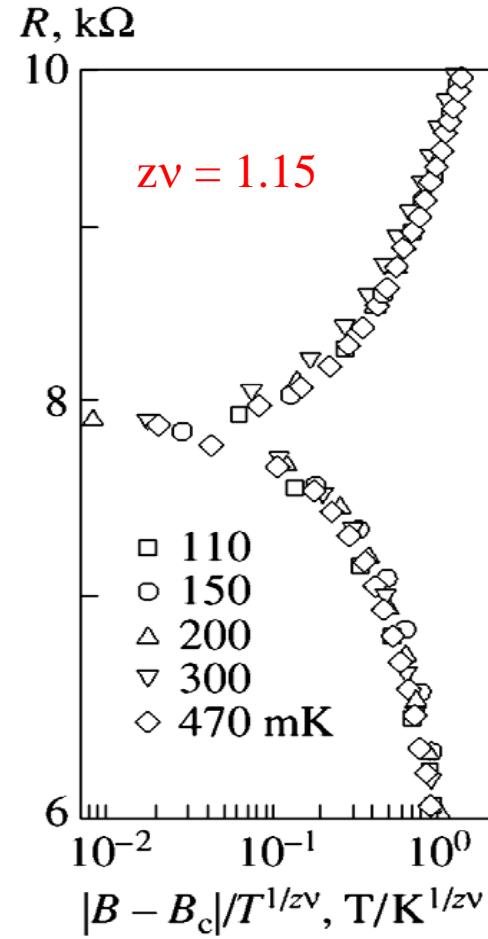
Field-induced superconductor – insulator transition

V. F. Gantmakher, M. V. Golubkov, V. T. Dolgopolov,
A. A. Shashkin, G. E. Tsydynzhapov, JETP Lett. 71,
160 (2000); 71, 473 (2000)

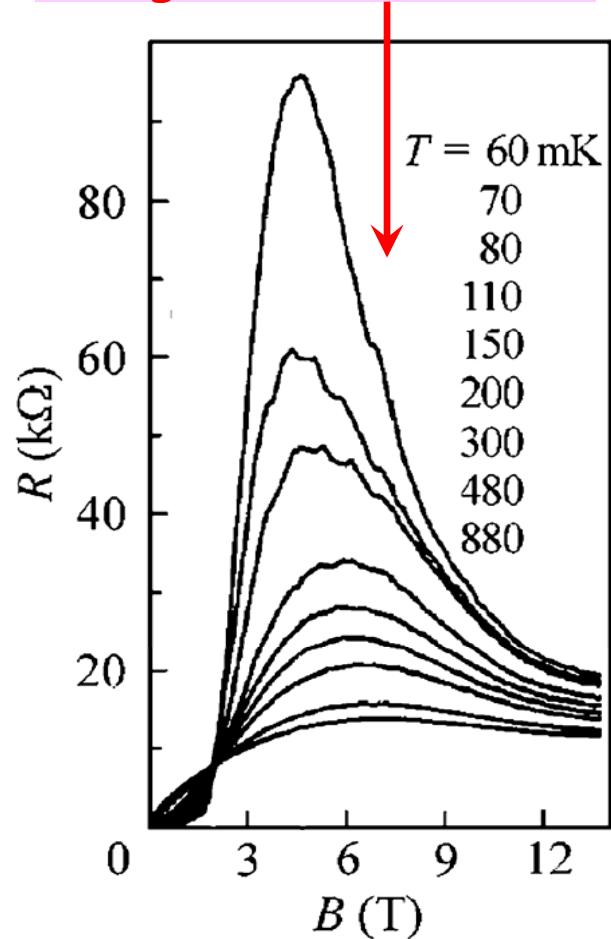
Fan-shaped curves



Scaling



InO_x films
Negative magnetoresistance

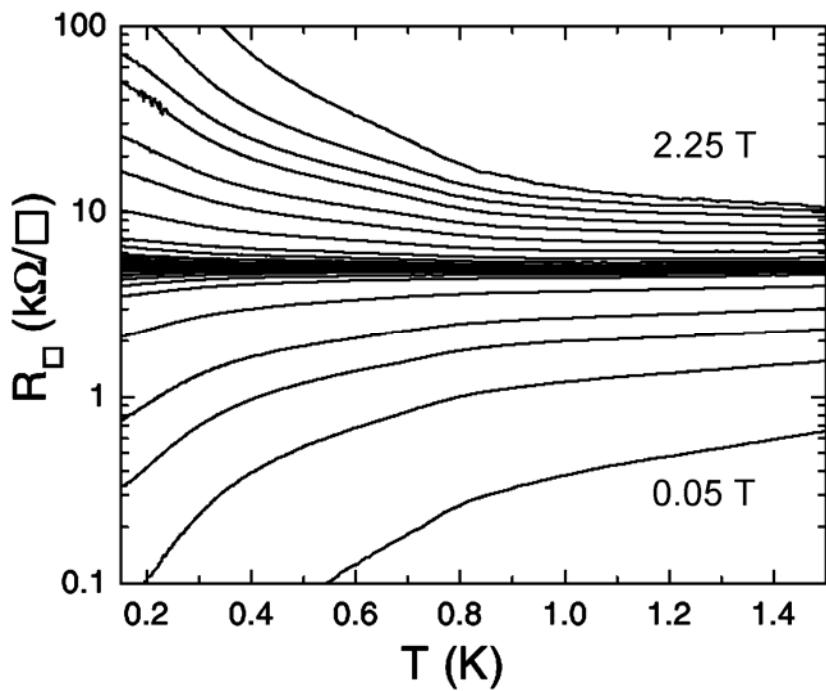


Field-induced superconductor – insulator transition

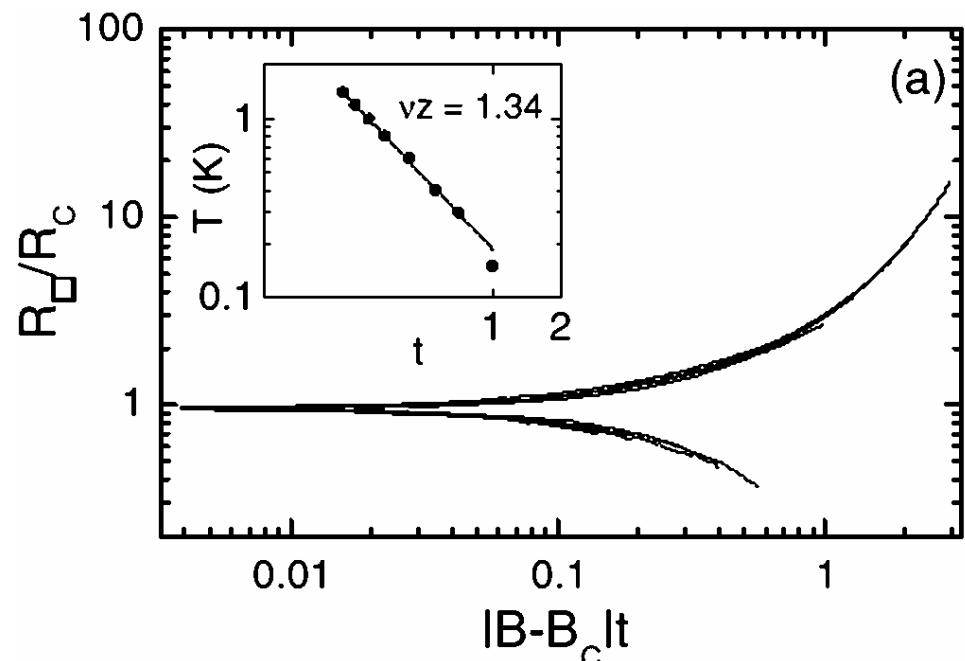
E. Bielejec and Wenhao Wu, PRL **88**, 206802 (2002).

Be films

Fan-shaped curves



Scaling



Field-induced superconductor – insulator transition



VOLUME 74, NUMBER 15

PHYSICAL REVIEW LETTERS

10 APRIL 1995

Superconducting-Insulating Transition in Two-Dimensional α -MoGe Thin Films

Ali Yazdani* and Aharon Kapitulnik

Department of Applied Physics, Stanford University, Stanford, California 94305

MoGe

$d = 8 \text{ nm}$, $R_c = 1750 \Omega$

Fan-shaped curves

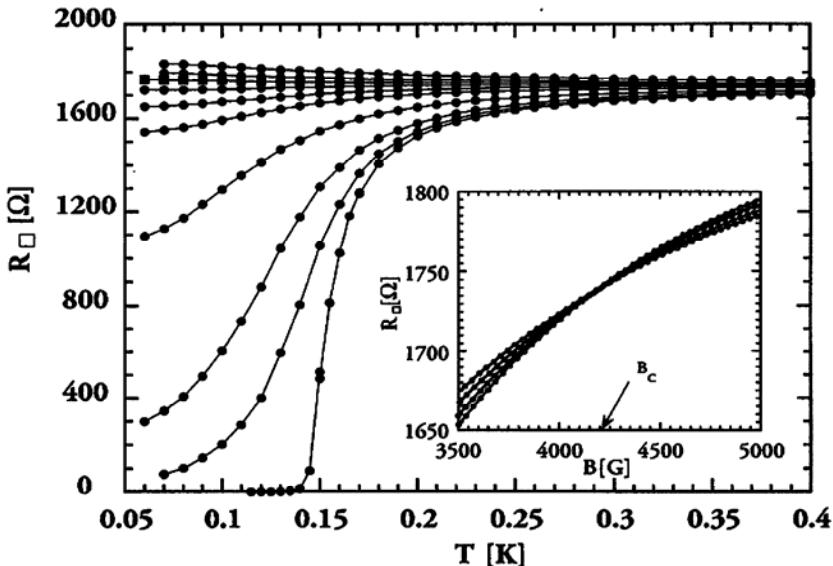


FIG. 1. Zero bias resistance of sample 2 plotted versus temperature at $B = 0, 0.5, 1.0, 2.0, 3.0, 4.0, 4.4, 4.5, 5.5, 6 \text{ kG}$. In the inset, $R_\square(B, T, E = 0)$ for the same sample measured versus field, at $T = 80, 90, 100, 110 \text{ mK}$.

Scaling

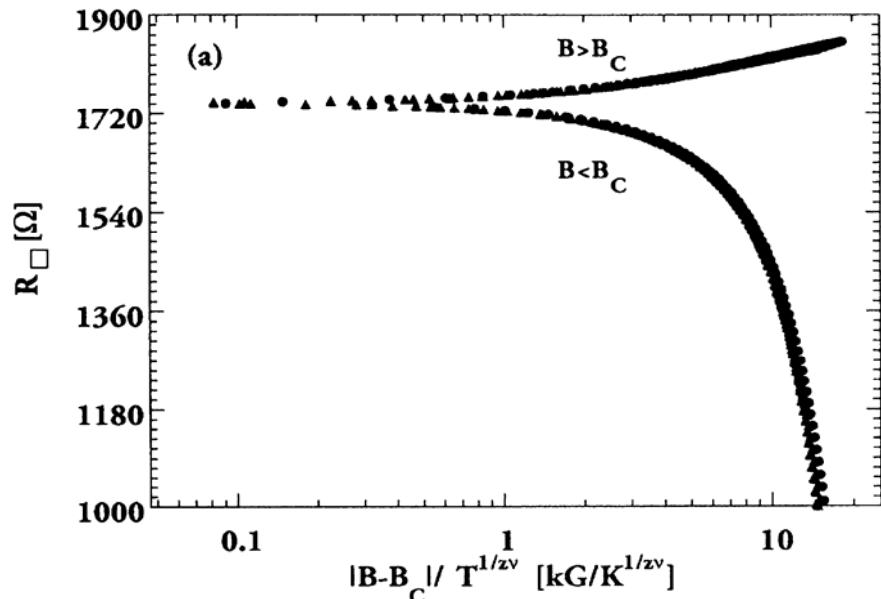


FIG. 3. Top: Scaling of $R_\square(B, T, E = 0)$ for sample 2 measured at $T = 80, 90, 100, 110 \text{ mK}$ ($B_c = 4.19 \text{ kG}$, $\nu z = 1.36$).

Field-induced superconductor – insulator transition



PHYSICAL REVIEW B

VOLUME 58, NUMBER 5

1 AUGUST 1998-I

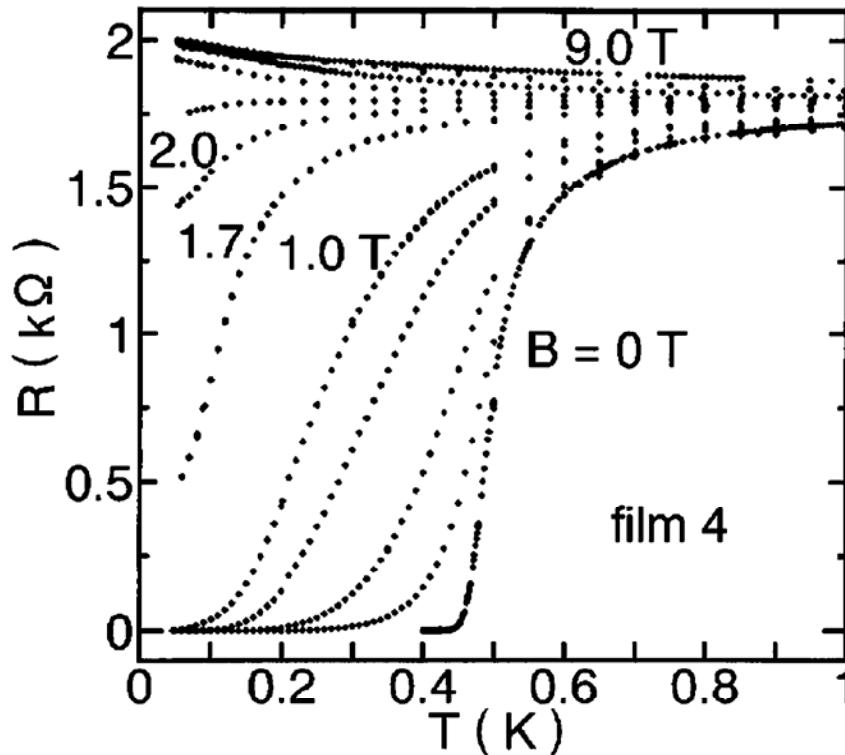
Anomalous magnetoresistance near the superconductor-insulator transition in ultrathin films of $\alpha\text{-Mo}_x\text{Si}_{1-x}$

MoSi

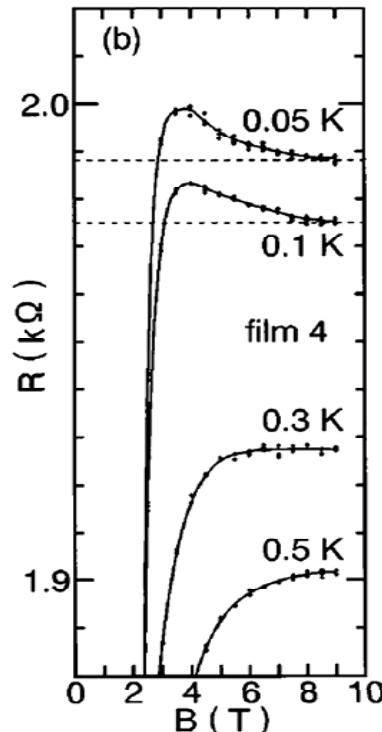
S. Okuma, T. Terashima, and N. Kokubo

Research Center for Very Low Temperature System, Tokyo Institute of Technology, 2-12-1, Ohokayama, Meguro-ku,
Tokyo 152-8551, Japan

Fan-shaped curves



Negative magnetoresistance



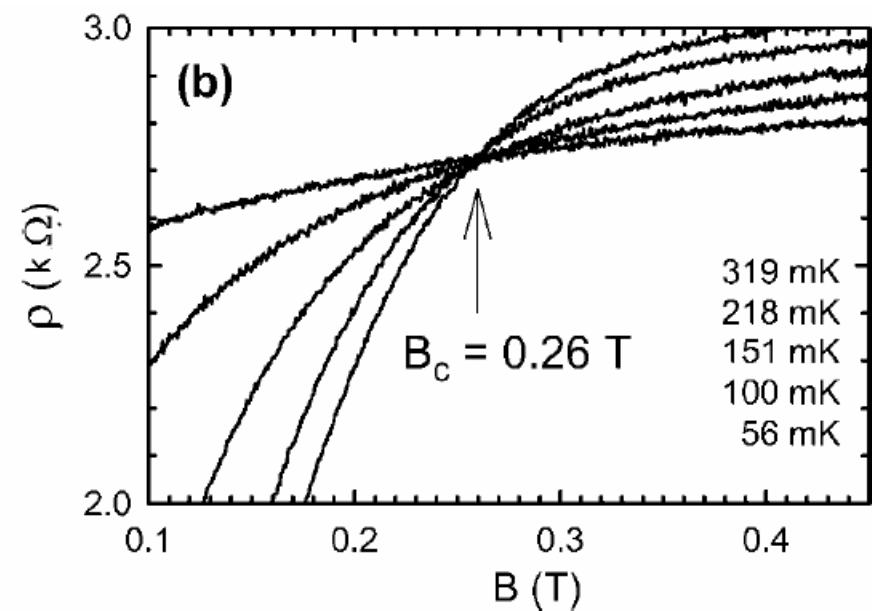
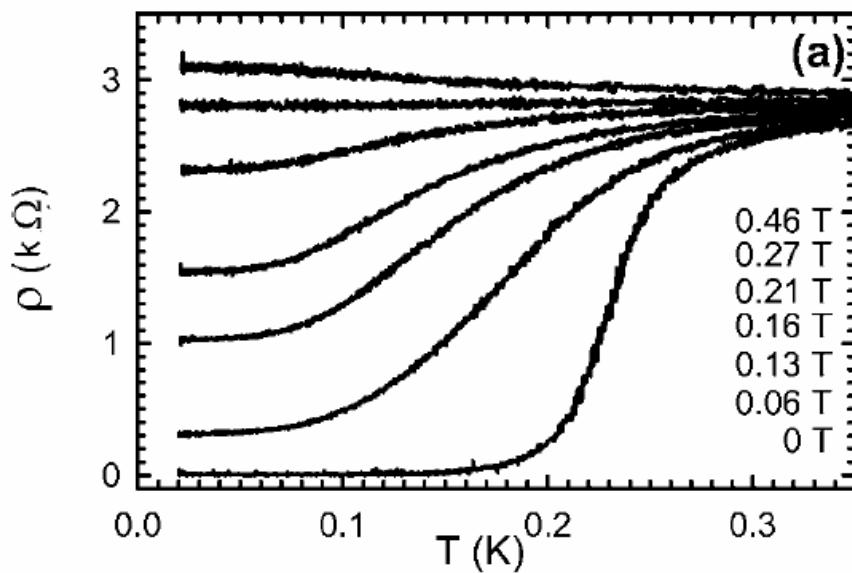
Field-induced superconductor – insulator transition



Y. Qin, C.L. Vicente, J. Yoon,
PRB 73, 100505(R) (2006).

The resistance in the low T limit increases toward ρ_n with increasing B , and at $B=0.27$ T it becomes almost T independent over the entire T range. At higher fields [the top trace in Fig. 2(a)] $d\rho/dT$ becomes negative, which we take as an indication for an insulator.

Ta films



Field-induced superconductor – insulator transition



PHYSICAL REVIEW B

VOLUME 60, NUMBER 6

1 AUGUST 1999-II

Superconductor-insulator transition in two dimensions

Bi films

N. Marković,* C. Christiansen, A. M. Mack, W. H. Huber, and A. M. Goldman

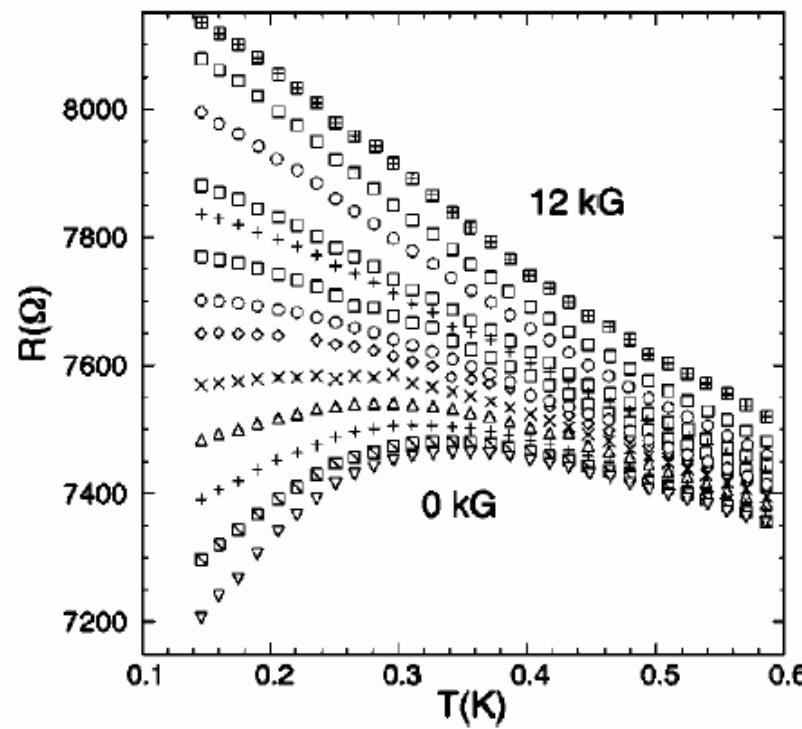
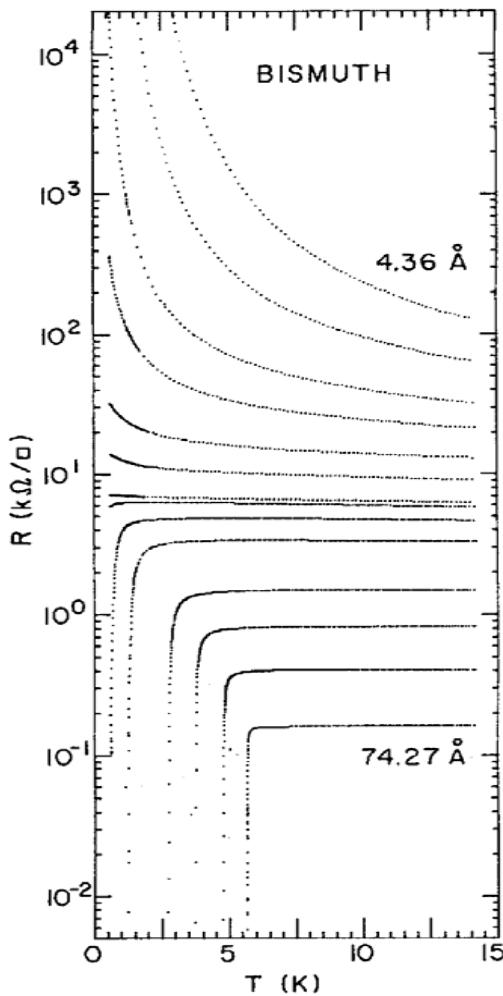


FIG. 1. Resistance per square as a function of temperature in different magnetic fields, ranging from 0 kG (bottom) to 12 kG (top), in 1 kG increments.

Field-induced superconductor – insulator transition



PHYSICAL REVIEW B

VOLUME 60, NUMBER 6

1 AUGUST 1999-II

Superconductor-insulator transition in two dimensions

Bi films

N. Marković,* C. Christiansen, A. M. Mack, W. H. Huber, and A. M. Goldman

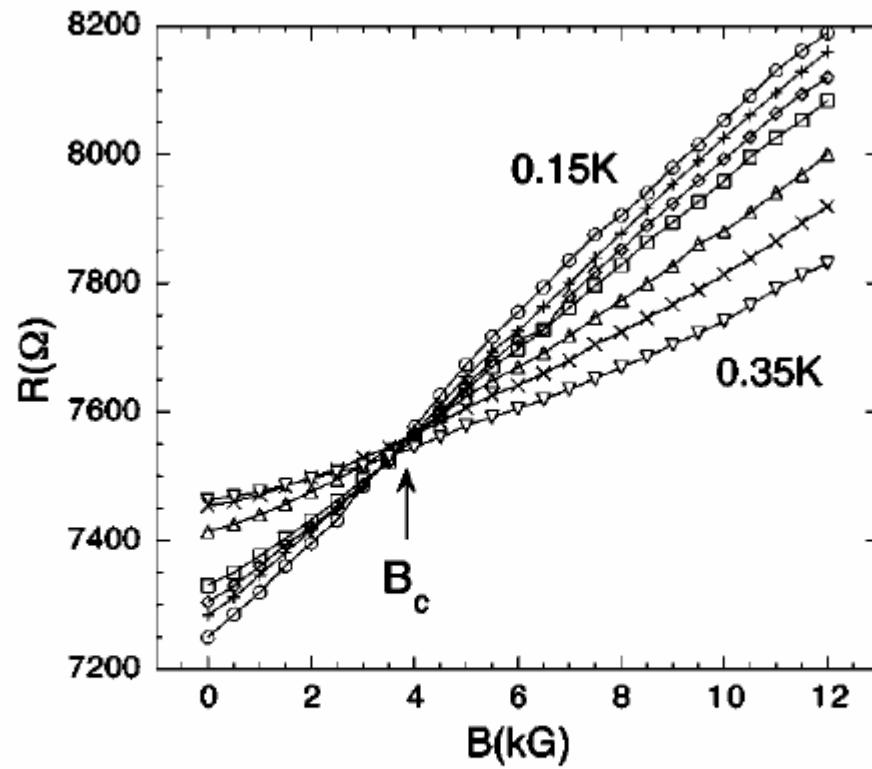
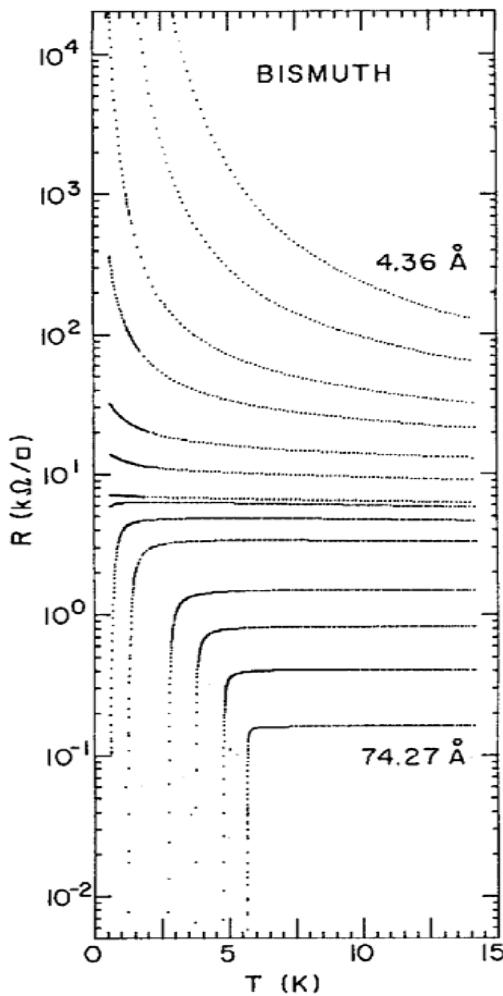


FIG. 2. Resistance per square as a function of magnetic field for a bismuth film close to the transition. Different curves represent different temperatures: 0.15, 0.17, 0.19, 0.2, 0.25, 0.3, and 0.35 K.

Field-induced superconductor – insulator transition



PHYSICAL REVIEW B

VOLUME 60, NUMBER 6

1 AUGUST 1999-II

Superconductor-insulator transition in two dimensions

Bi films

N. Marković,* C. Christiansen, A. M. Mack, W. H. Huber, and A. M. Goldman

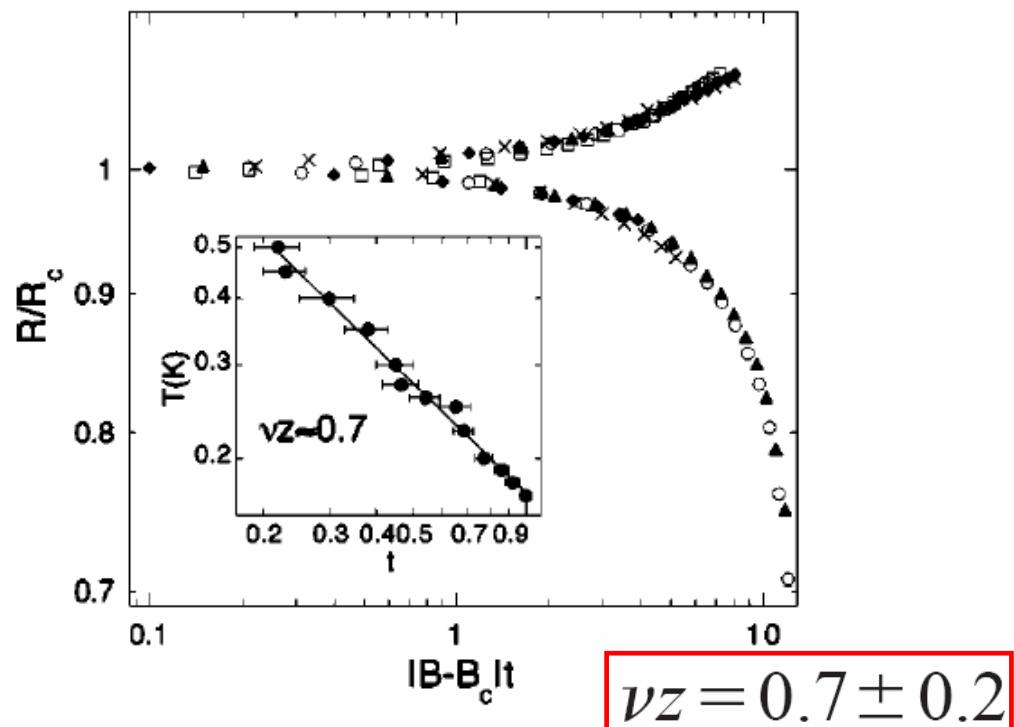
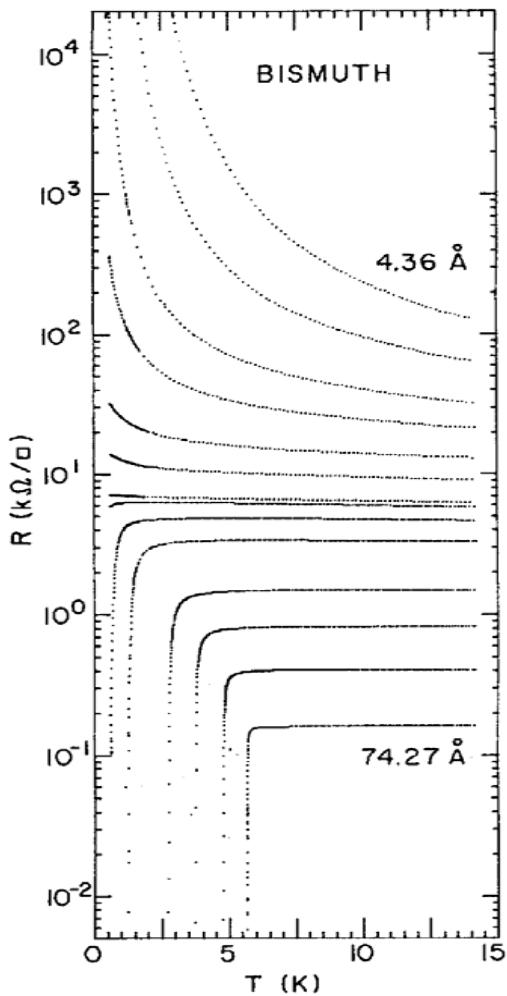


FIG. 3. Normalized resistance per square as a function of the scaling variable $T^{-1/\nu z} |B - B_c| l t$. Each symbol represents one film at different temperatures (only a small portion of the data is shown for clarity). Inset: The fitting a power law to the temperature dependence of the parameter t determines the value of νz .

$$\nu z = 0.7 \pm 0.2$$

Field-induced superconductor – insulator transition

InO_x films

M. Steiner and A. Kapitulnik,
Physica C **422**, 16 (2005)

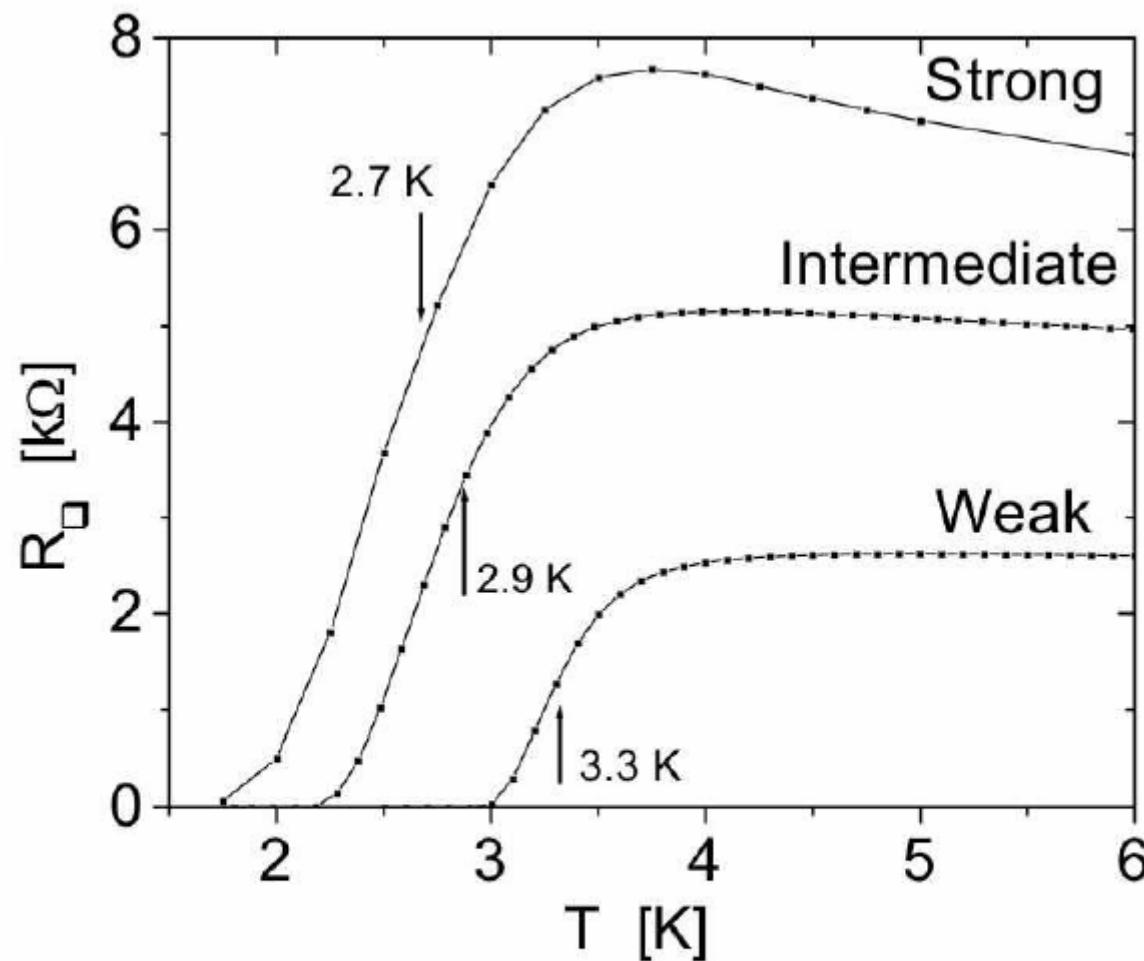
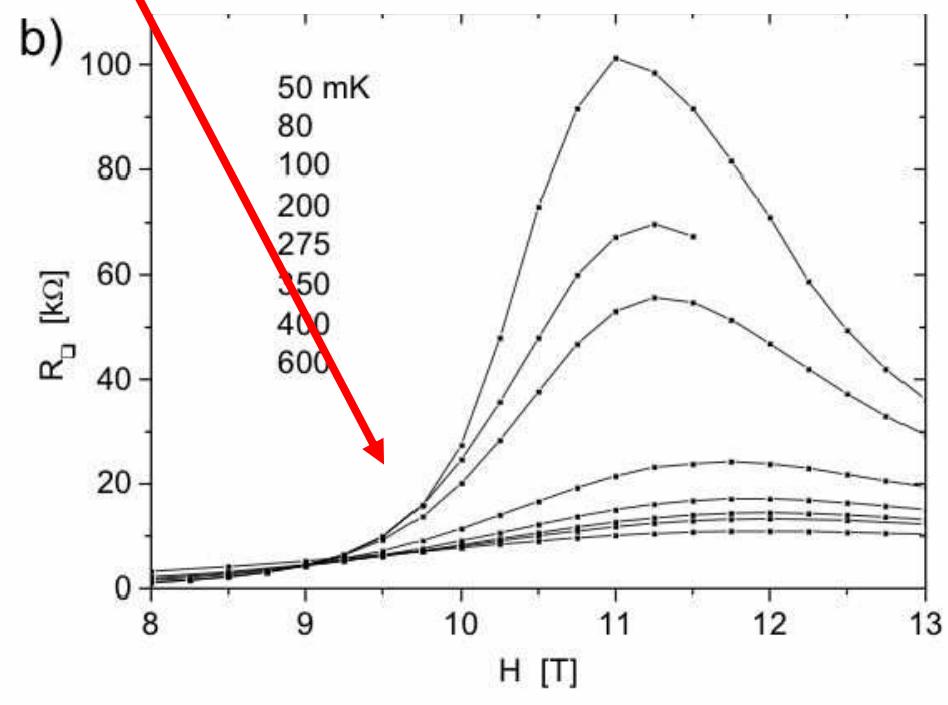
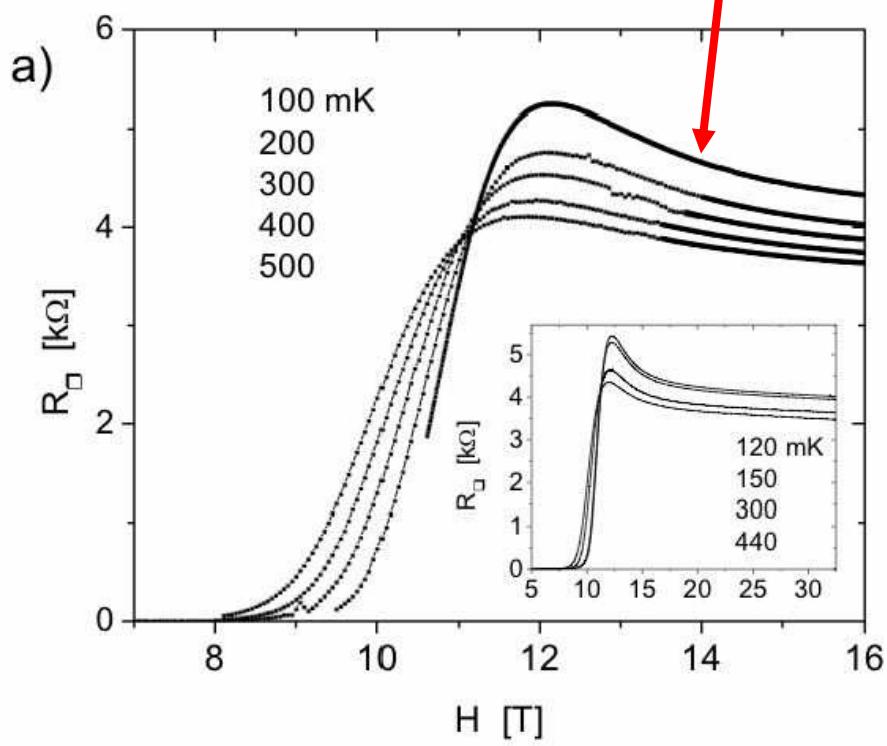
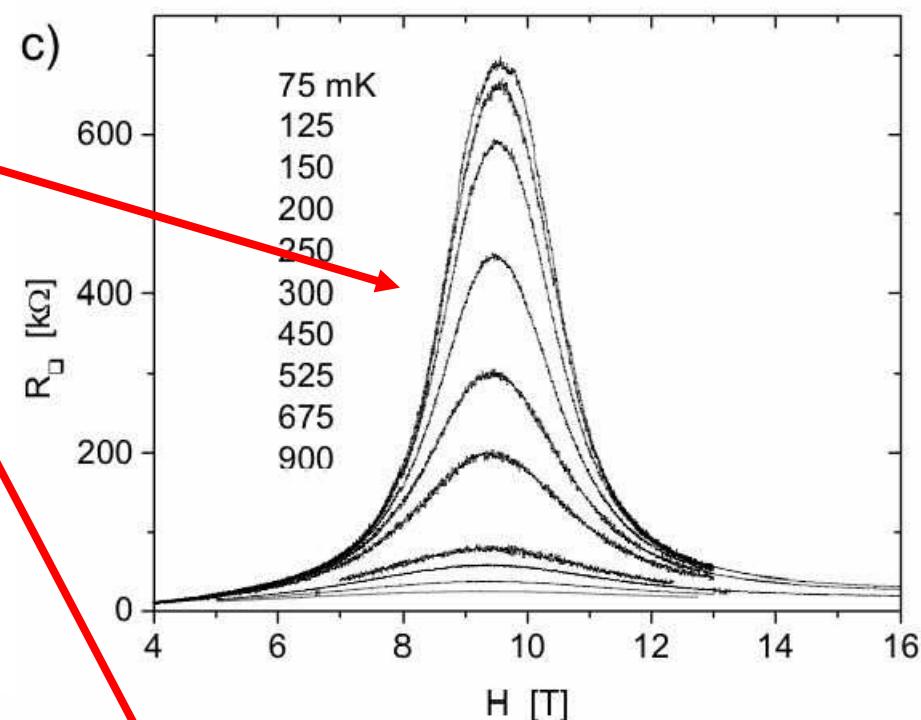
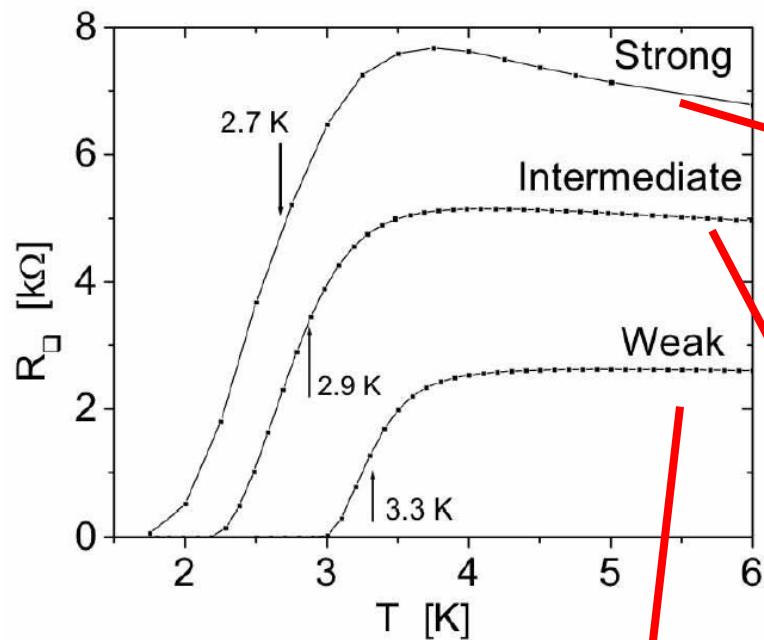


FIG. 1: Zero-field superconducting transitions for three samples. The labels denote the strength of the insulating phase, discussed later in the text. The mean field transition temperatures T_{c0} are indicated by the vertical arrows.

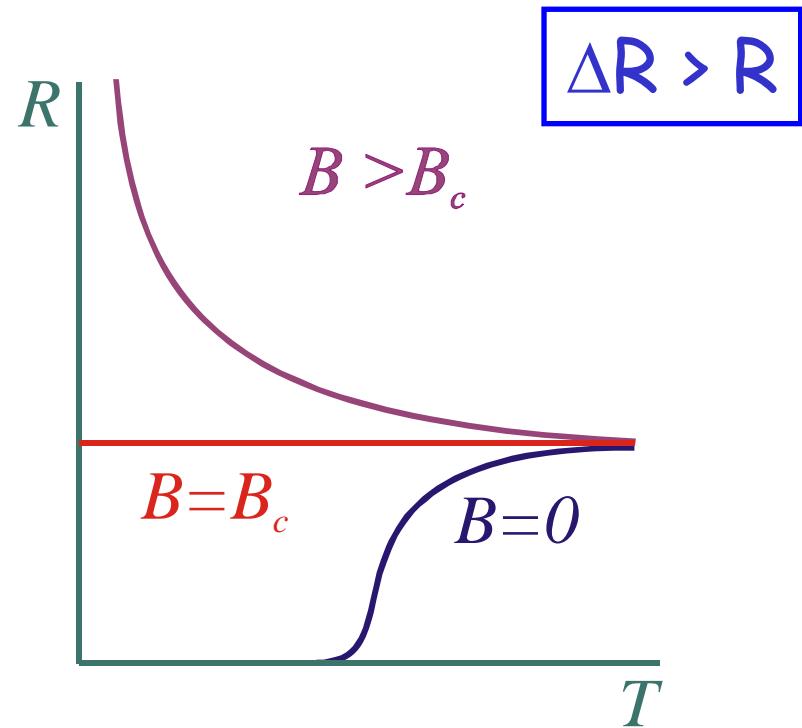
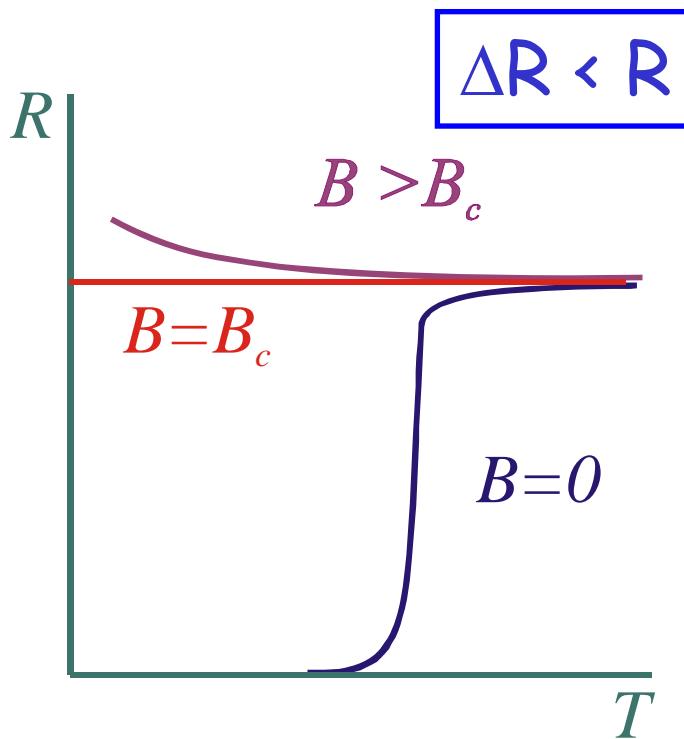


Suppression of Superconductivity by Magnetic Field

Field-induced...

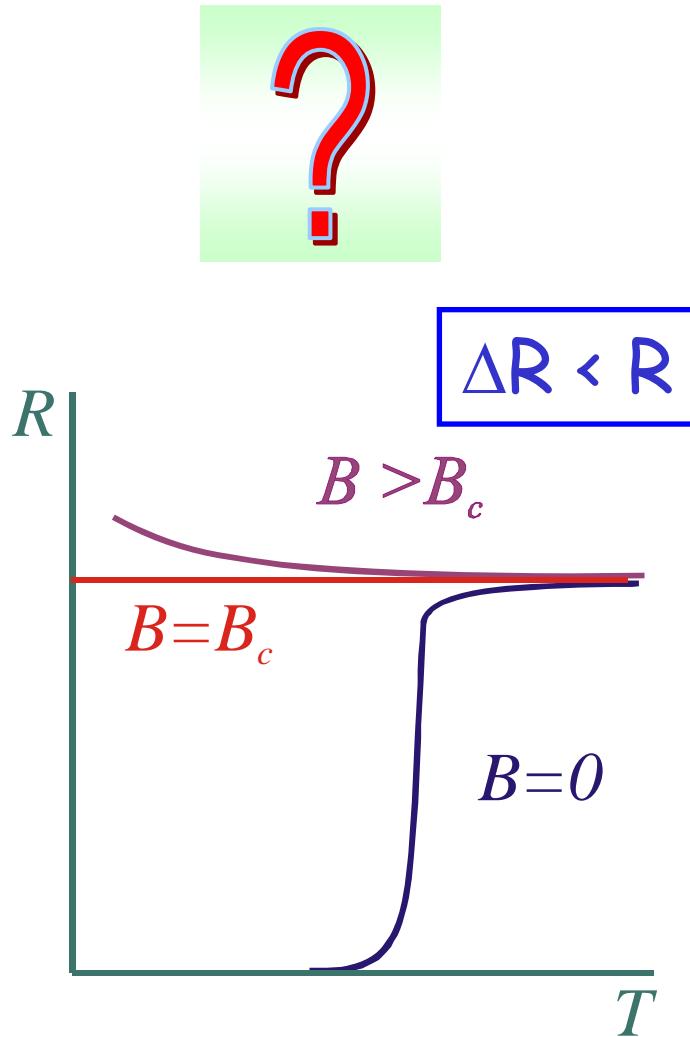


*superconductor –
insulator
transition*



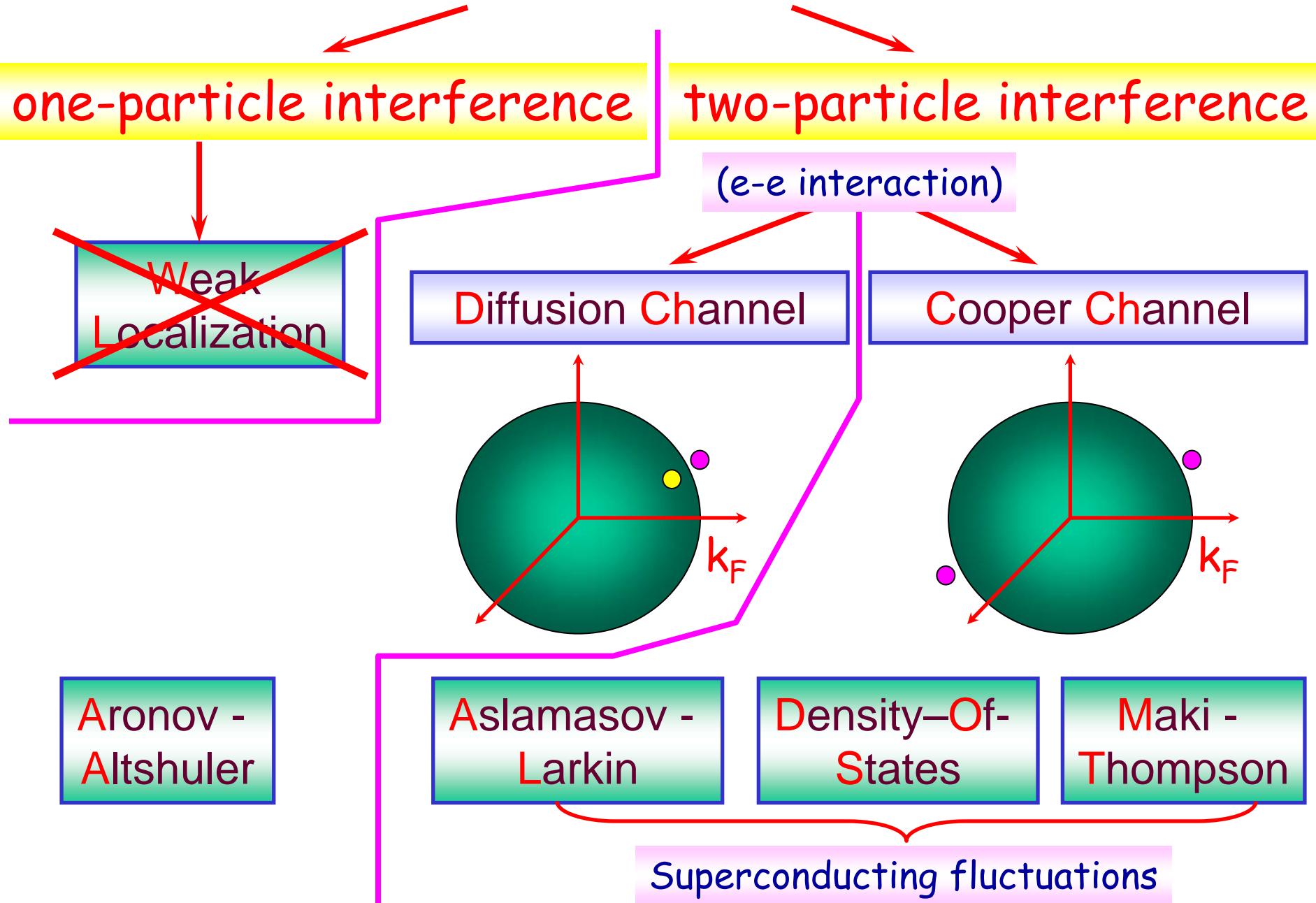
Suppression of Superconductivity by Magnetic Field

Field-induced...



This reminds us of the behavior of a disordered metal with quantum corrections to the conductivity rather than that of an insulator.

Quantum corrections to conductivity



Quantum corrections to conductivity

Aronov -
Altshuler

Aslamasov -
Larkin

Density–Of-
States

Maki -
Thompson

$$\delta_{AA}\sigma(T) \propto \ln(T)$$

Superconducting fluctuations

at $T \ll T_{c0}$ in magnetic field ???

V.M. Galitski and A.I. Larkin, PRB **63**, 174506 (2001)

An analytical expression for the fluctuation conductivity in the region close to the transition line at low temperatures

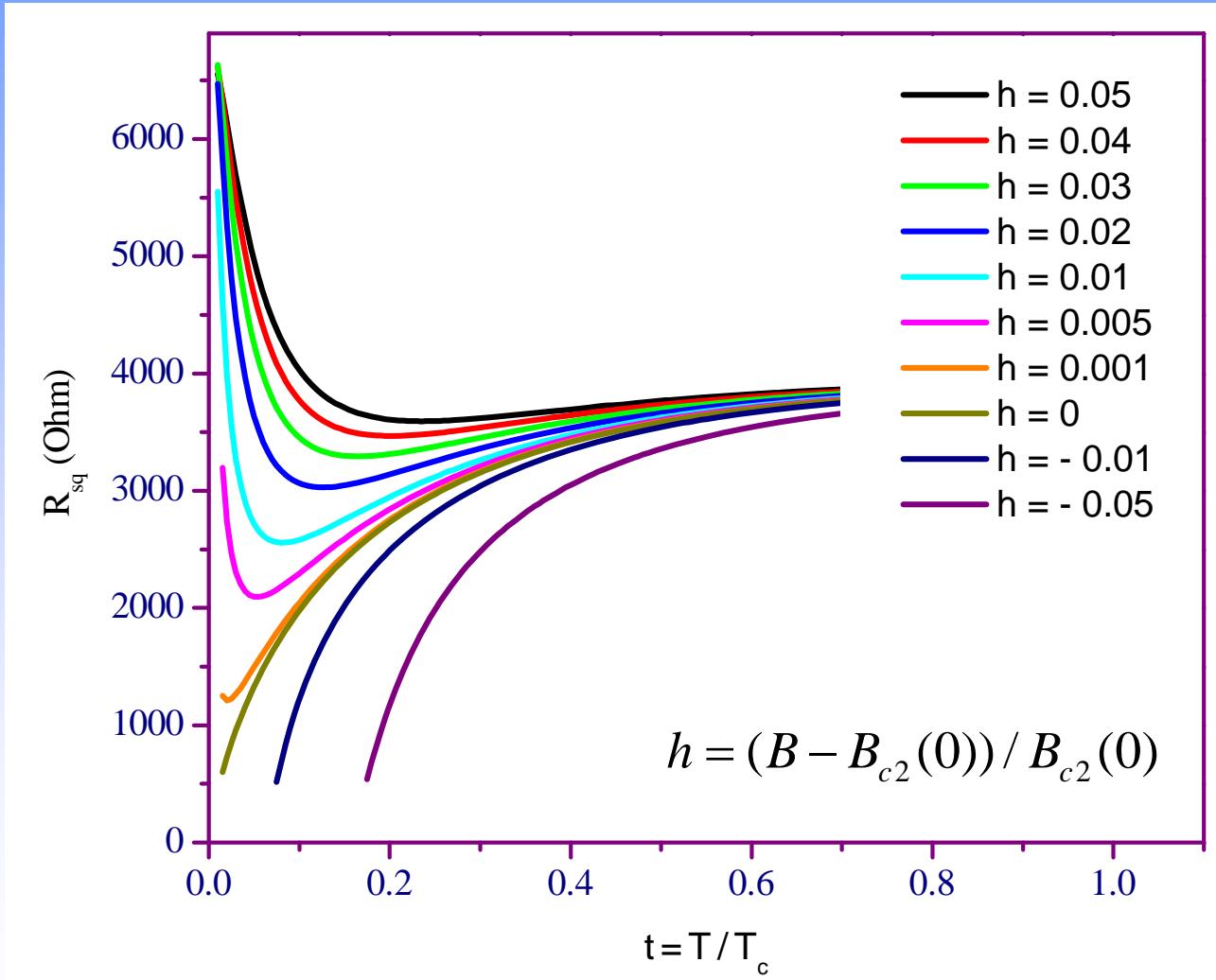
$$T_{c0}\tau \ll 1,$$

$$\delta\sigma = \frac{2e^2}{3\pi^2\hbar} \left[-\ln \frac{r}{h} - \frac{3}{2r} + \psi(r) + 4[r\psi'(r) - 1] \right]$$

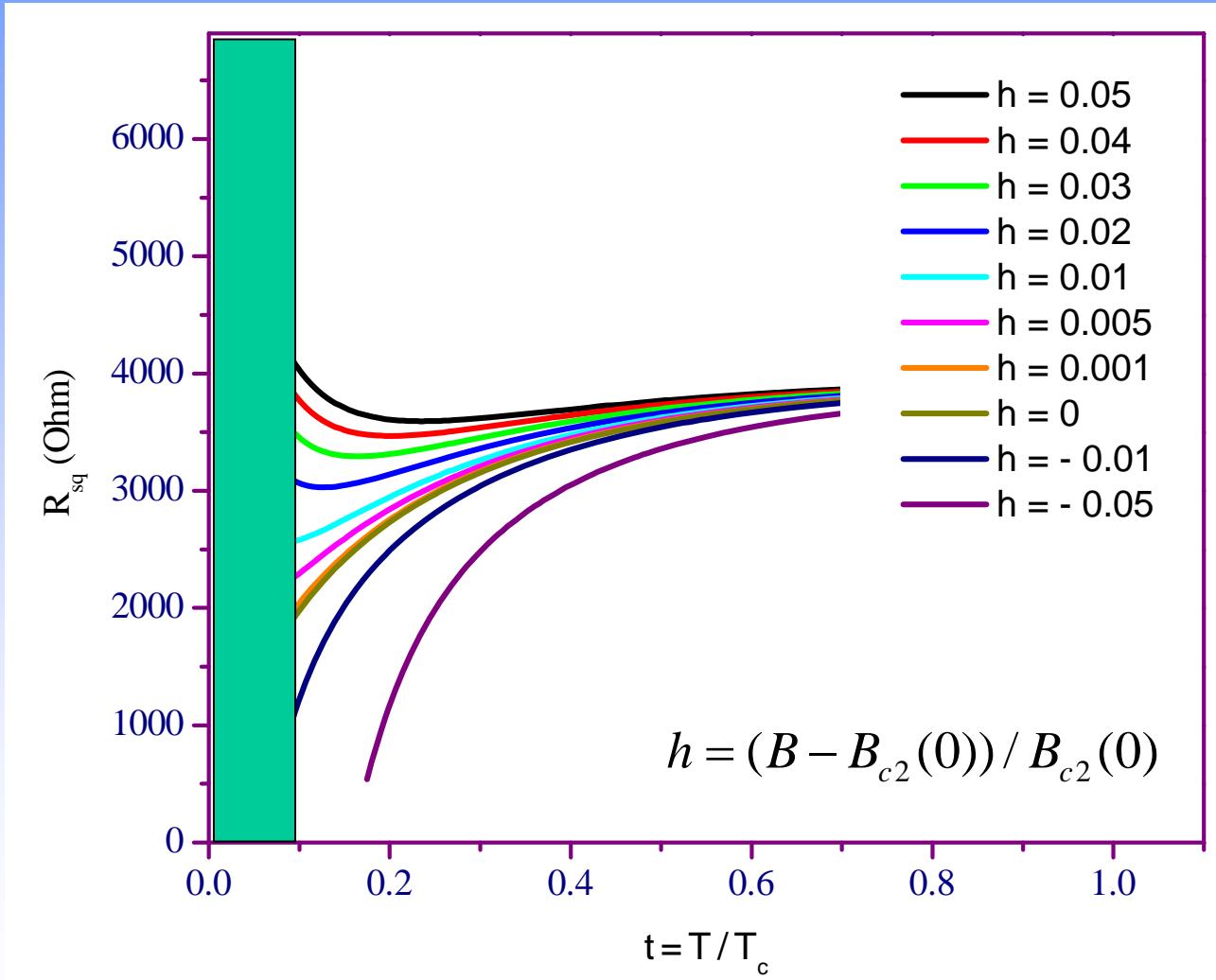
$$t = T / T_{c0} \ll 1, \quad h = (B - B_{c2}(T)) / B_{c2}(0) \ll 1 \quad r = (1/2\gamma)h/t$$

$$\gamma = 1.781$$

Superconducting fluctuations at low temperature



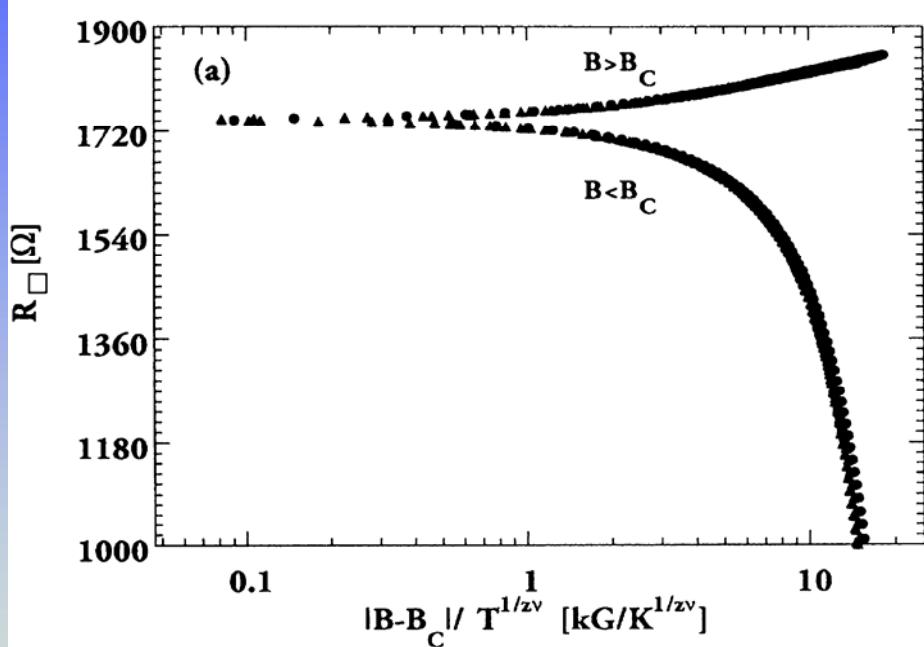
Superconducting fluctuations at low temperature



Superconducting fluctuations at low temperature

Scaling

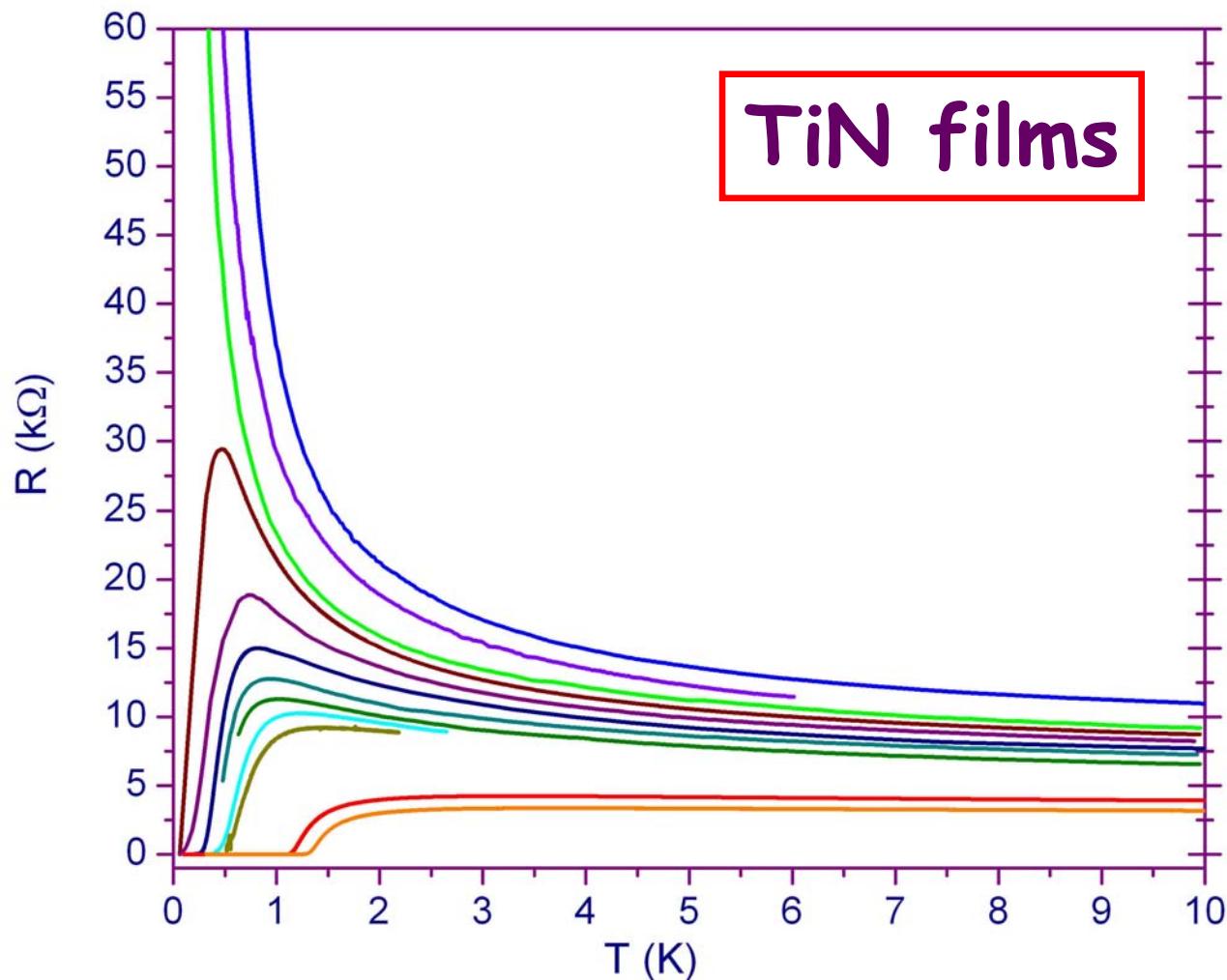
A.Yazdani and A.Kapitulnik (1995)

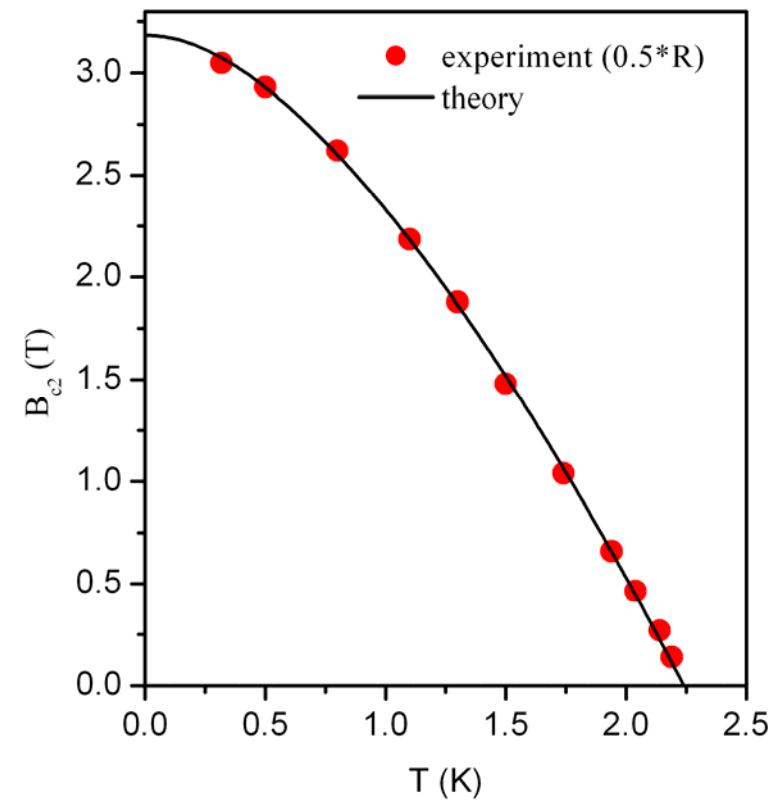
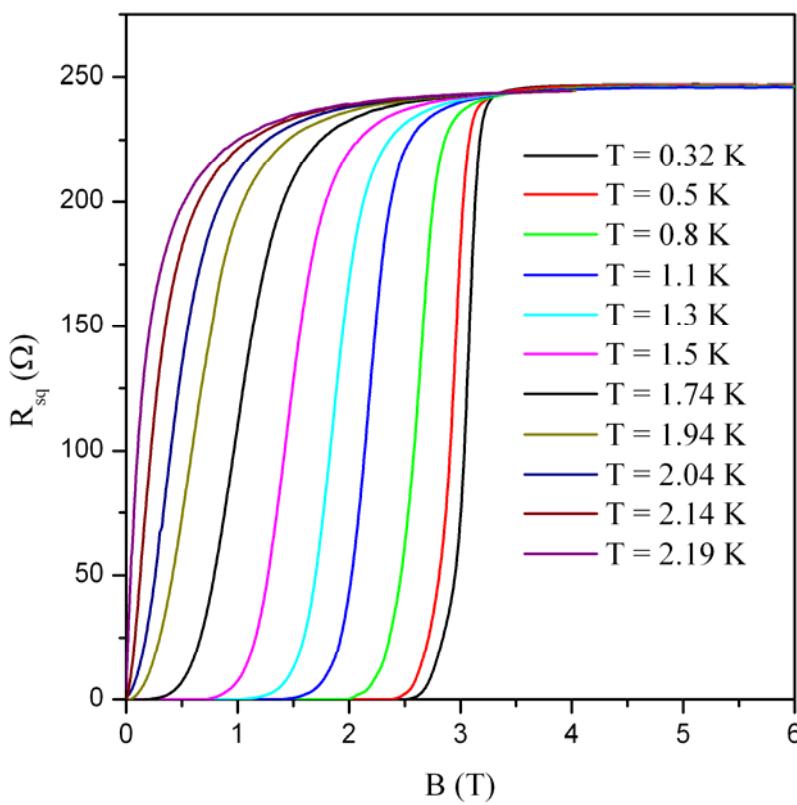
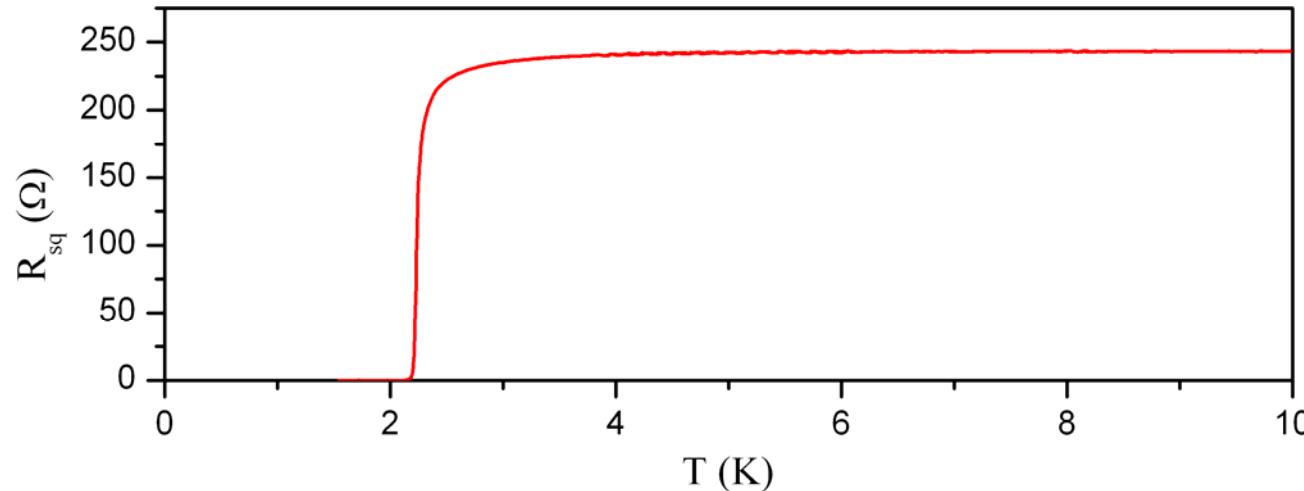


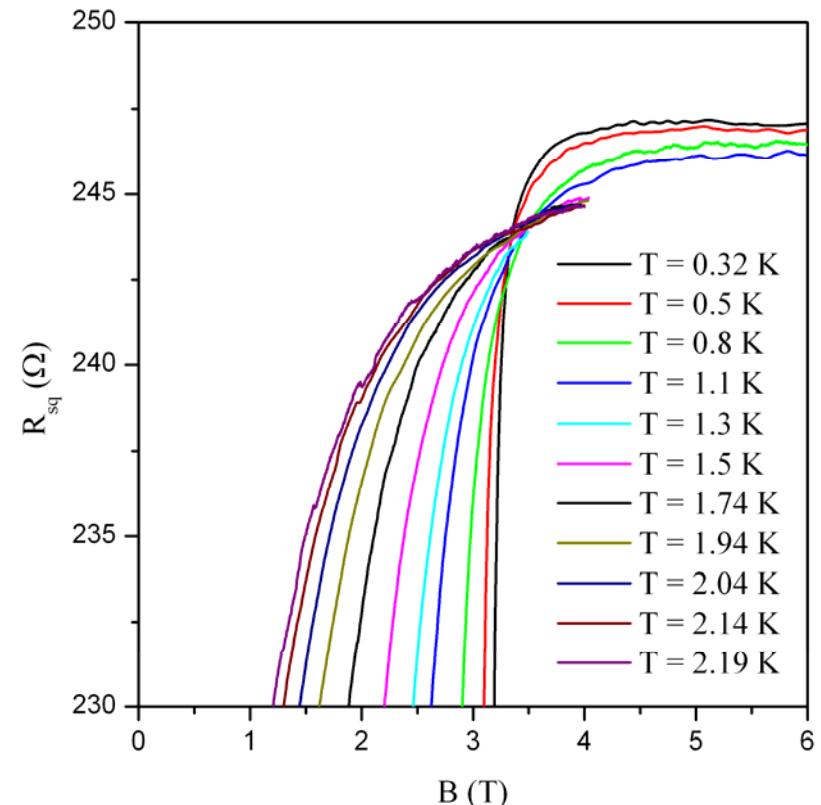
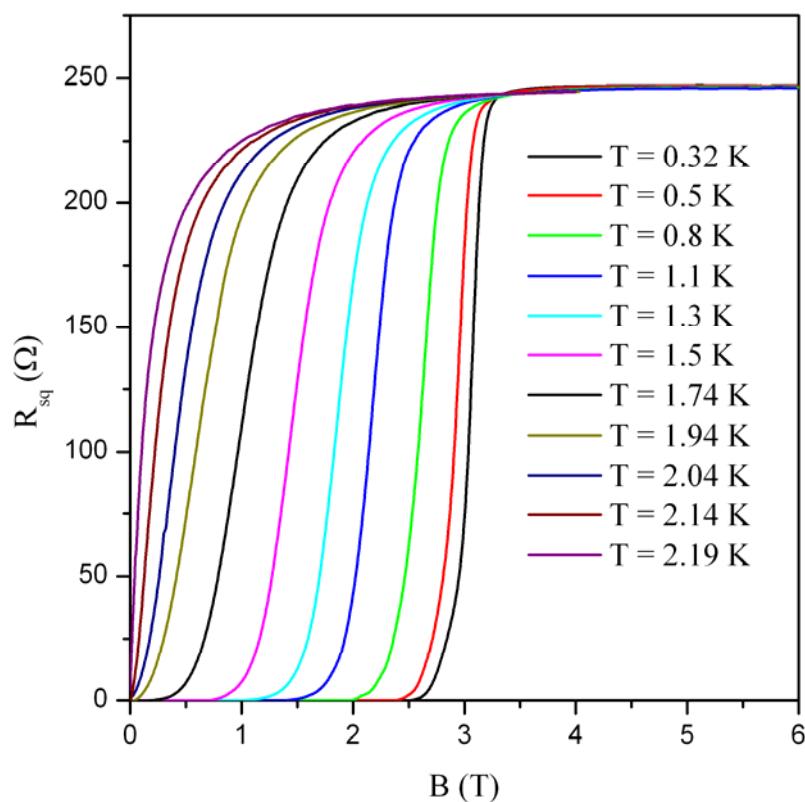
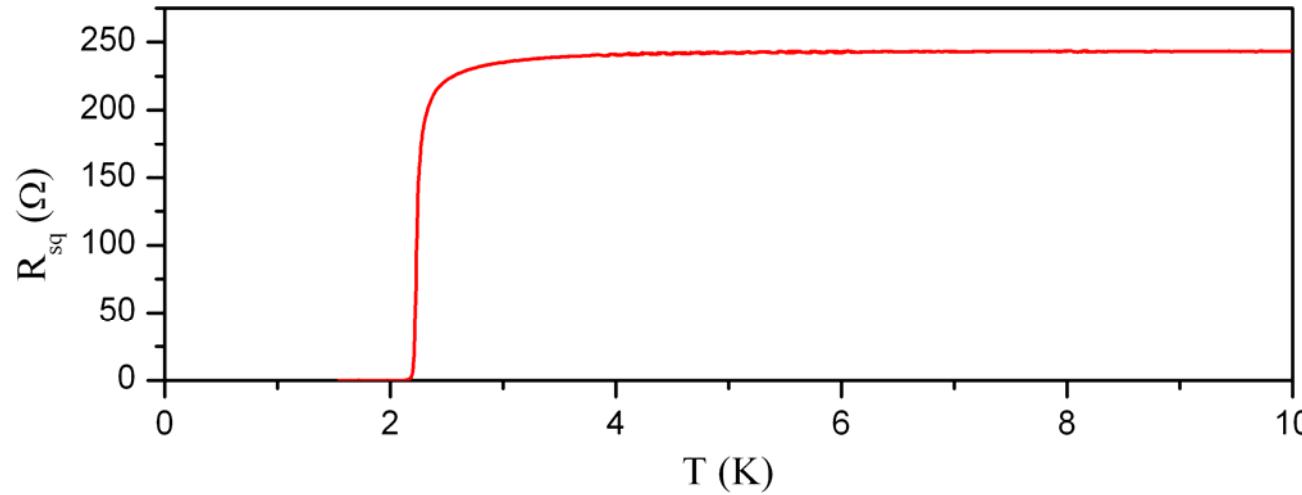
T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602



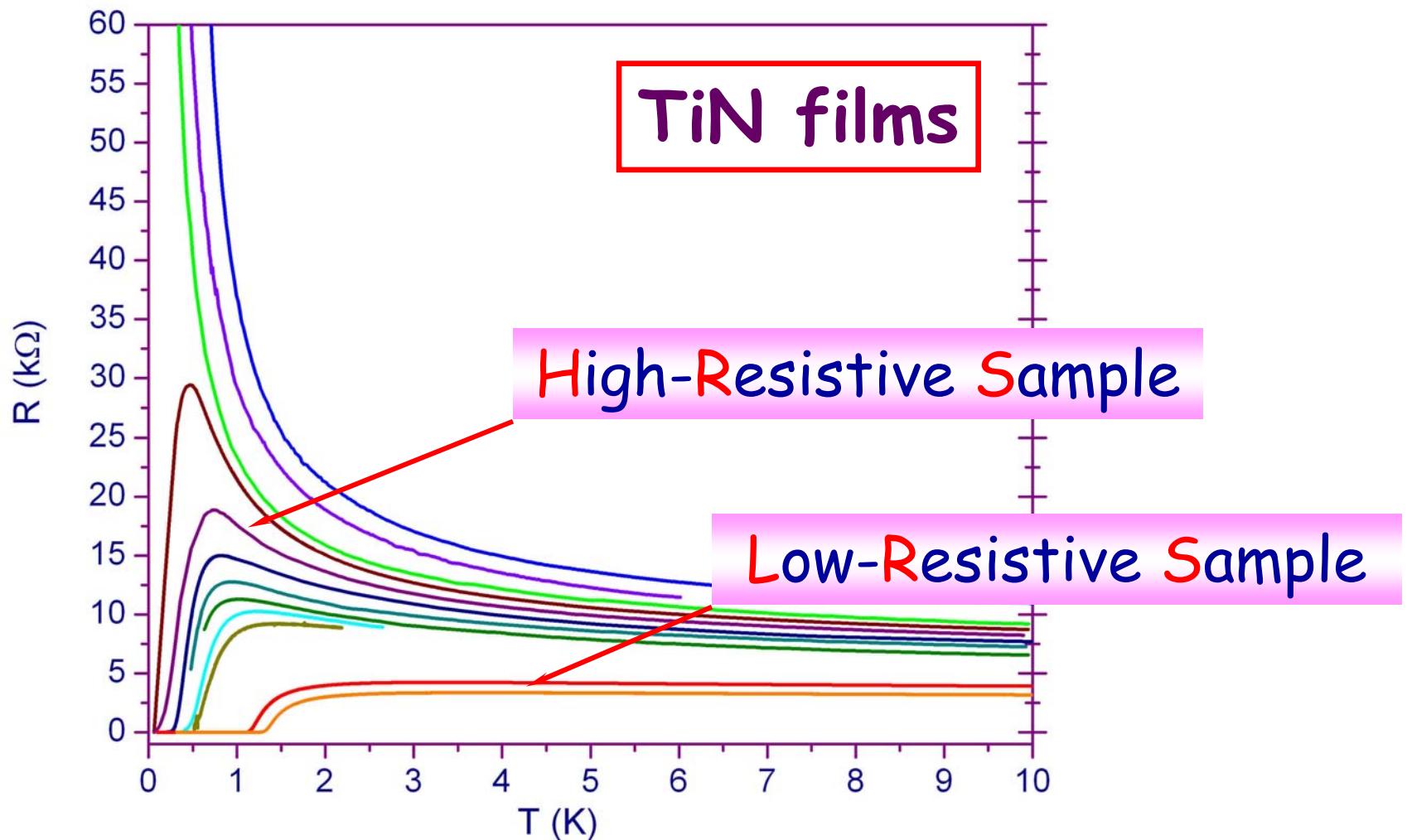




T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602

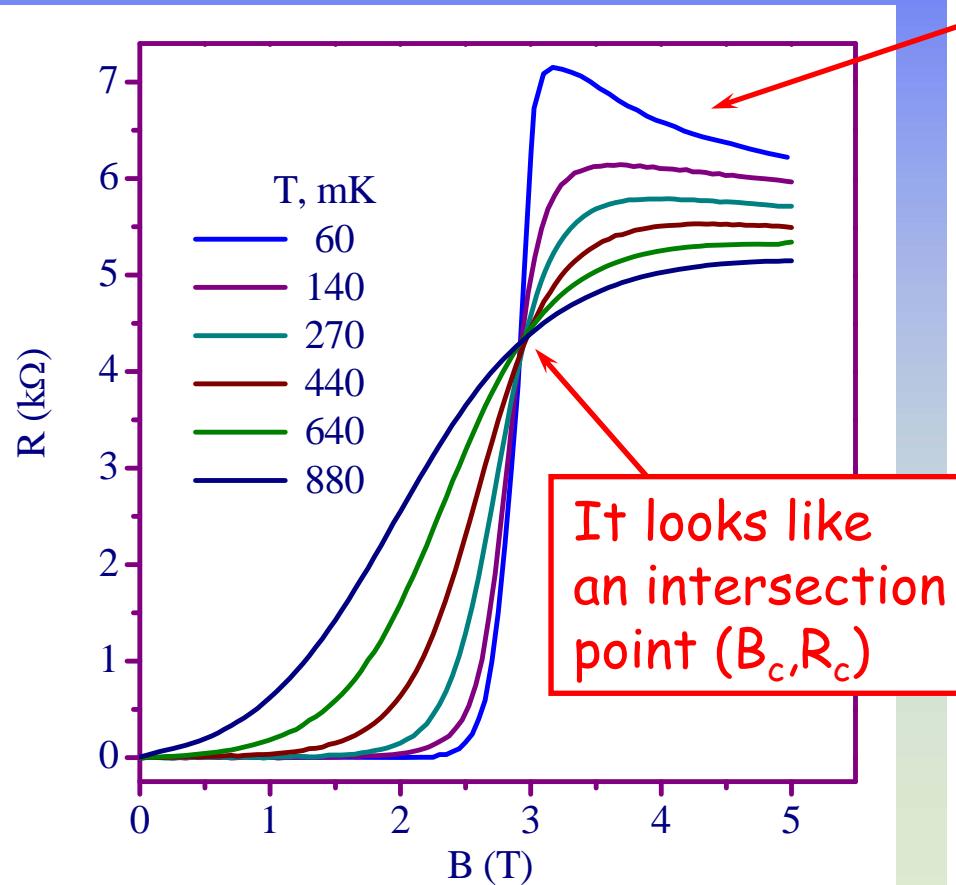


Experiment

TiN films

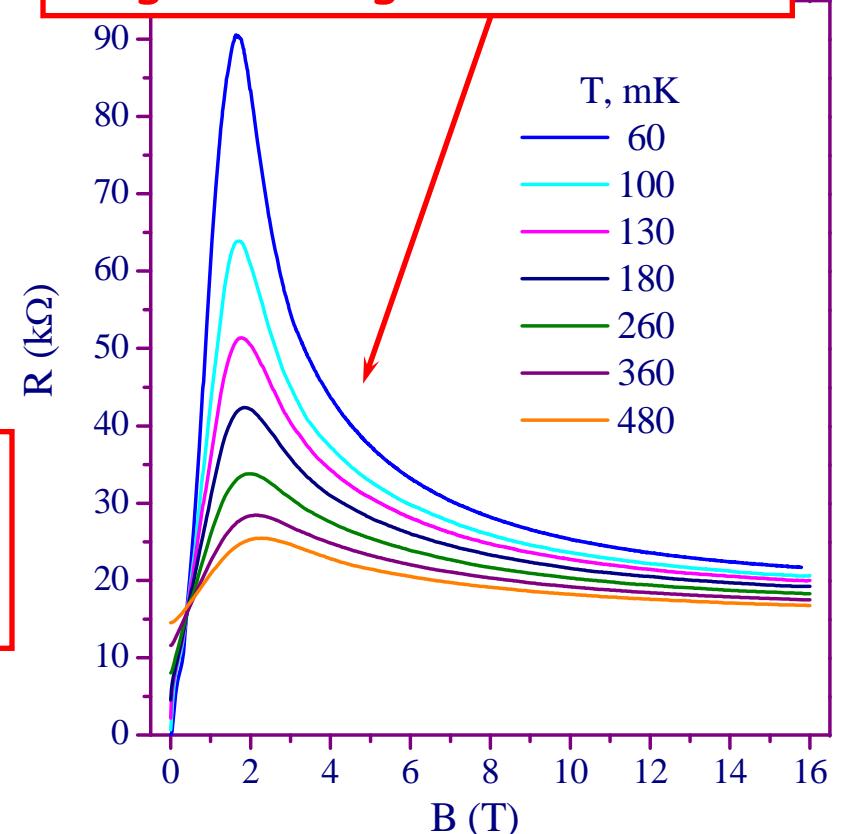
Magnetic-field dependence

Low-Resistive Sample



High-Resistive Sample

Negative magnetoresistance

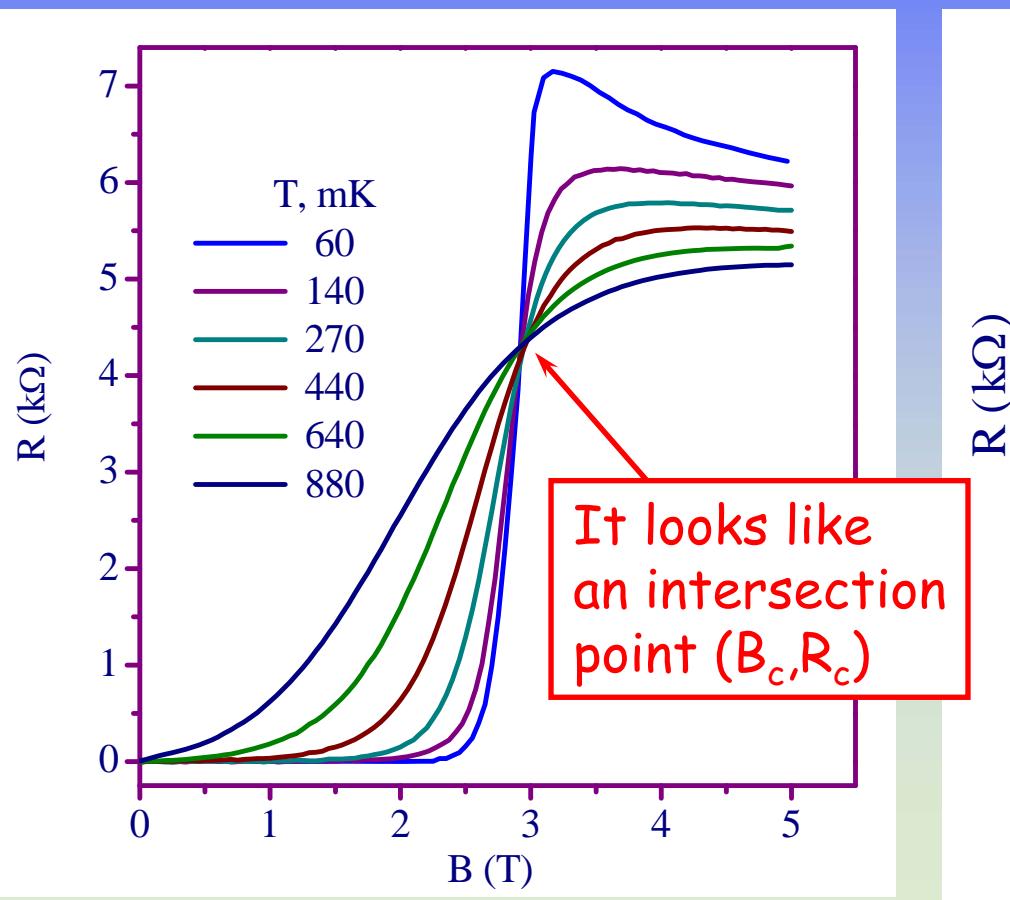


Experiment

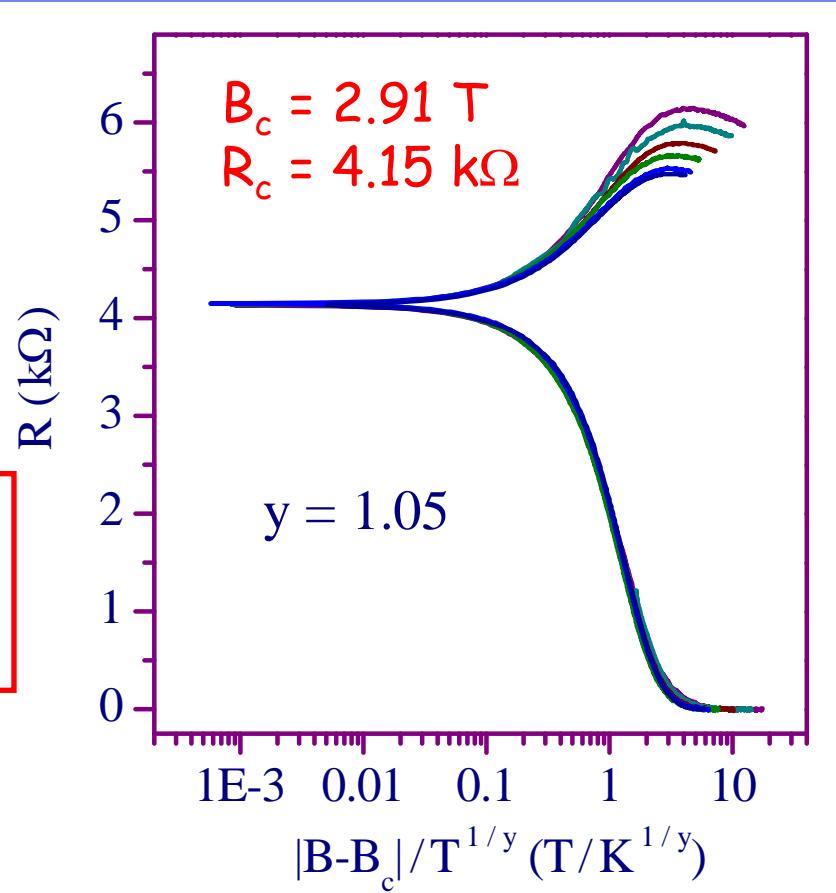
TiN films

Magnetic-field dependence

Low-Resistive Sample



Scaling

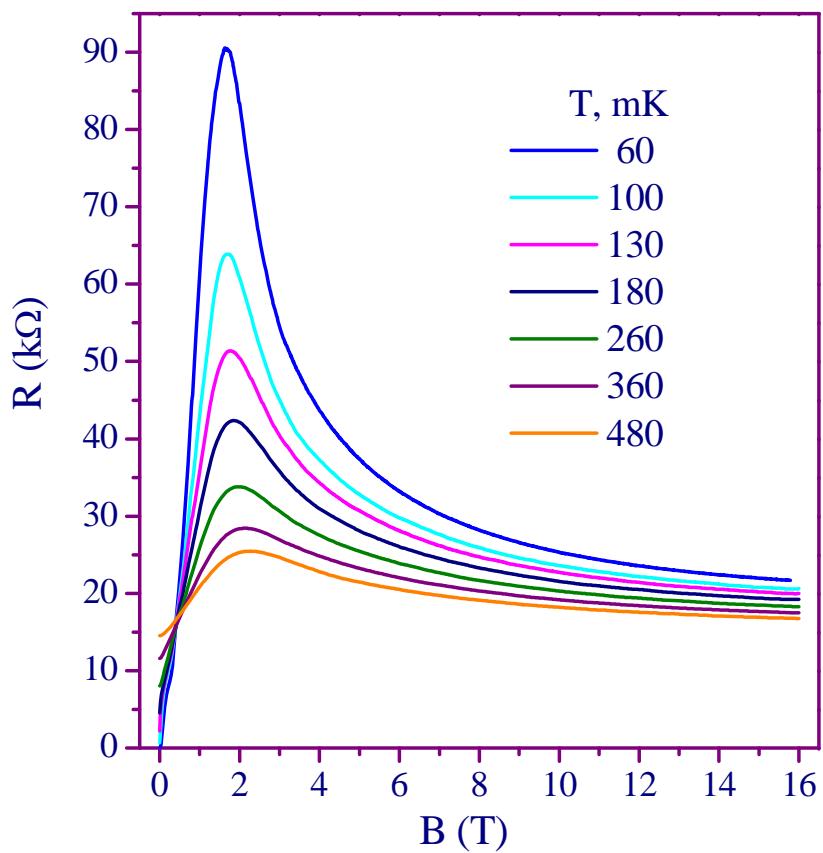


Experiment

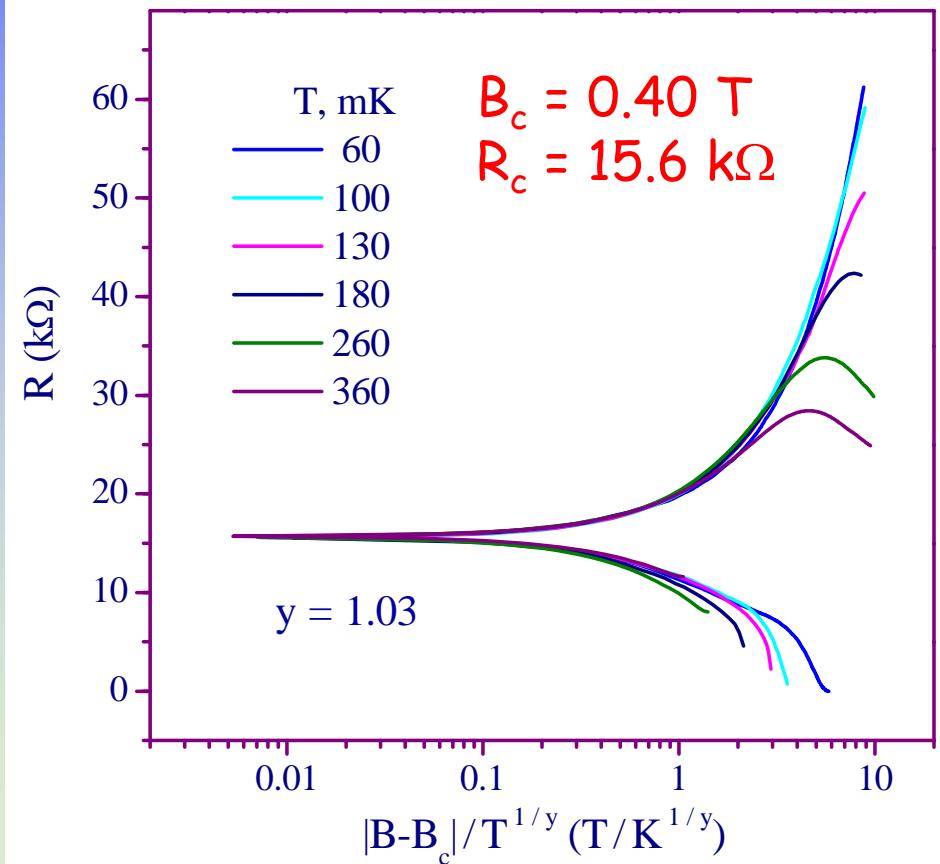
TiN films

Magnetic-field dependence

High-Resistive Sample



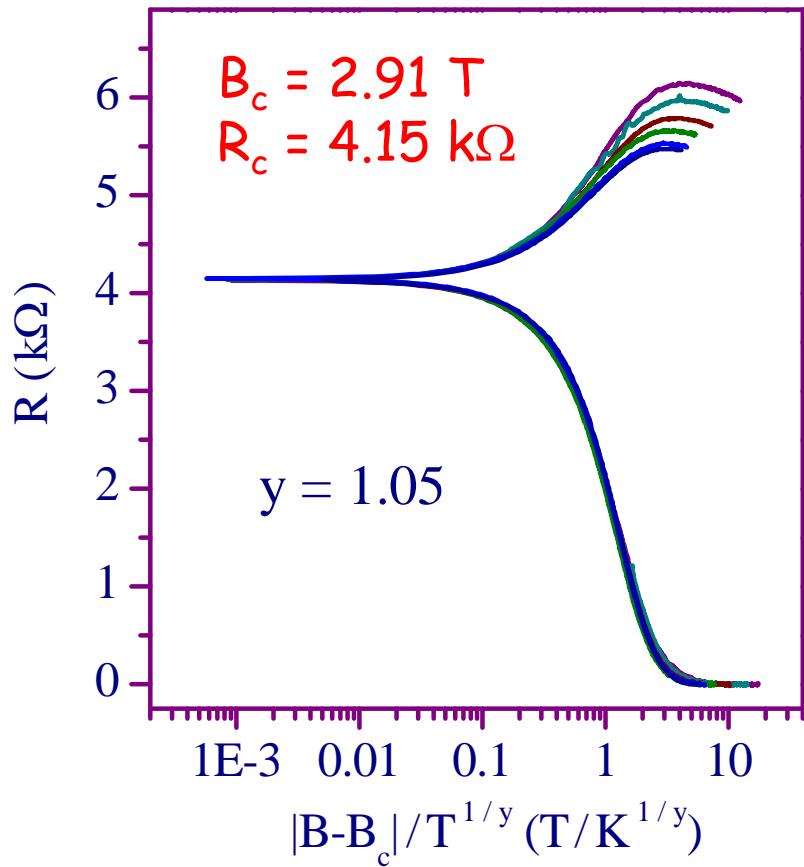
Scaling



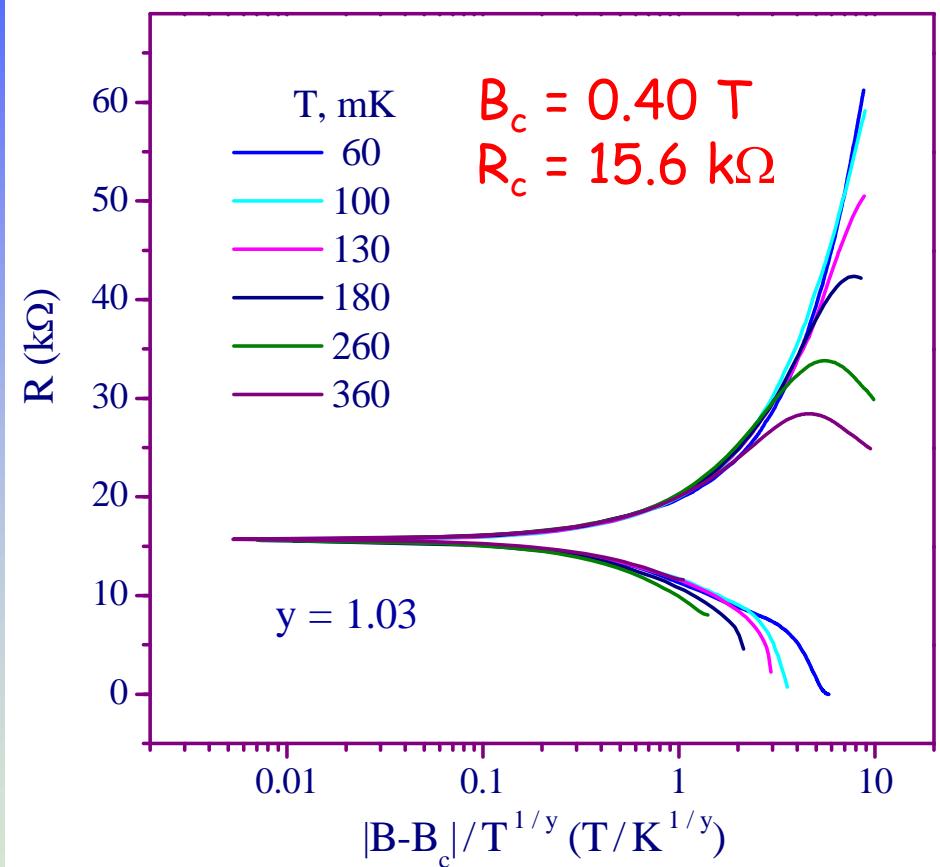
Scaling

Magnetic-field dependence

Low-Resistive Sample



High-Resistive Sample



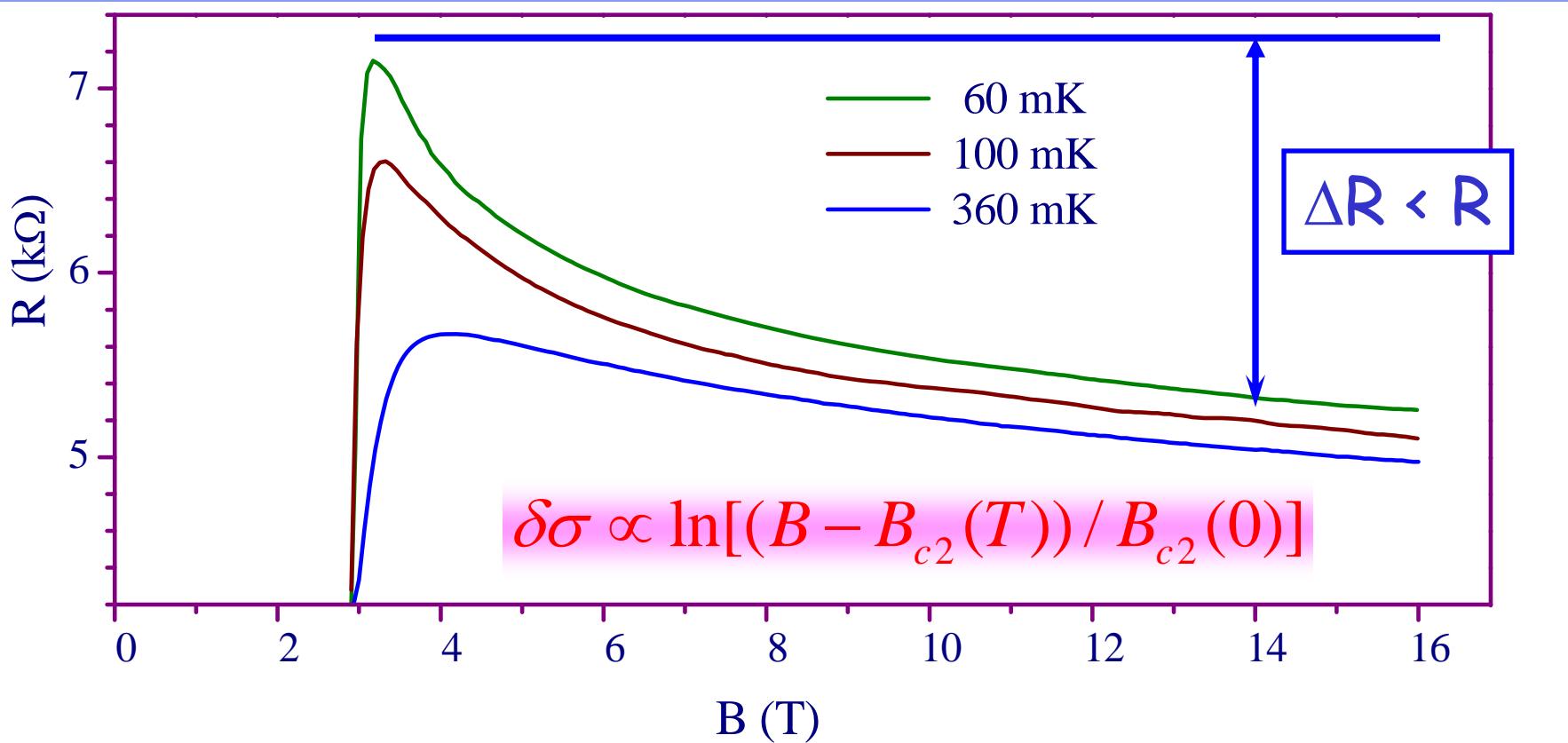
y ($= \nu z$) ≈ 1 for both samples !

Magnetic-field dependence

Low-Resistive Sample

Negative magnetoresistance

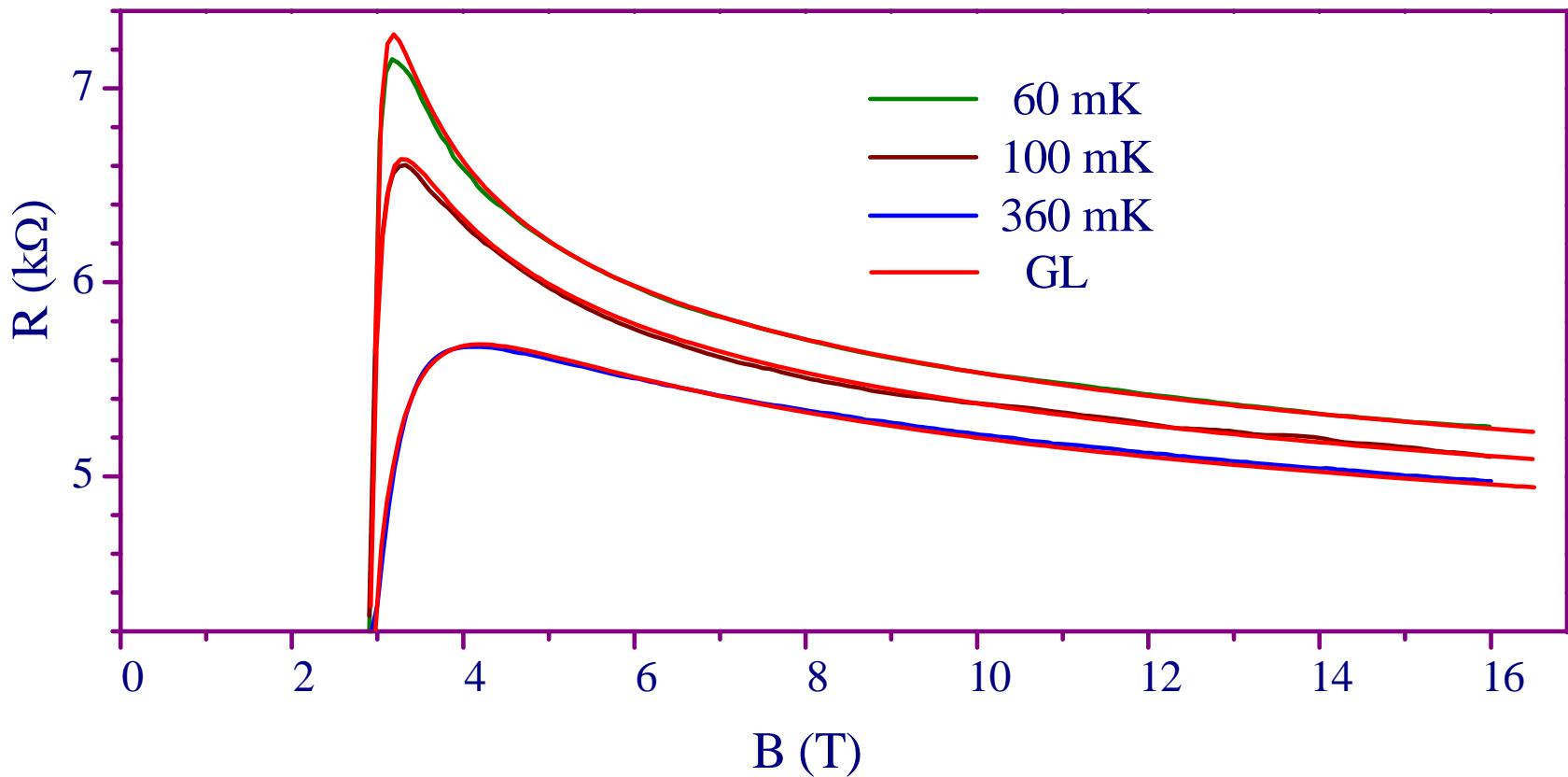
comparison with Galitski - Larkin calculations
of the quantum corrections



comparison with Galitski - Larkin calculations
of the quantum corrections

$T_c = 2 \text{ K}$, $B_{c2}(0) = 2.8 \text{ T}$

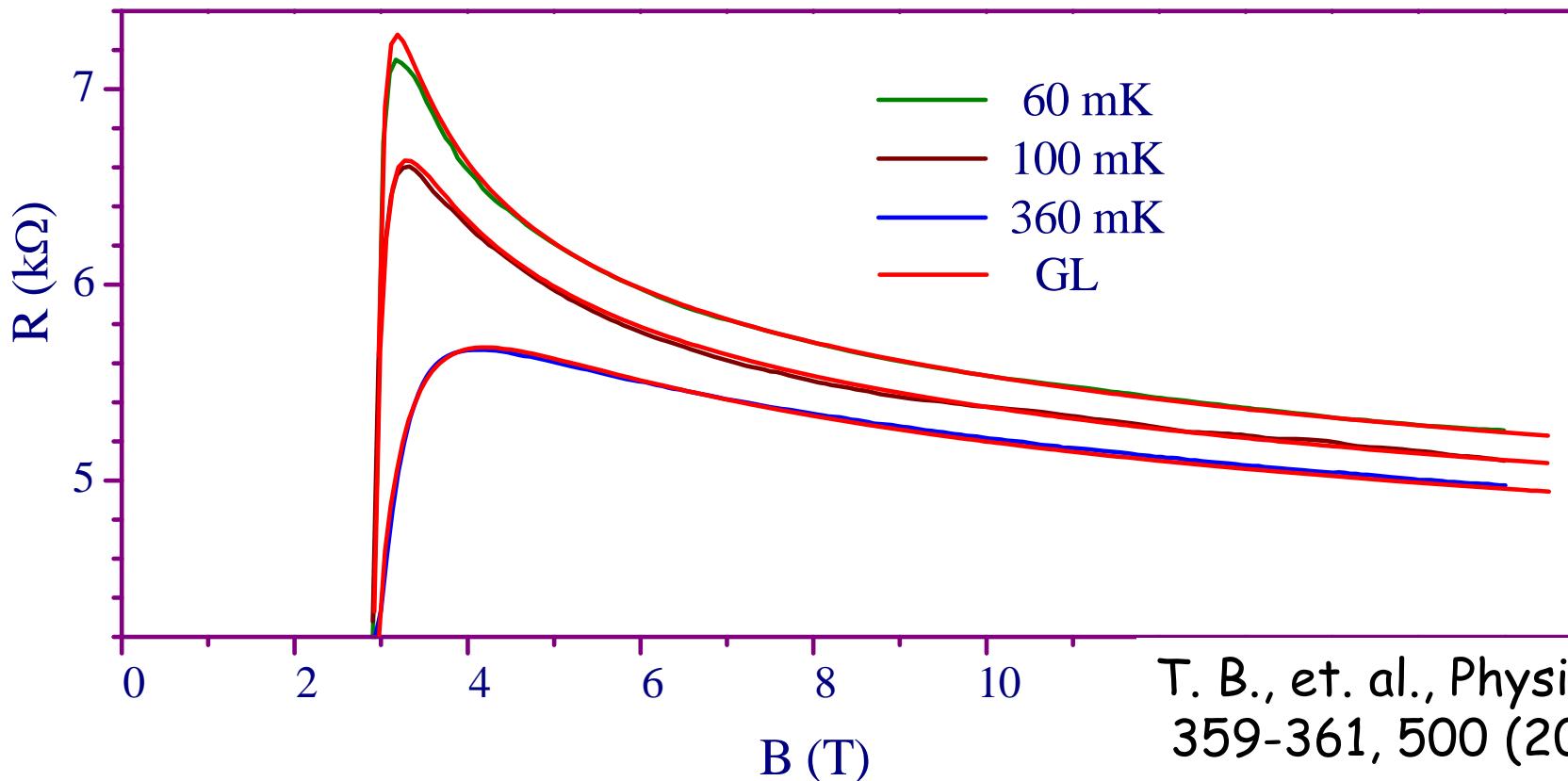
$$\delta\sigma = \frac{2e^2}{3\pi^2\hbar} \left[-\ln \frac{r}{h} - \frac{3}{2r} + \psi(r) + 4[r\psi'(r) - 1] \right]$$



comparison with Galitski - Larkin calculations
of the quantum corrections

$T_c = 2 \text{ K}$, $B_{c2}(0) = 2.8 \text{ T}$

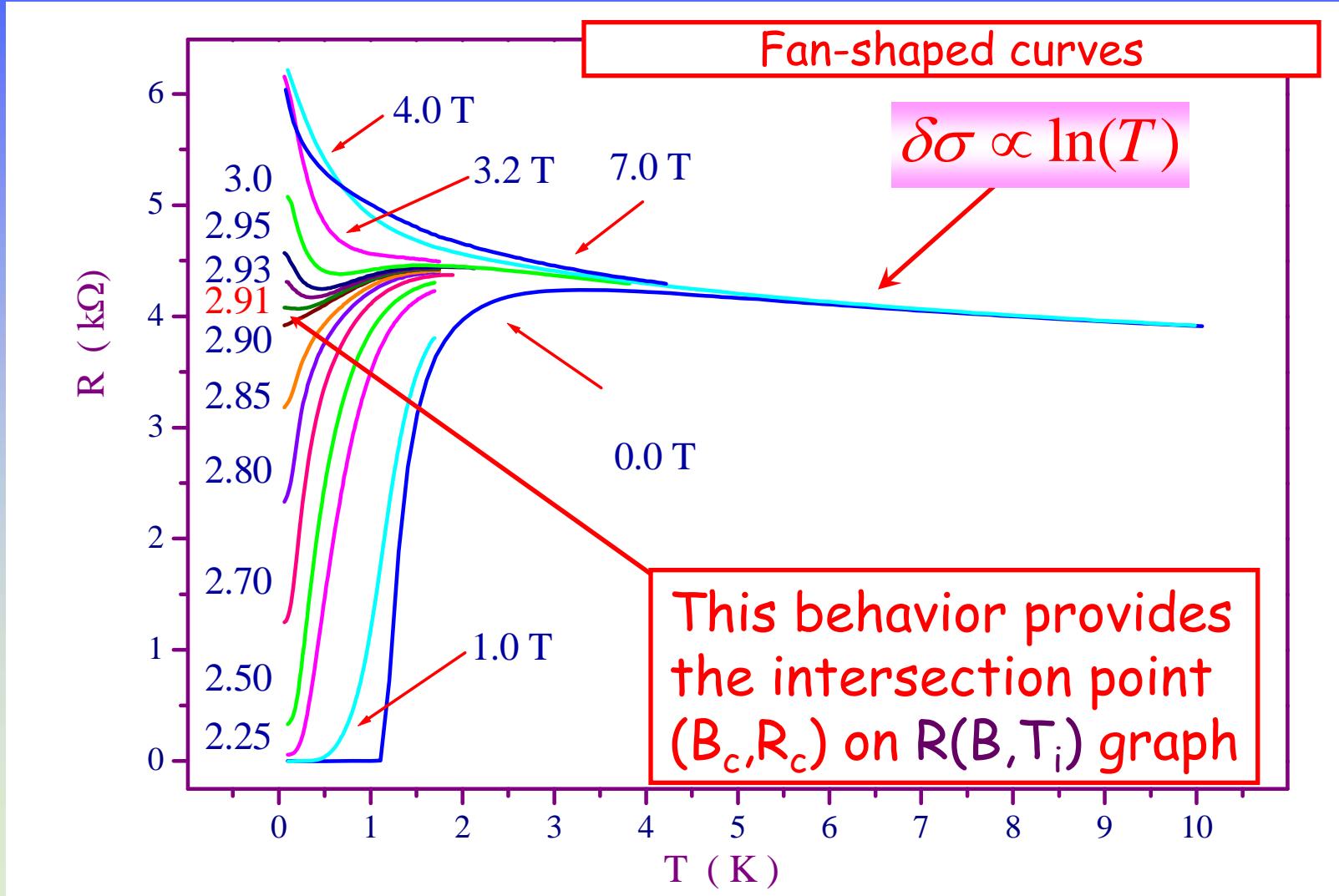
$$\delta\sigma = \frac{2e^2}{3\pi^2\hbar} \left[-\ln \frac{r}{h} - \frac{3}{2r} + \psi(r) + 4[r\psi'(r) - 1] \right]$$



Temperature dependence

Low-Resistive Sample

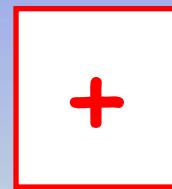
$R(T, B_i)$



LRS

Temperature dependence

comparison with
Galitski - Larkin
calculations
of the quantum
corrections

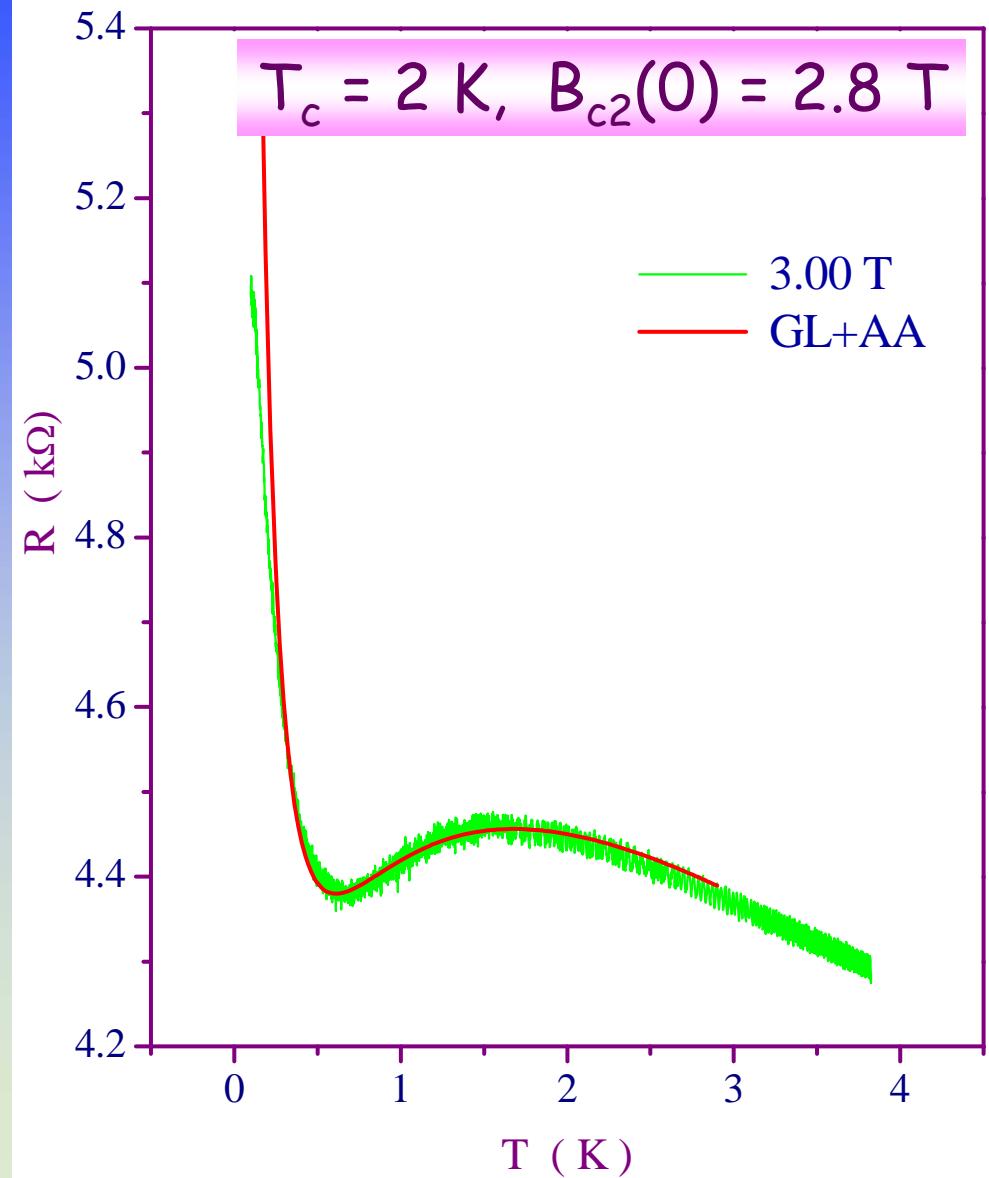


Aronov -
Altshuler

$$\delta\sigma_{AA} \propto \ln(T)$$

Cooper Channel

Diffusion Channel

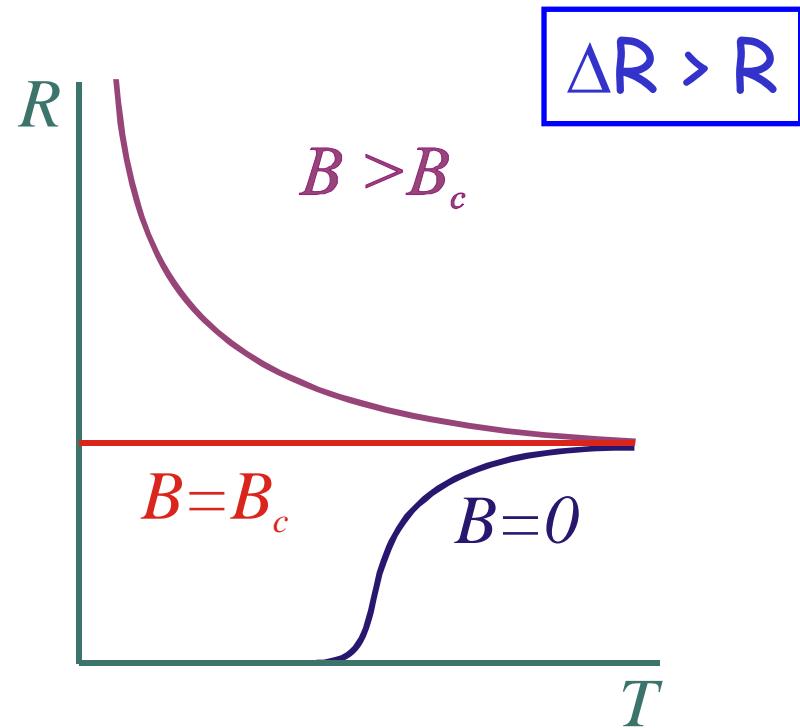
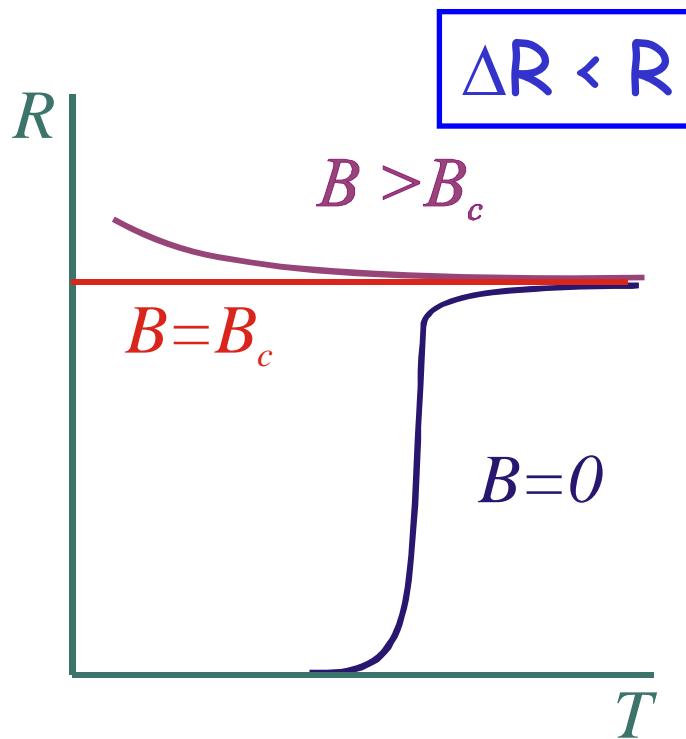


Suppression of Superconductivity by Magnetic Field

Field-induced...

*superconductor –
metal
transition*

*superconductor –
insulator
transition*



Superconducting fluctuations and SIT related behavior in low resistive superconducting films

*superconductor –
metal
transition*

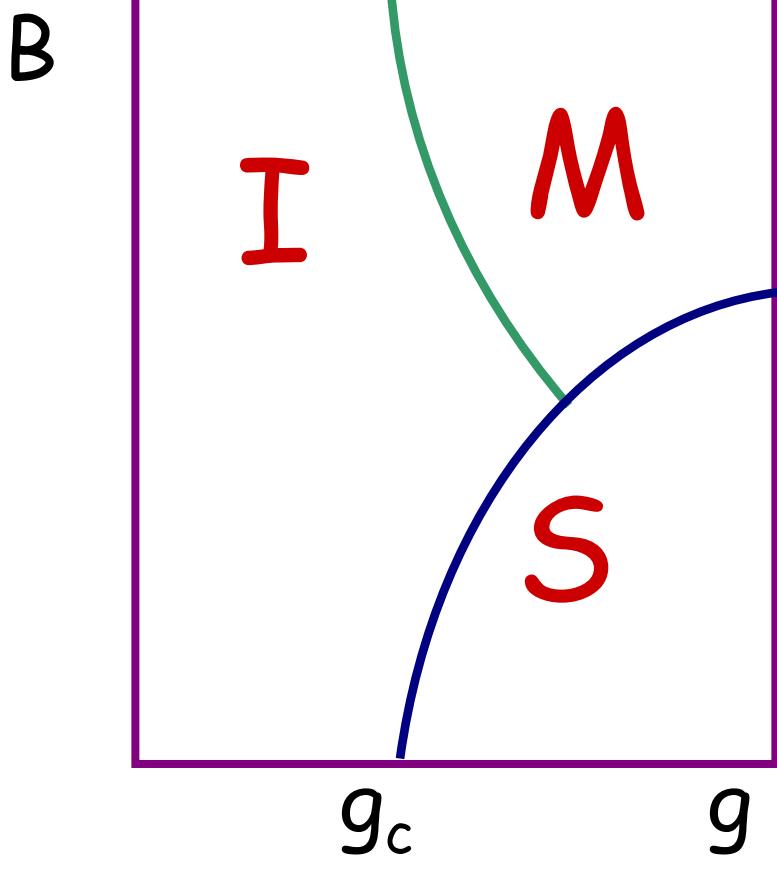
V.M. Galitski and A.I. Larkin,
PRB **63**, 174506 (2001)

*superconductor –
insulator
transition*

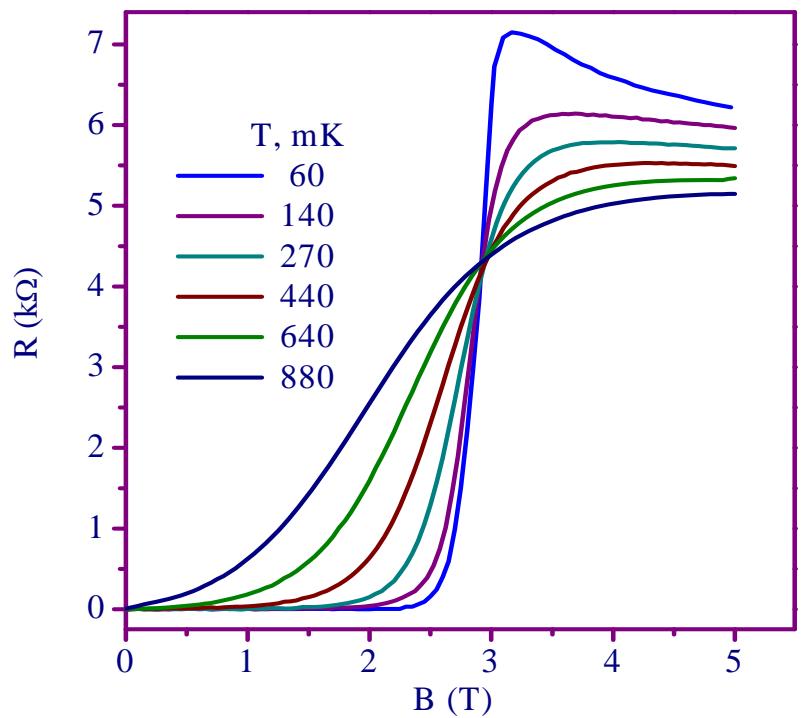
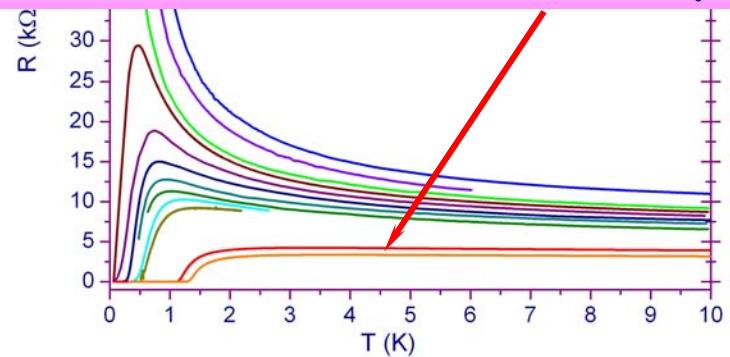
Common features

- ✓ Fan-shaped structure of $R(T, B_i)$ curves
- ✓ Negative magnetoresistance in high fields
- ✓ Scaling

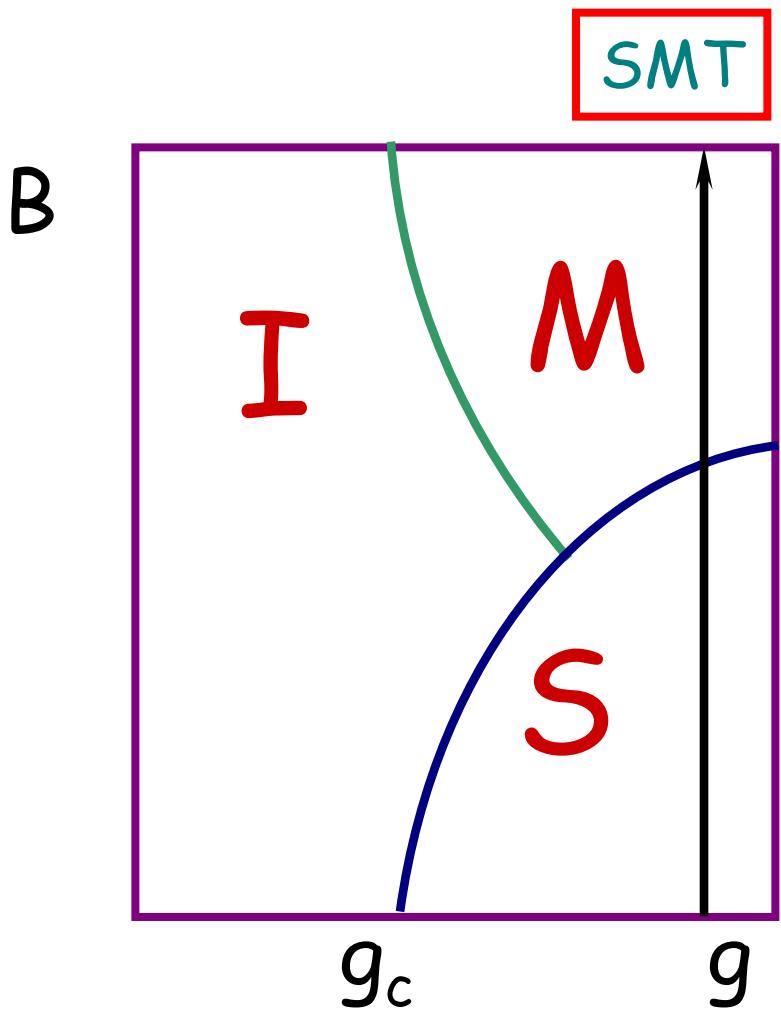
schematic phase diagram



Low-Resistive Sample

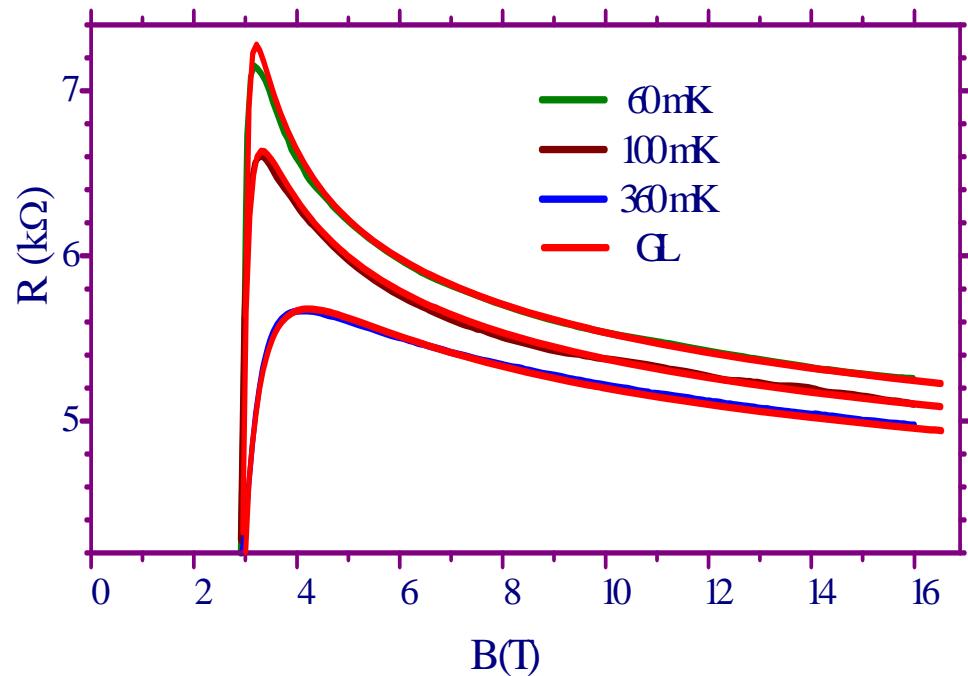


schematic phase diagram

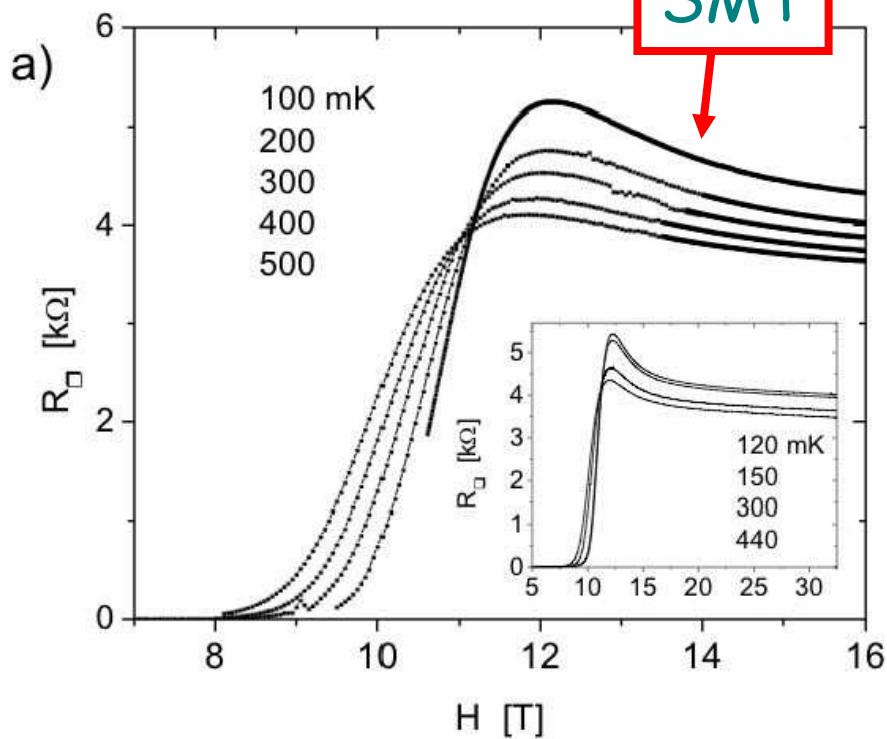
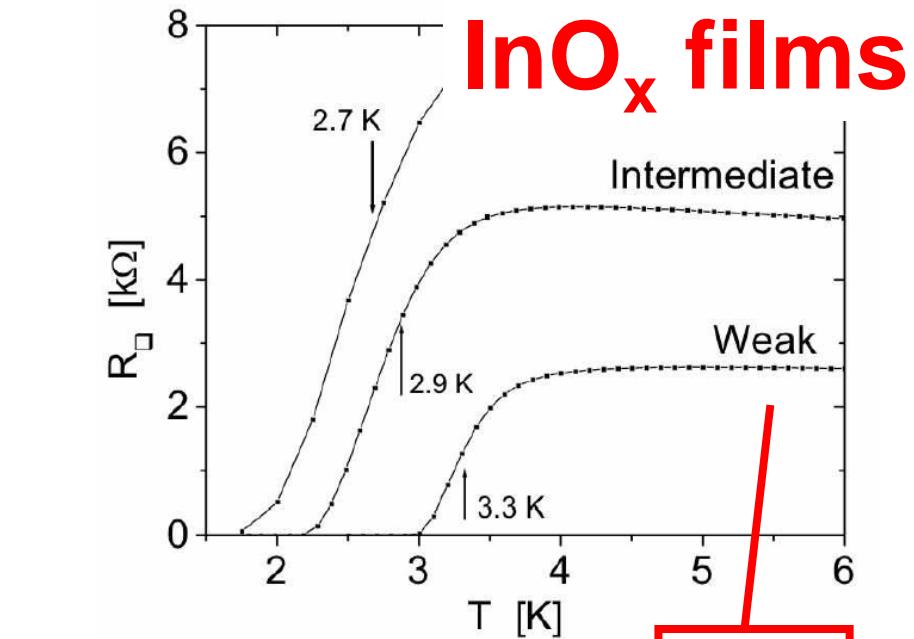
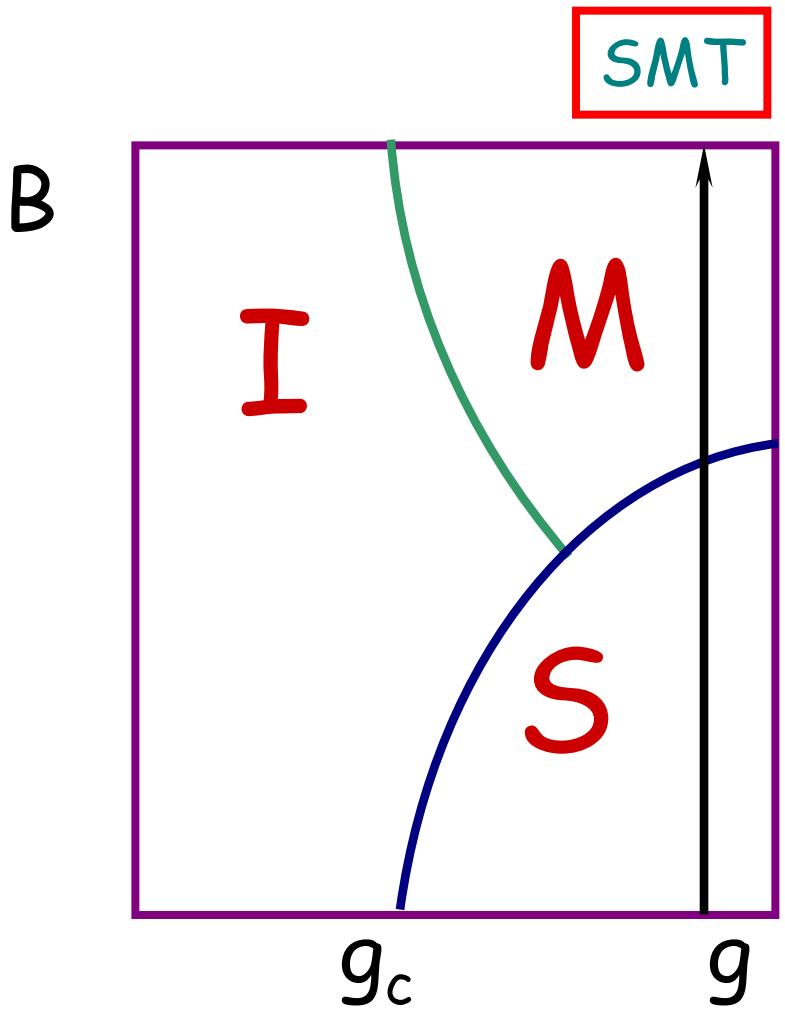


comparison with Galitski - Larkin
calculations of the quantum corrections

T. Baturina, et. al., Physica B
359-361, 500 (2005)



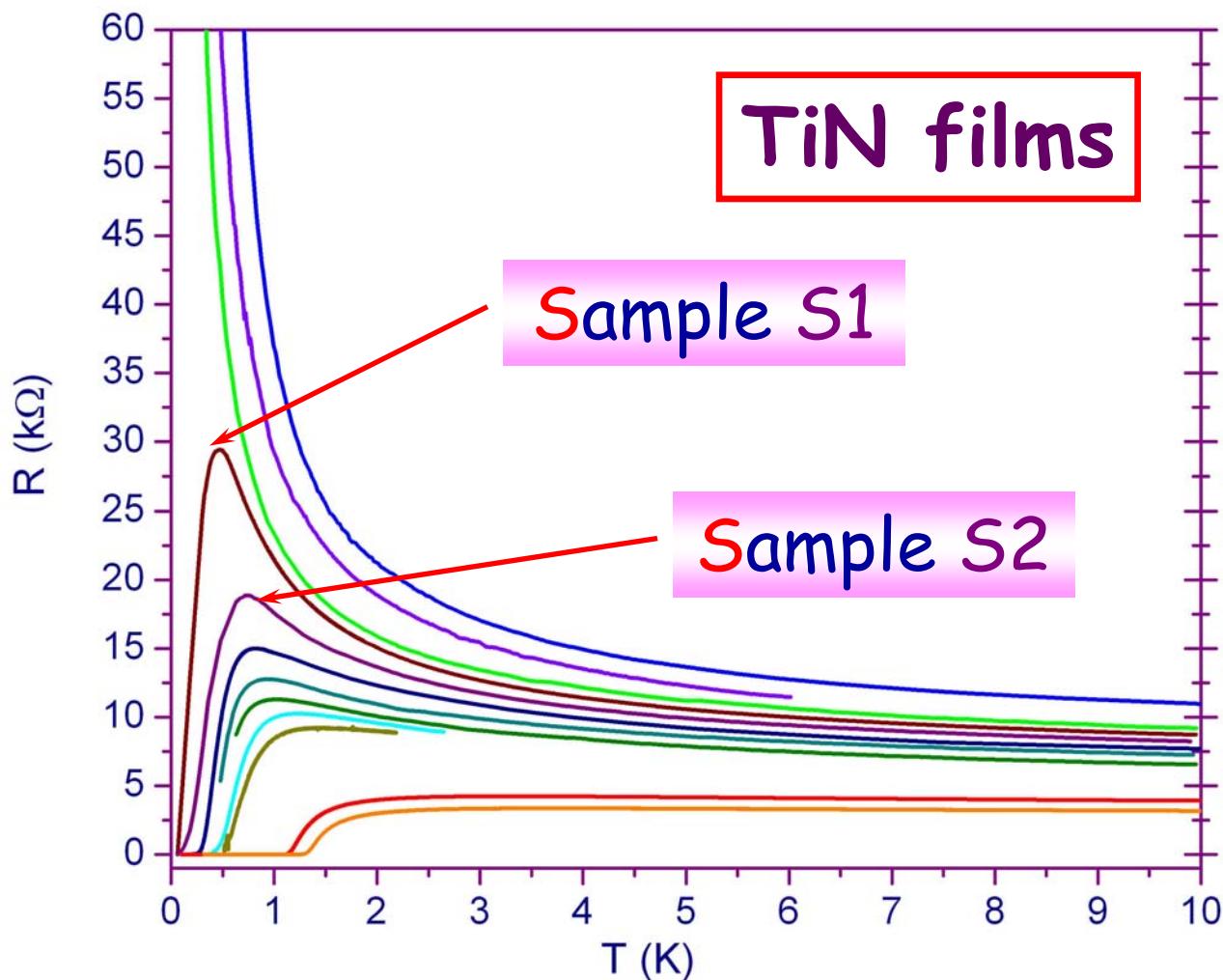
schematic phase diagram



T.I. Baturina, D.R. Islamov, J. Bentner, C. Strunk, M.R. Baklanov, and A. Satta,
JETP Lett. 79, 337 (2004).

T.I. Baturina, C. Strunk, M.R. Baklanov, A. Satta, PRL 98, 127003 (2007).

T.I. Baturina, A.Yu. Mironov, V.M. Vinokur, M.R. Baklanov, and C. Strunk,
cond-mat/0705.1602

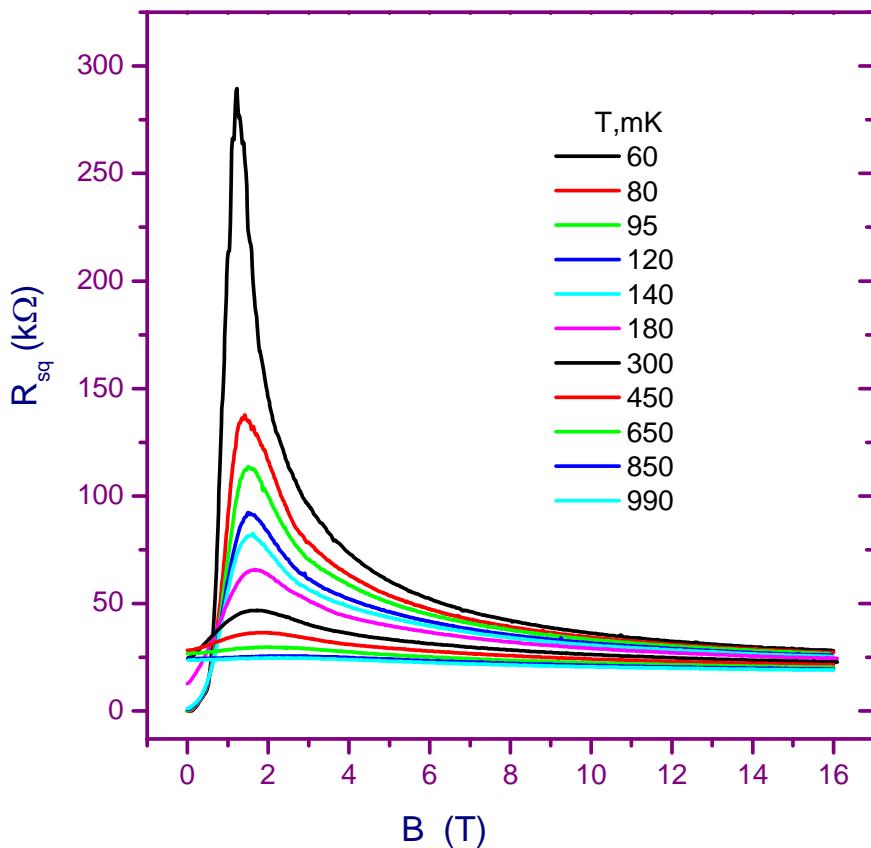


Experiment

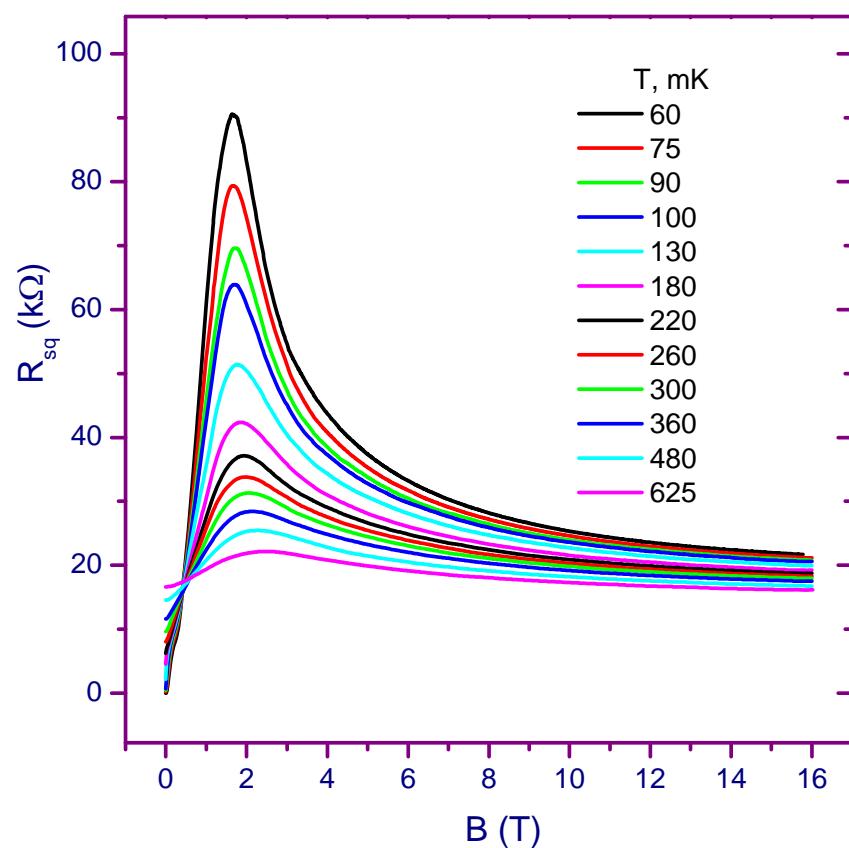
T. B., C. Strunk, M.R. Baklanov, A. Satta
PRL 98, 127003 (2007)

Magnetic-field-tuned
superconductor – insulator
quantum phase transition

Sample S1



Sample S2

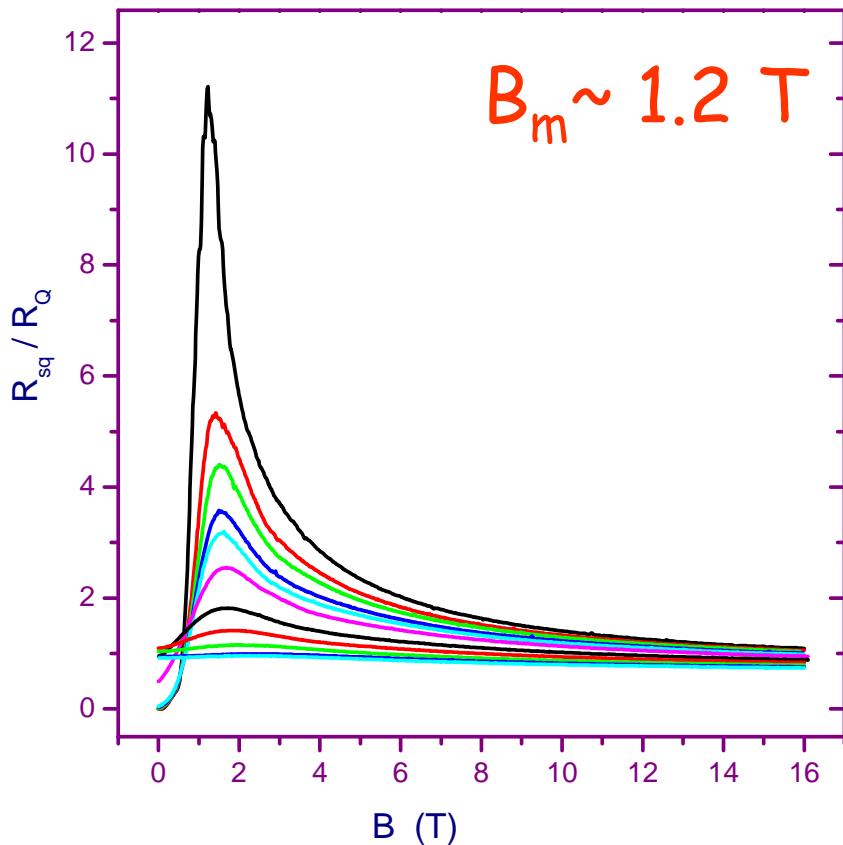


Experiment

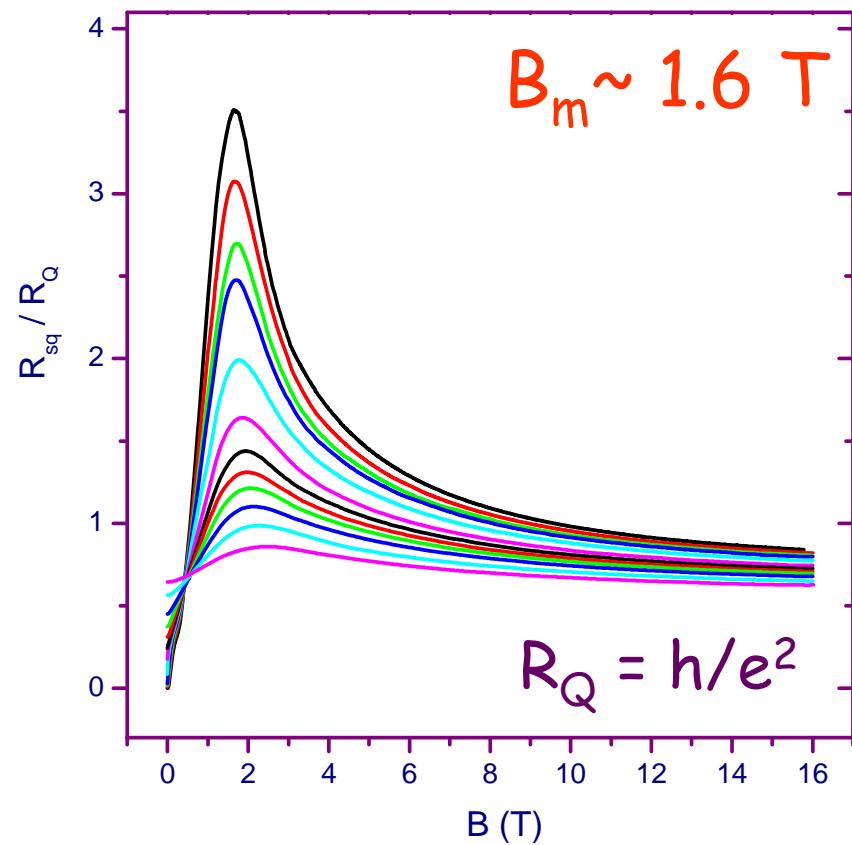
T. B., C. Strunk, M.R. Baklanov, A. Satta
PRL 98, 127003 (2007)

Magnetic-field-tuned
superconductor – insulator
quantum phase transition

Sample S1



Sample S2



The saturation occurs at a resistance

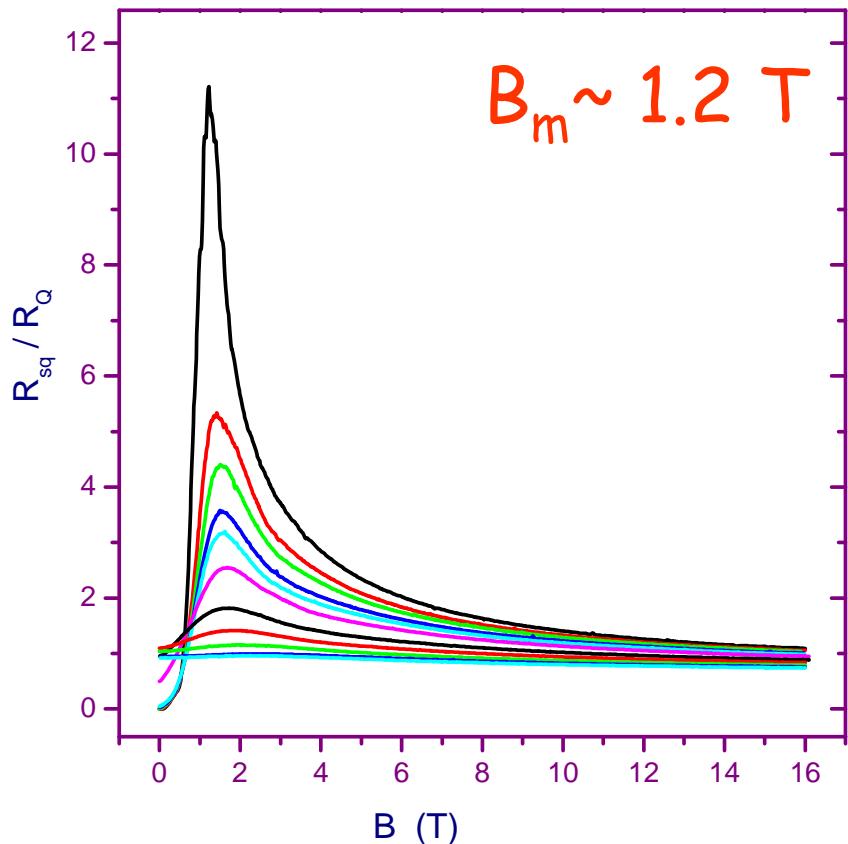
R_{sat}

near the quantum resistance

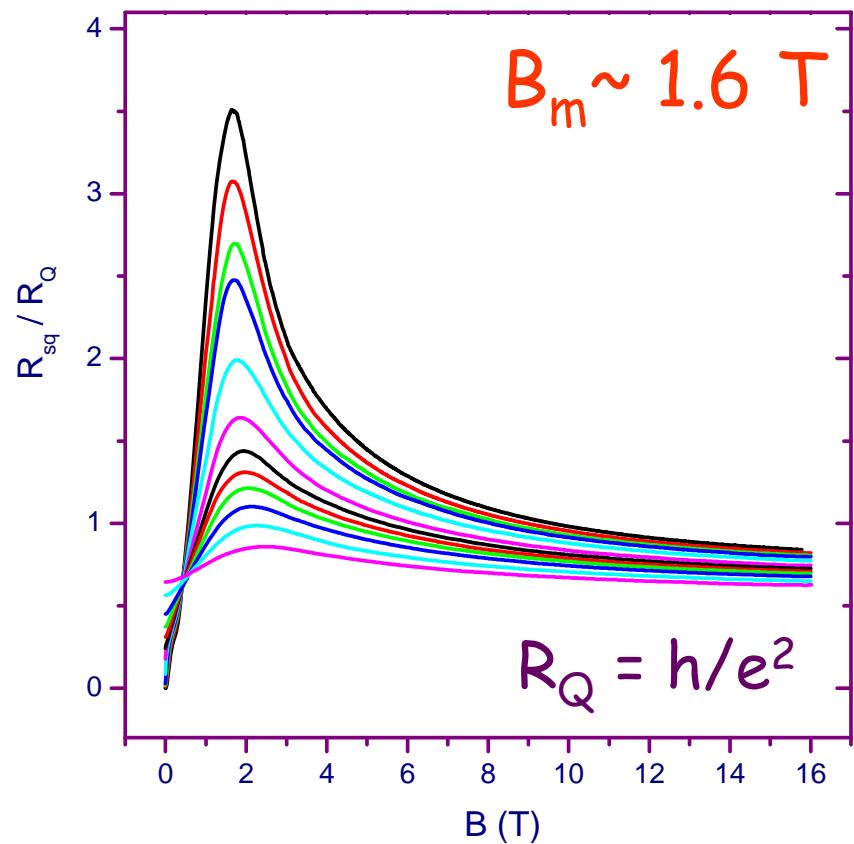
h/e^2

!!!

Sample S1



Sample S2



by varying the value of

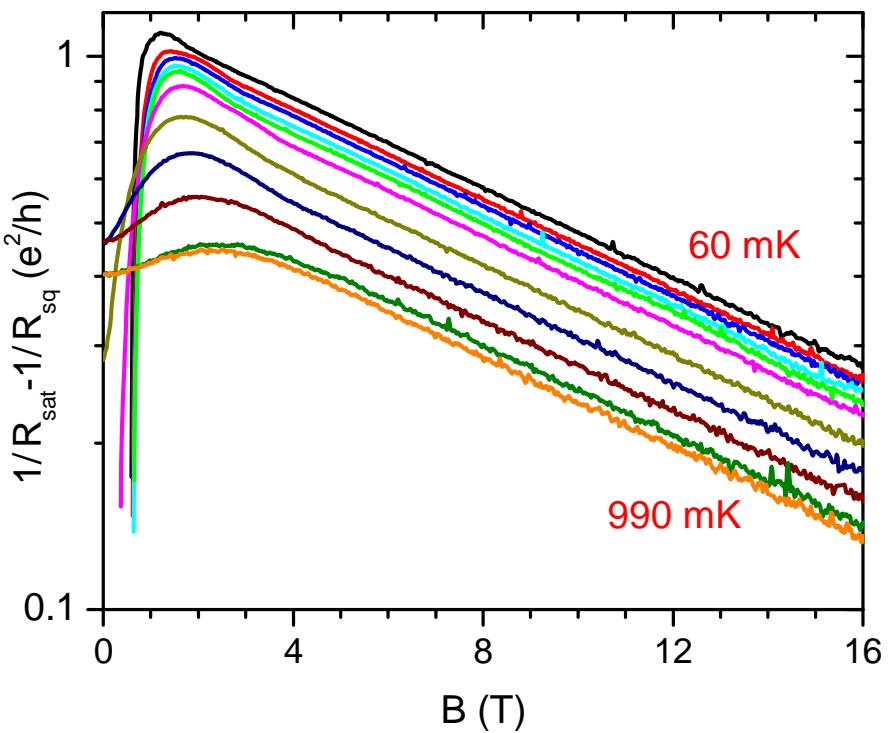
$$R_{\text{sat}}$$

for each curve , we can linearize

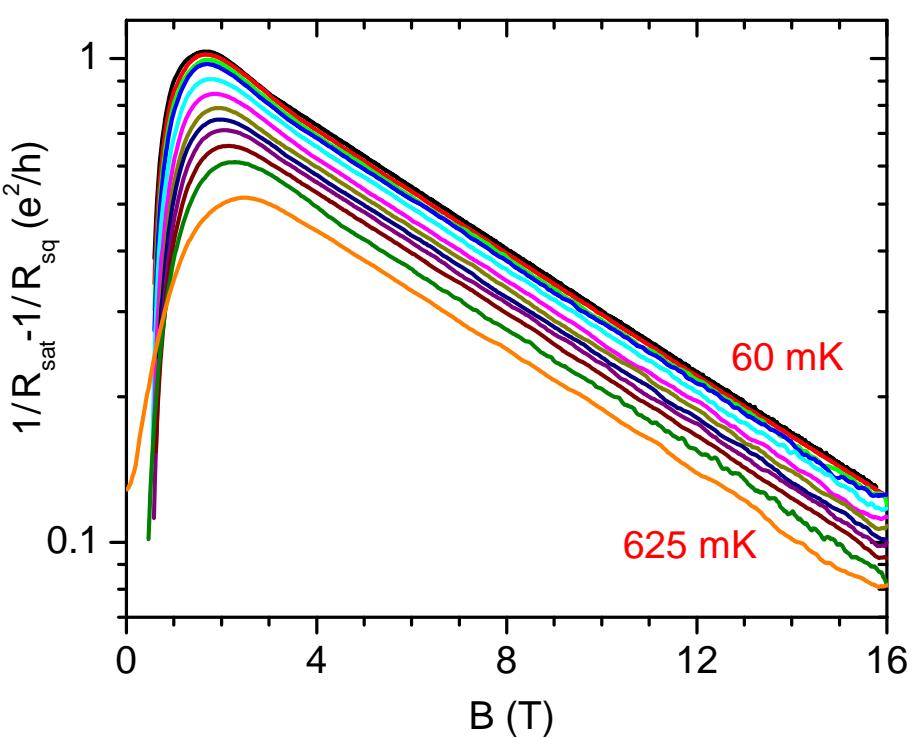
$$\ln(1/R_{\text{sat}} - 1/R_{\text{sq}}(B)) \text{ vs. } B$$

over a large range of B
with T-independent slope !!!

Sample S1



Sample S2



by varying the value of R_{sat} for each curve , we can linearize

$$\ln(1/R_{\text{sat}} - 1/R_{\text{sq}}(B)) \text{ vs. } B$$

over a large range of B
with T-independent slope !!!

$$G_{\text{sq}}(T, B) [=1/R_{\text{sq}}(T, B)] = 1/R_{\text{sat}}(T) - \beta(T) \exp(-B/B^*)$$

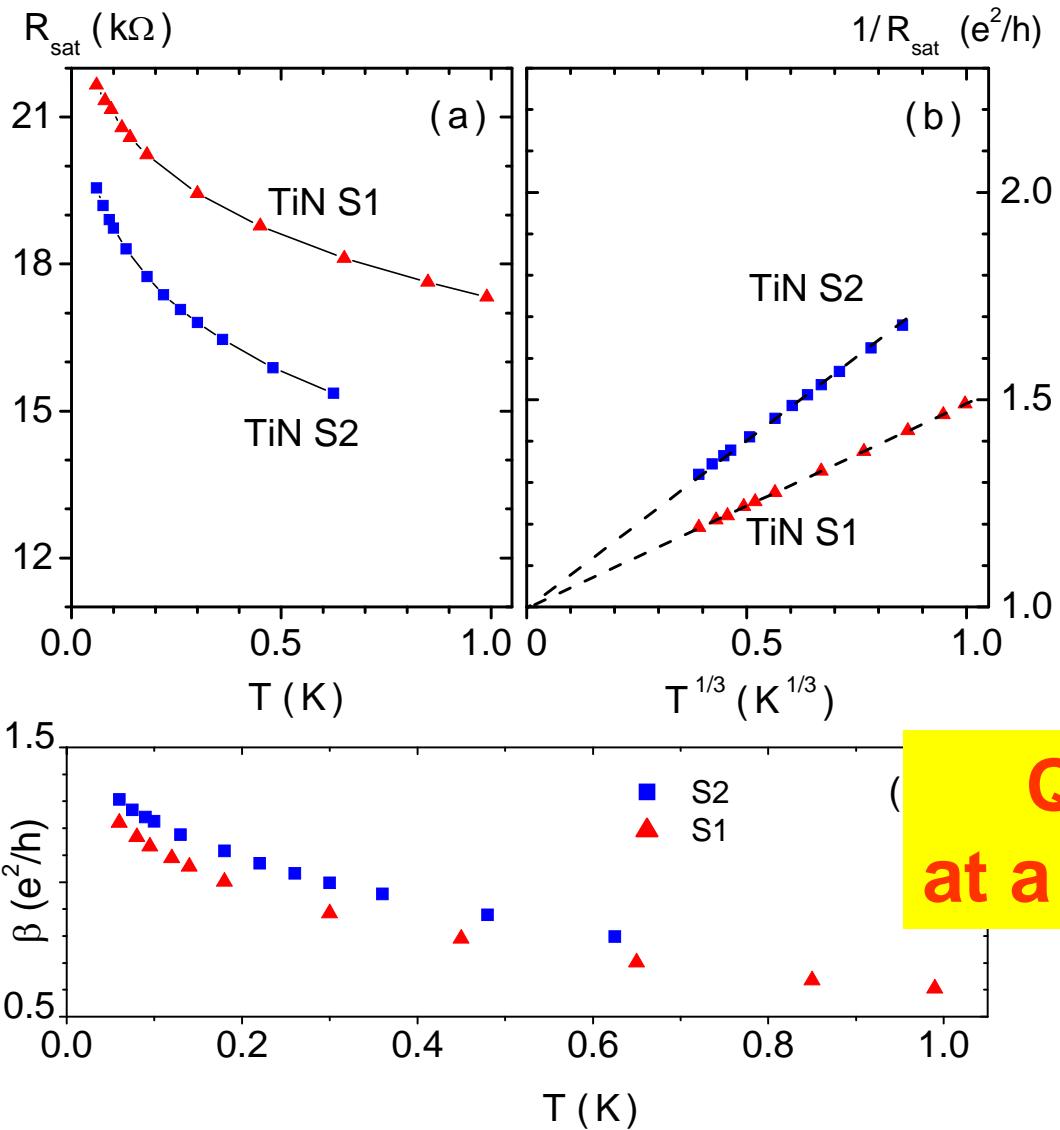
Sample S1

$$B^* = 10.7 \text{ T}$$

Sample S2

$$B^* = 6.8 \text{ T}$$

$$G_{sq}(T,B) [=1/R_{sq}(T,B)] = 1/R_{sat}(T) - \beta(T) \exp(-B/B^*)$$



$R_{sat}(T \rightarrow 0) \rightarrow h/e^2$

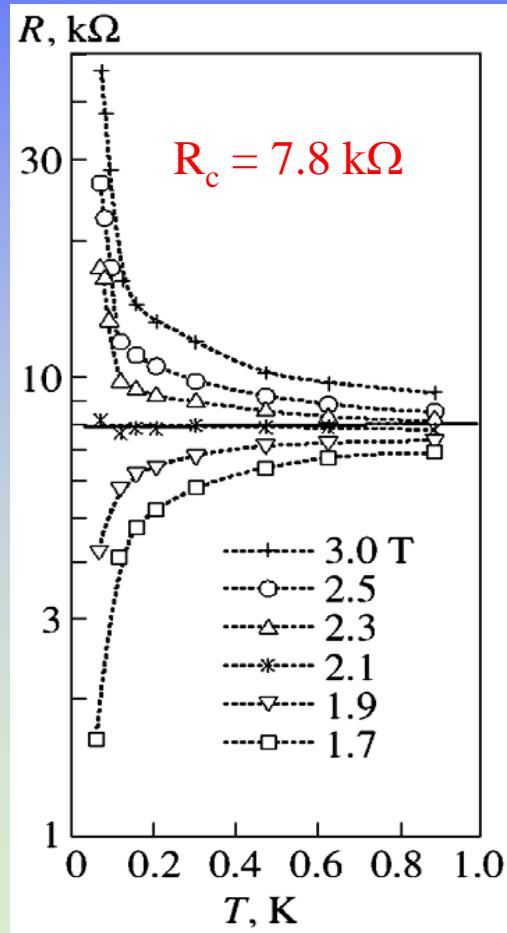
Quantum metallicity
at a high-field side of SIT

Field-induced superconductor – insulator transition

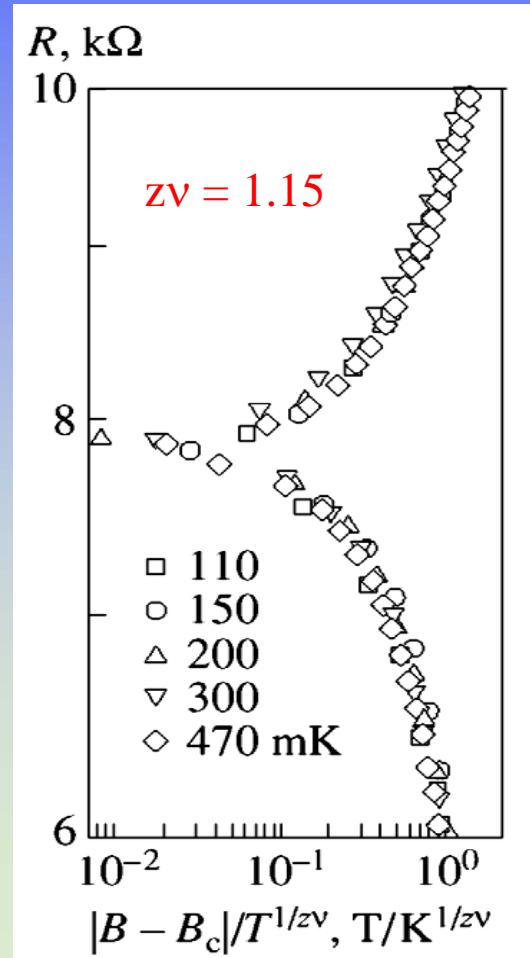
V. F. Gantmakher, M. V. Golubkov, V. T. Dolgopolov, A. A. Shashkin, G. E. Tsydynzhapov,
JETP Lett. 71, 160 (2000); 71, 473 (2000)

$a\text{-InO}_x$

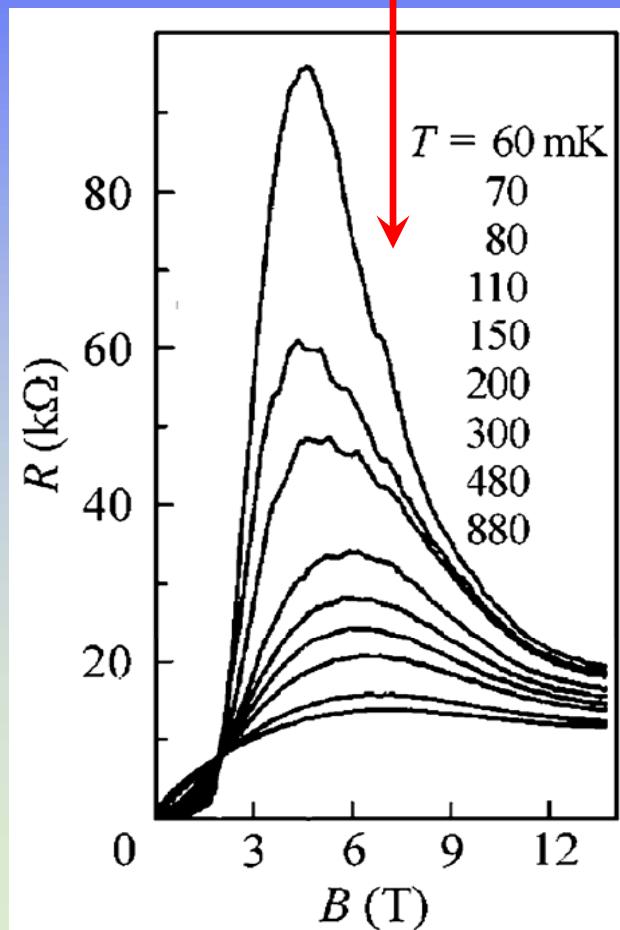
Fan-shaped curves

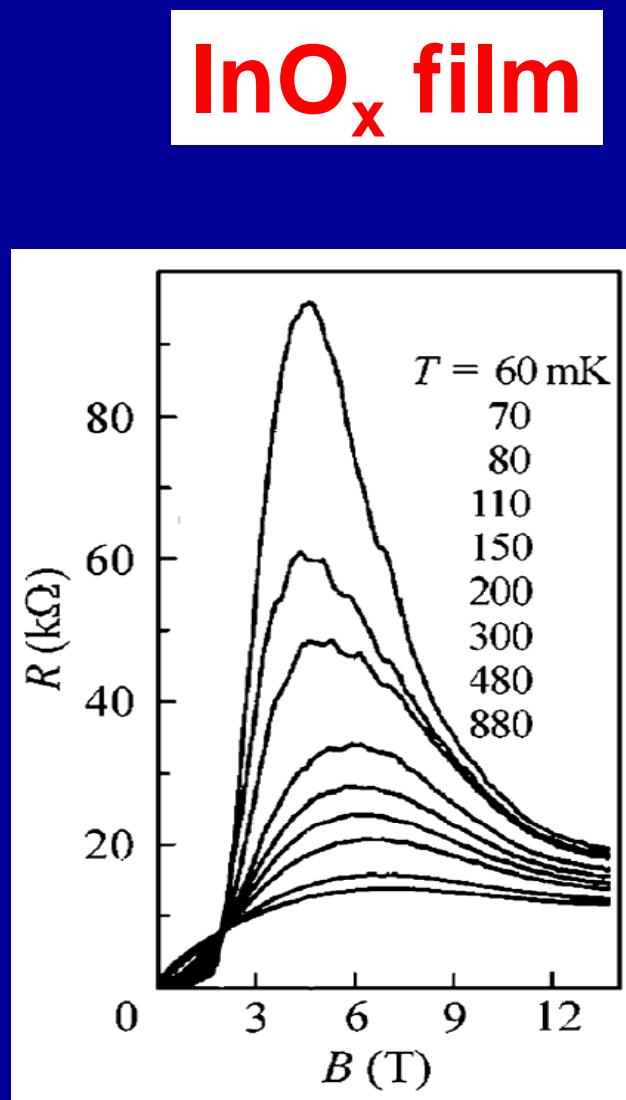
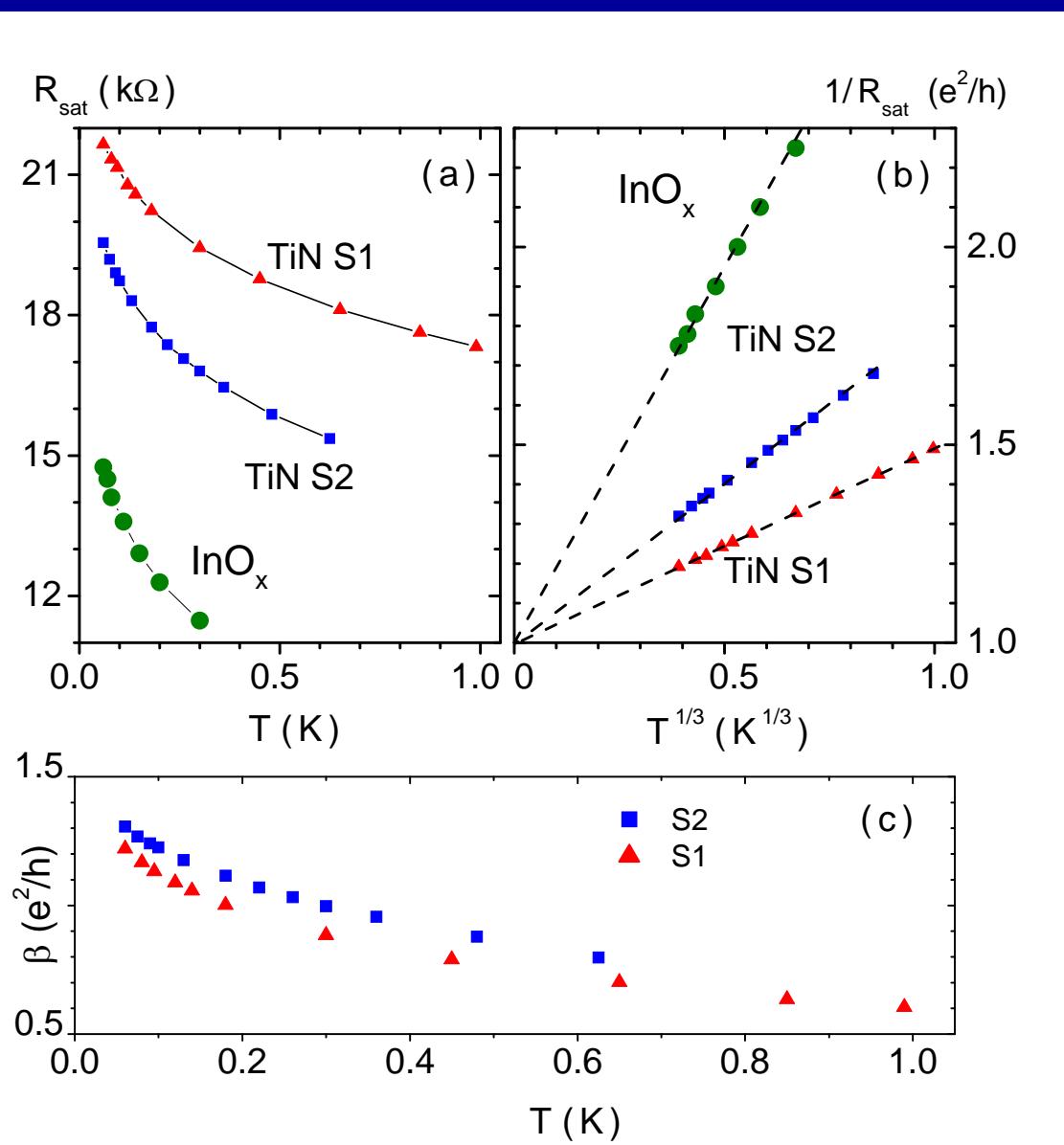


Scaling



Negative magnetoresistance





Quantum metallicity in a two-dimensional insulator

Nature 409, 161 (2001)

V. Yu. Butko^{*†} & P. W. Adams^{*}

Be films

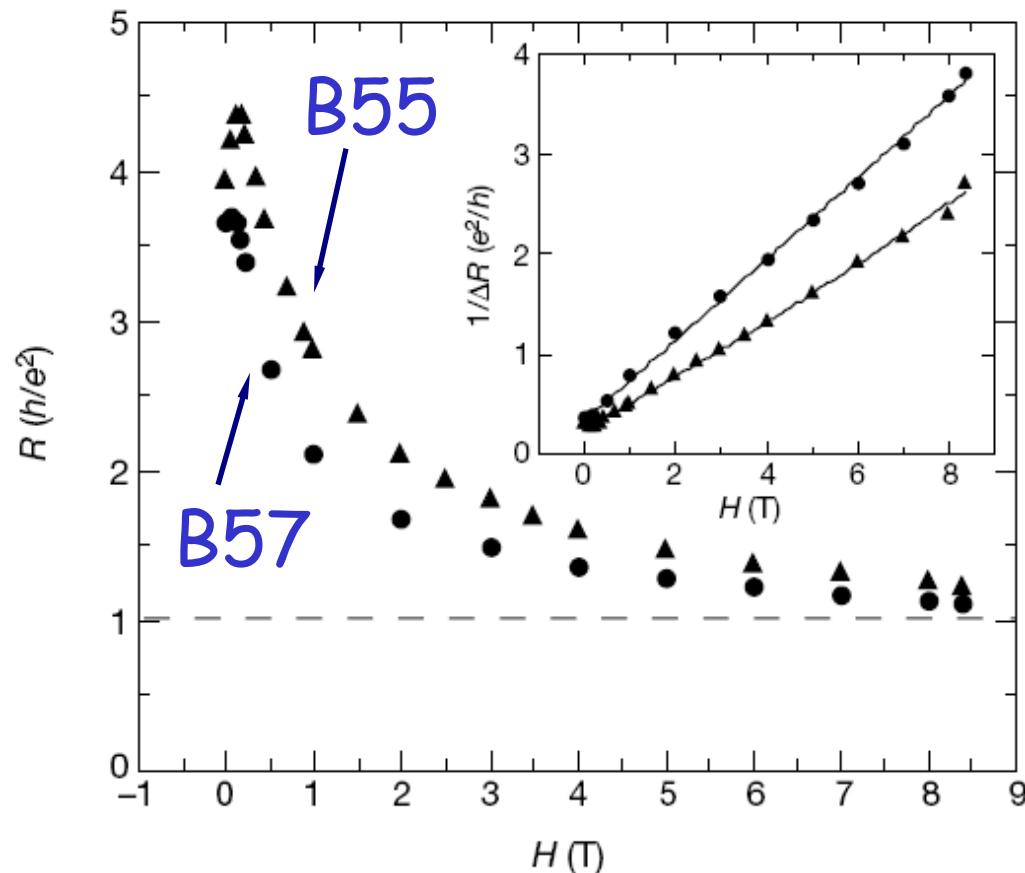


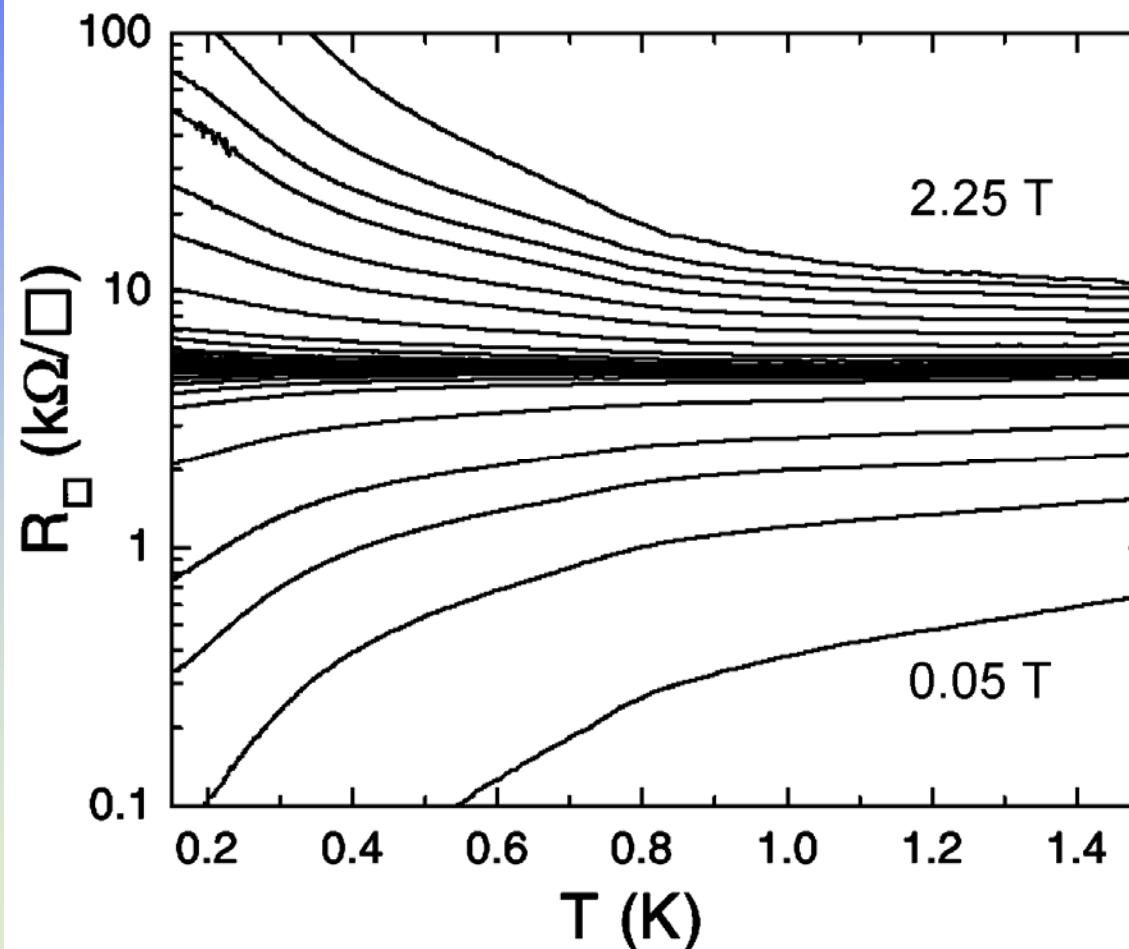
Figure 2 Low-temperature magnetoresistance. The figure shows the resistance in units of h/e^2 as a function of magnetic field H at $T = 40 \text{ mK}$, for samples B57 (circles) and B55 (triangles). We note the saturation at $R \approx h/e^2$. Inset, linear behaviour after subtracting a saturation resistance of $0.85 \text{ } h/e^2$, $\Delta R = R - 0.85$. The solid lines are guides to the eye.

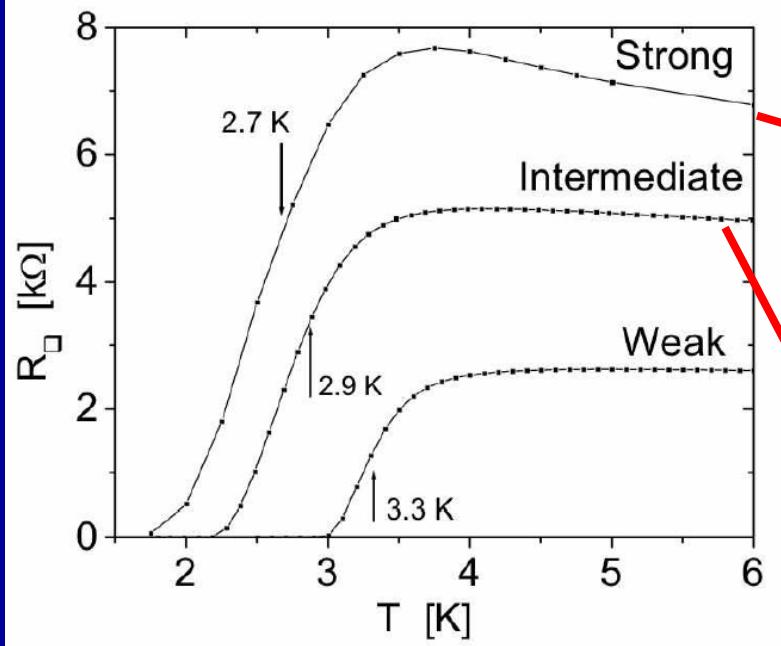
Field-induced superconductor – insulator transition

E. Bielejec and Wenhao Wu, PRL 88, 206802 (2002)

Be films

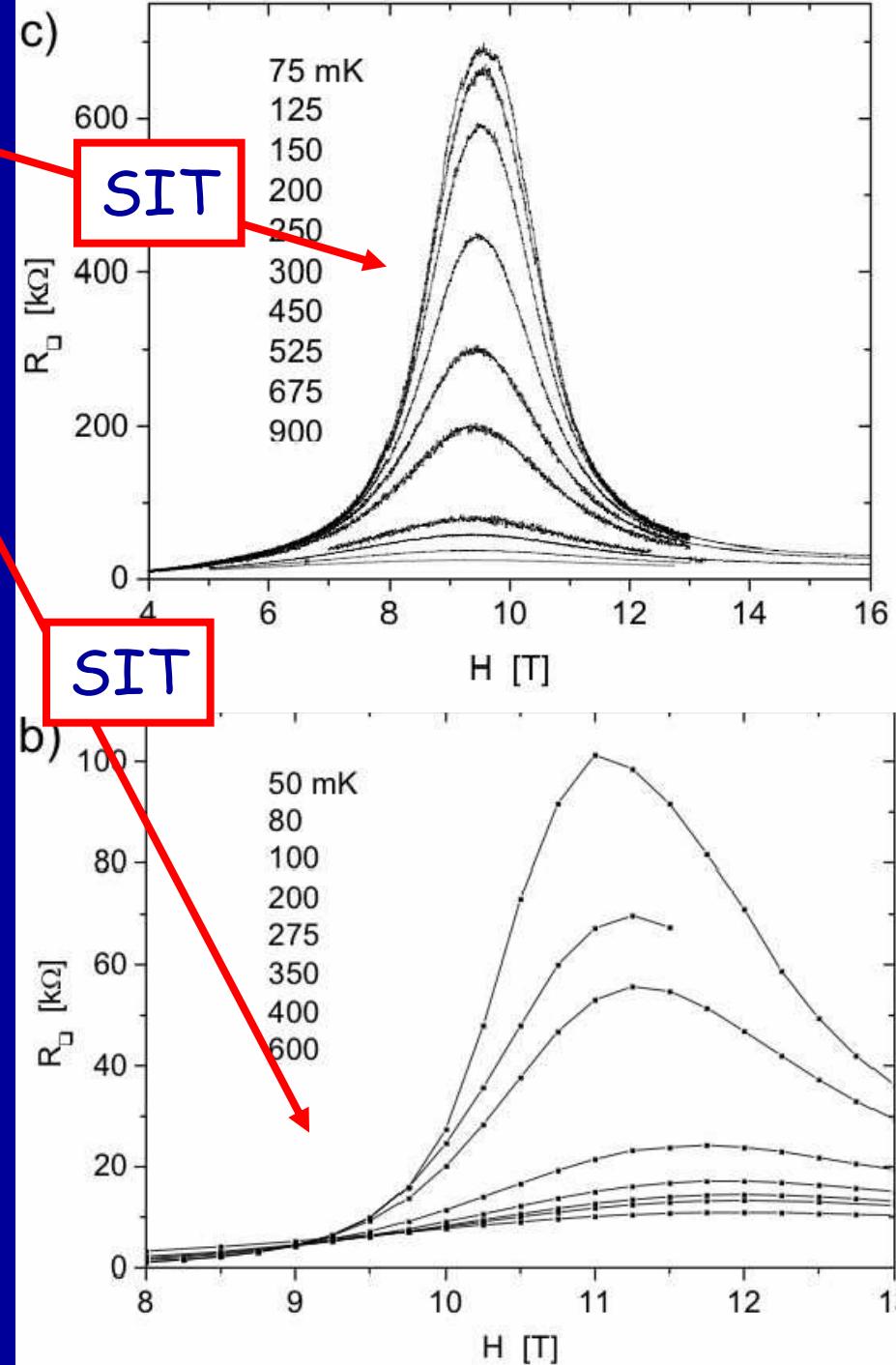
Fan-shaped curves

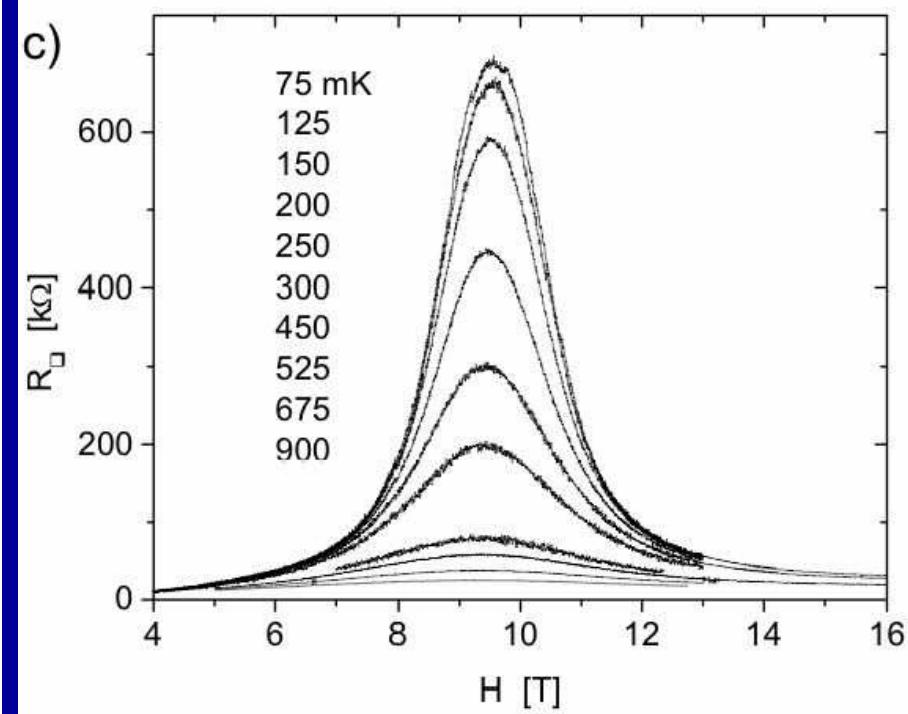
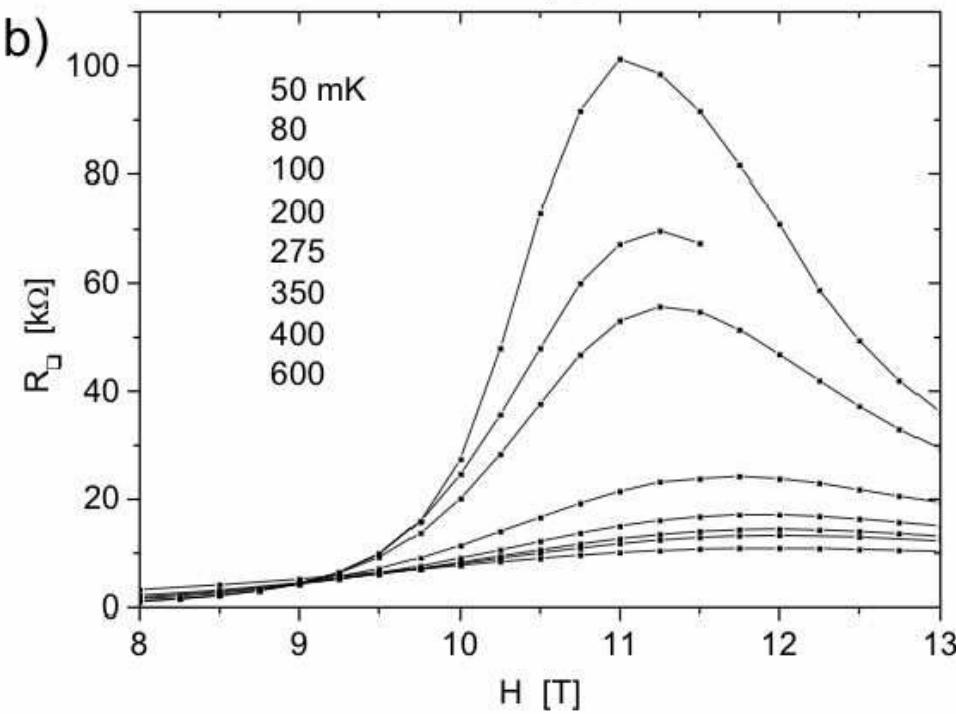




InO_x films

M. Steiner and A. Kapitulnik,
Physica C 422, 16 (2005)

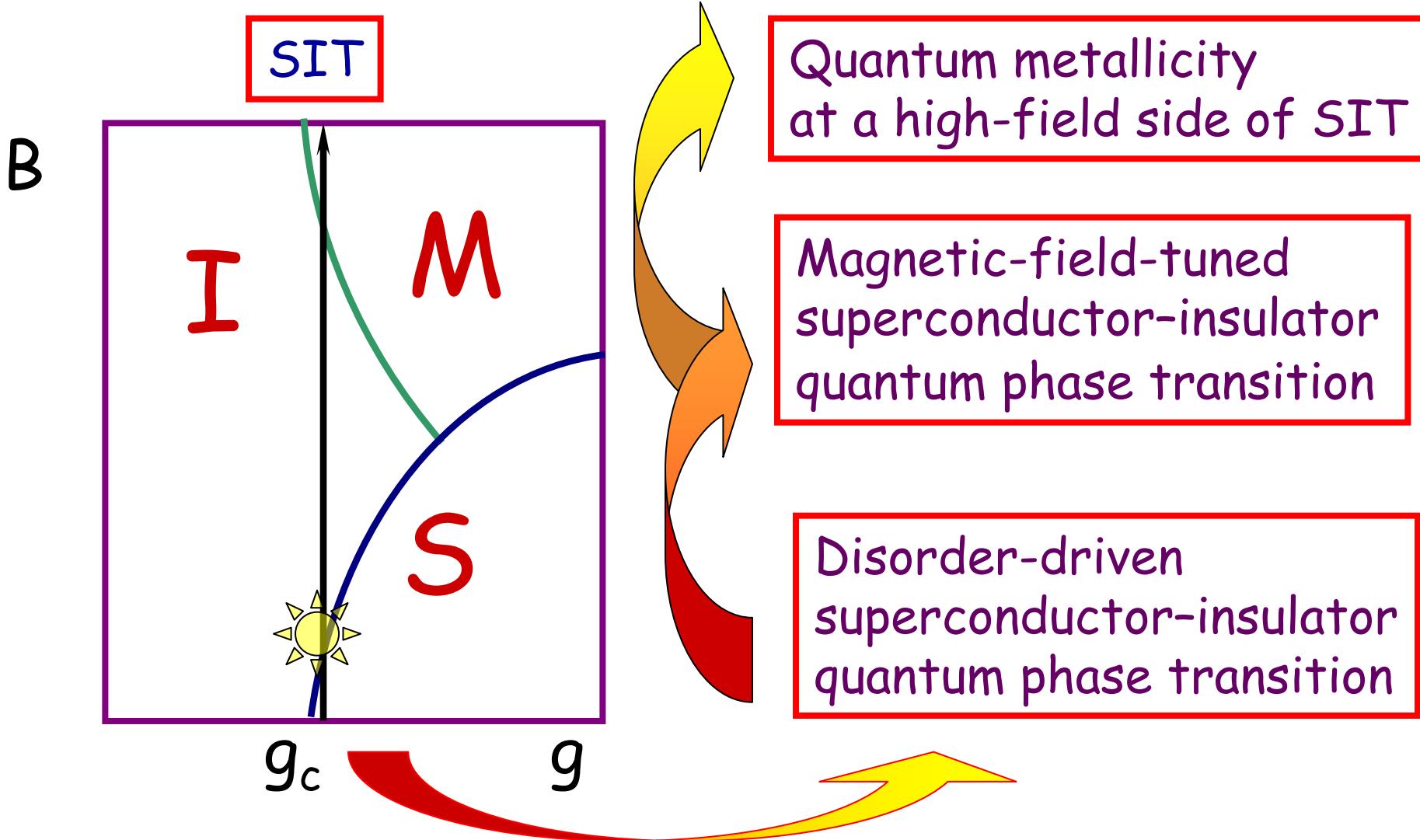




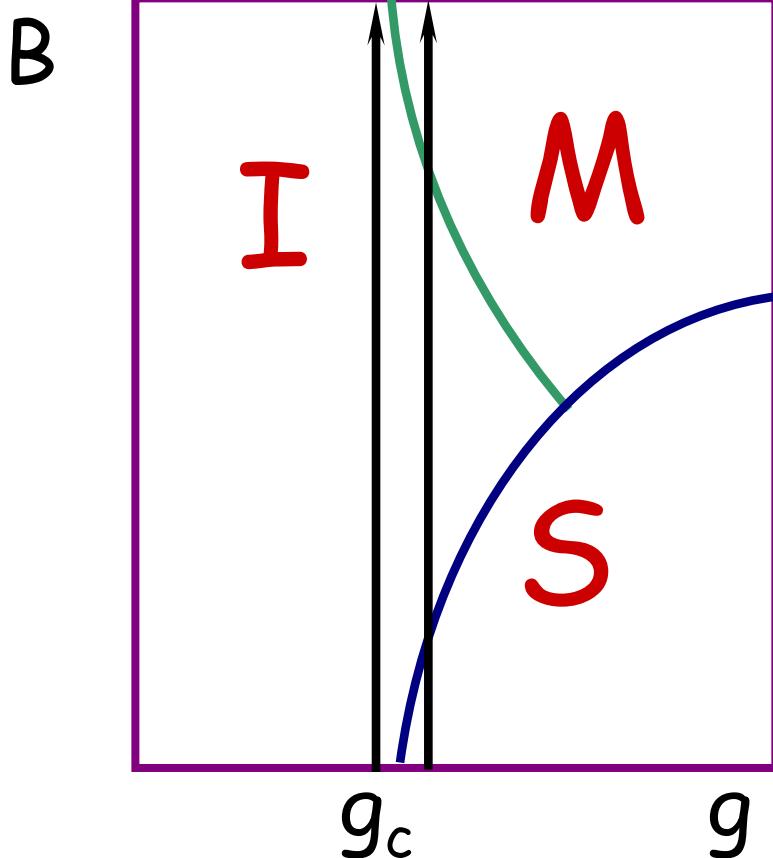
The insulating state above the crossing point becomes even more dramatic in the films with higher R_n . At low temperature and moderately high field these films reveal a new, extremely strong tendency towards the insulating phase, shown in Figures 4b and 4c. The resistance at the crossing point of both plots is comparable to that of the first film. We note, however, that the position of the crossing point shifts to lower field as the insulator strength increases. On the high field side of the peak the isotherms all decay to resistances ≤ 20 $k\Omega/\square$, above the normal resistance R_n , at the highest accessible fields.

schematic phase diagram

InO_x, Be, and TiN films



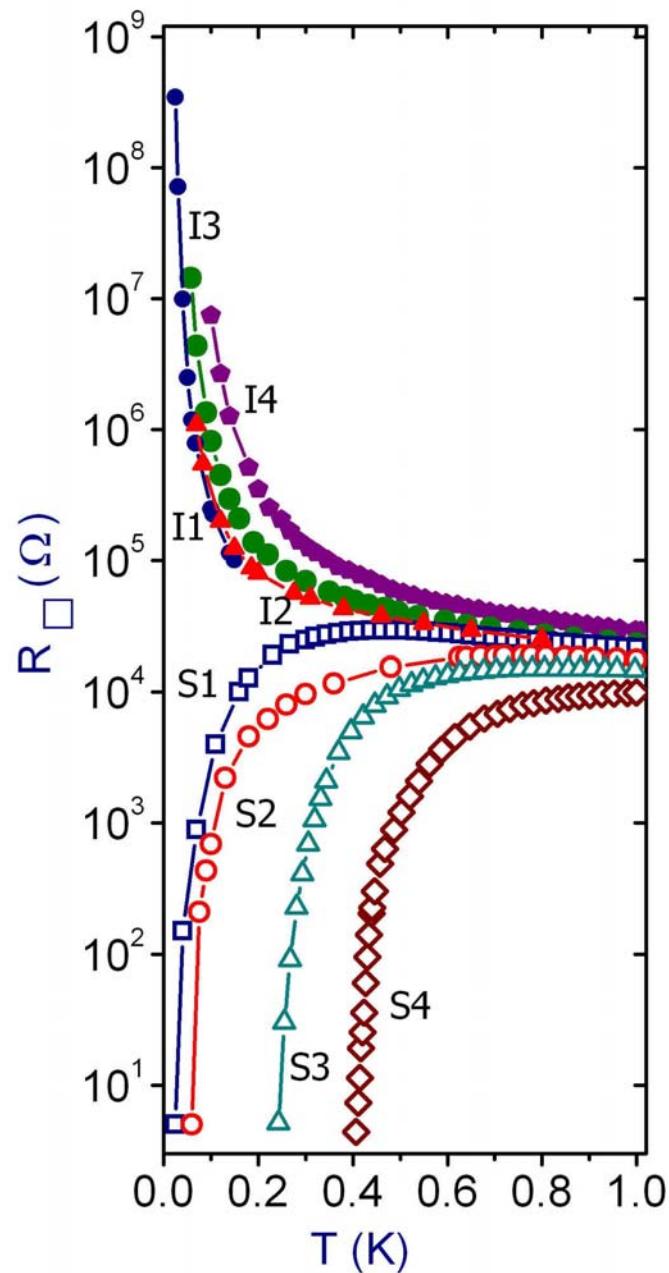
schematic phase diagram



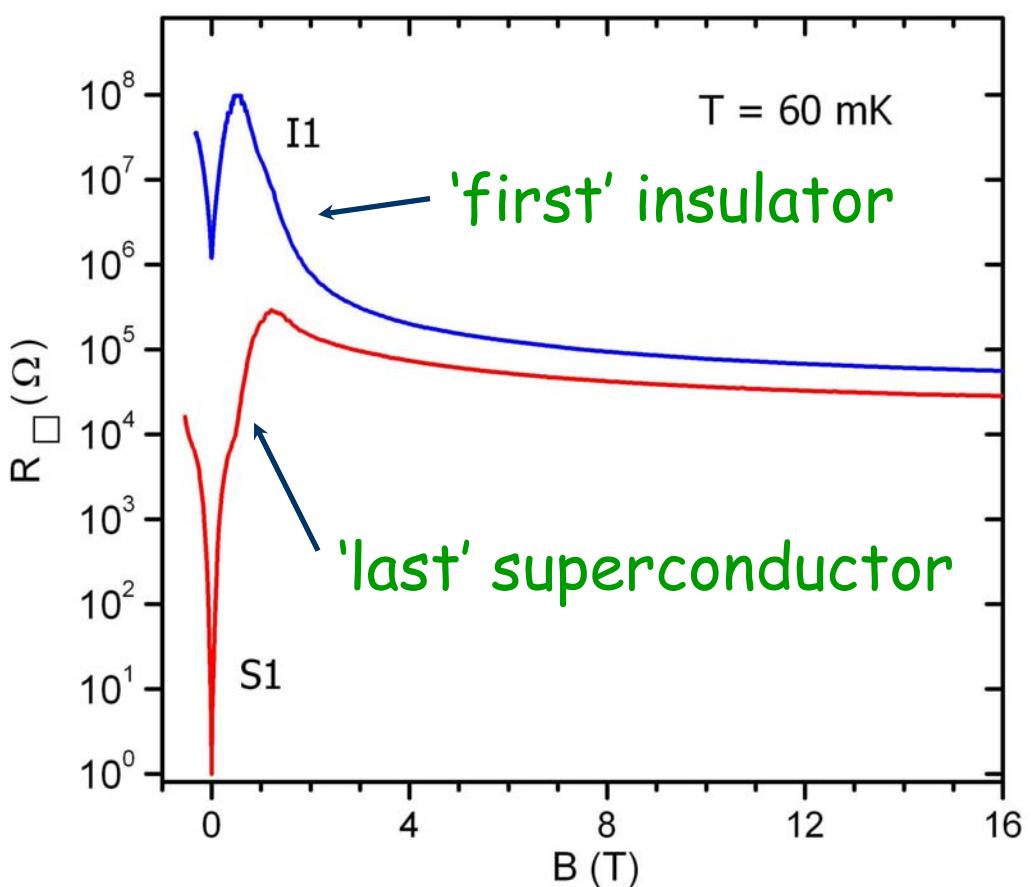
Critical Region of the Disorder-Driven
Superconductor-Insulator
quantum phase transition

T.I. Baturina et al., cond-mat/0705.1602

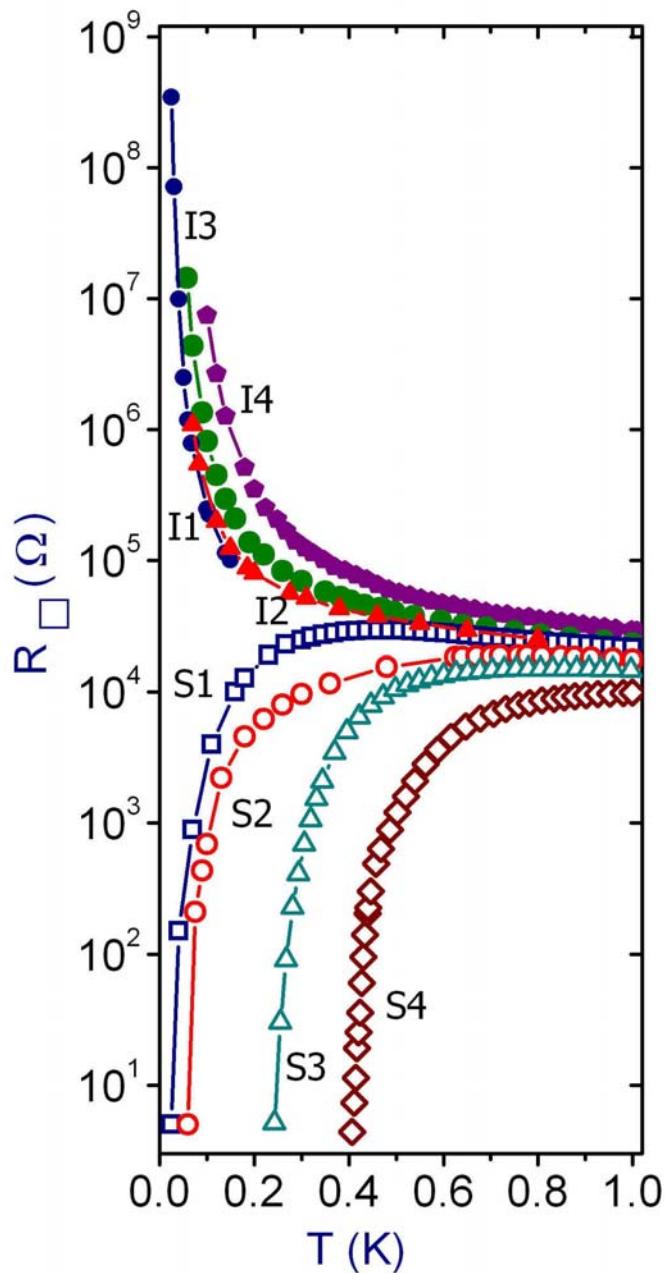
T.I. Baturina et al., Physica C, in press



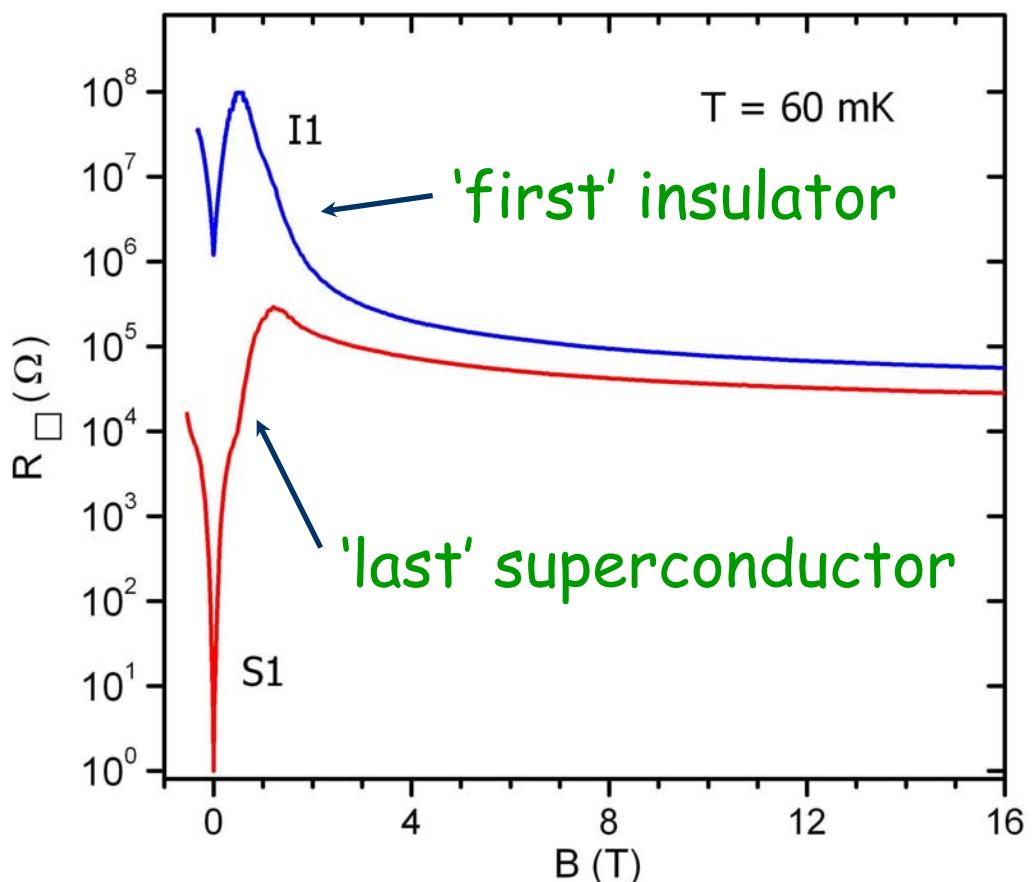
TiN films



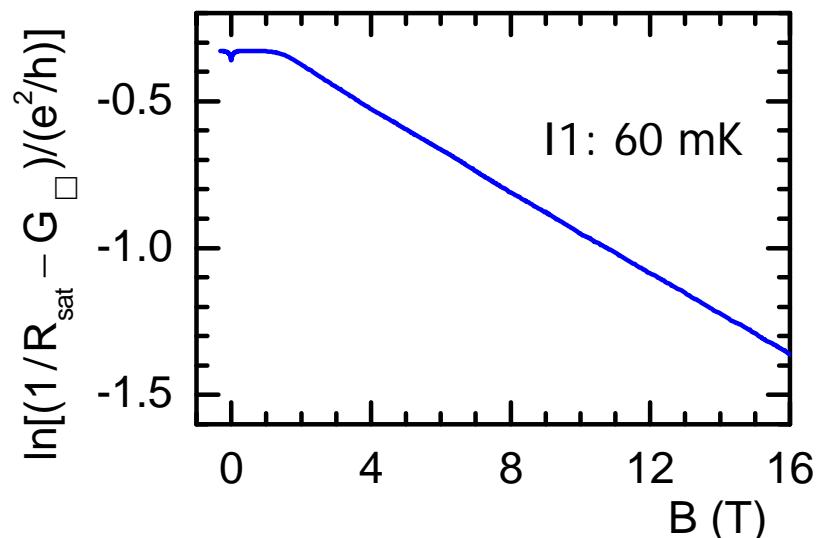
In all samples, including the insulating films, $R(B)$ varies nonmonotonically with B , starting a positive magnetoresistance (PMR) at low fields, then reaching a maximum, followed first by a rapid drop and eventually saturating at higher magnetic fields



Magnetoresistance



Behavior in high magnetic field

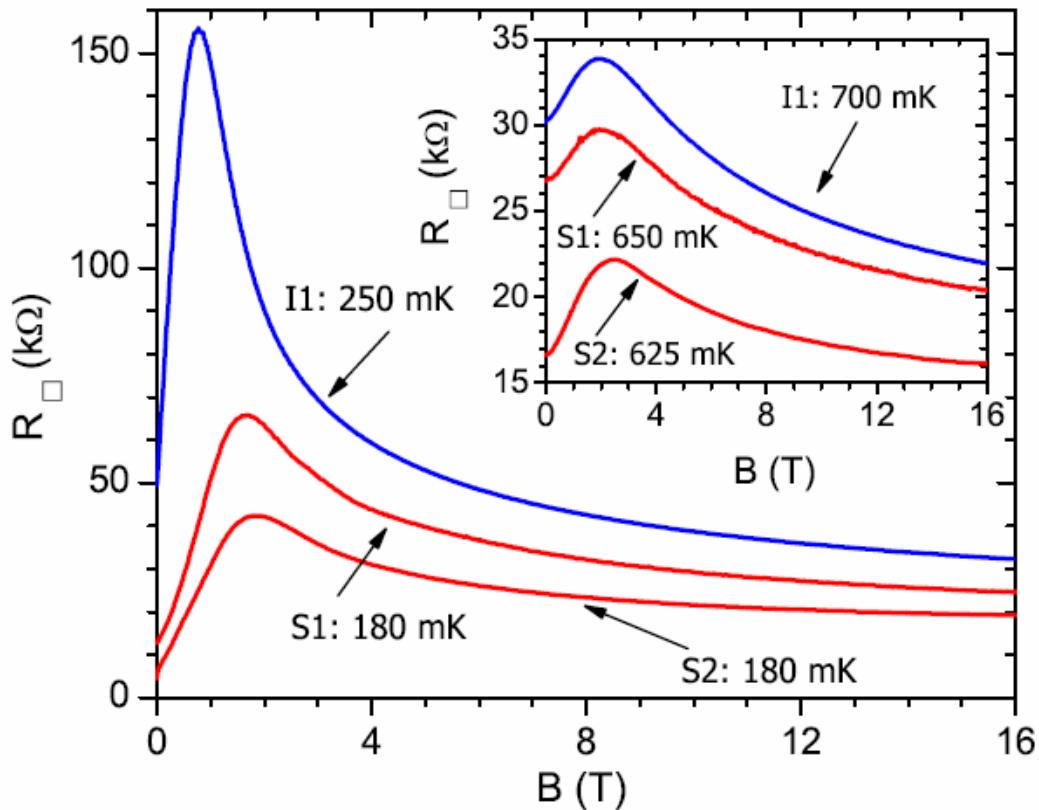


$$\ln\left(\frac{1}{R_{\text{sat}}} - \frac{1}{R_{\text{sq}}(B)}\right) \text{ vs. } B$$

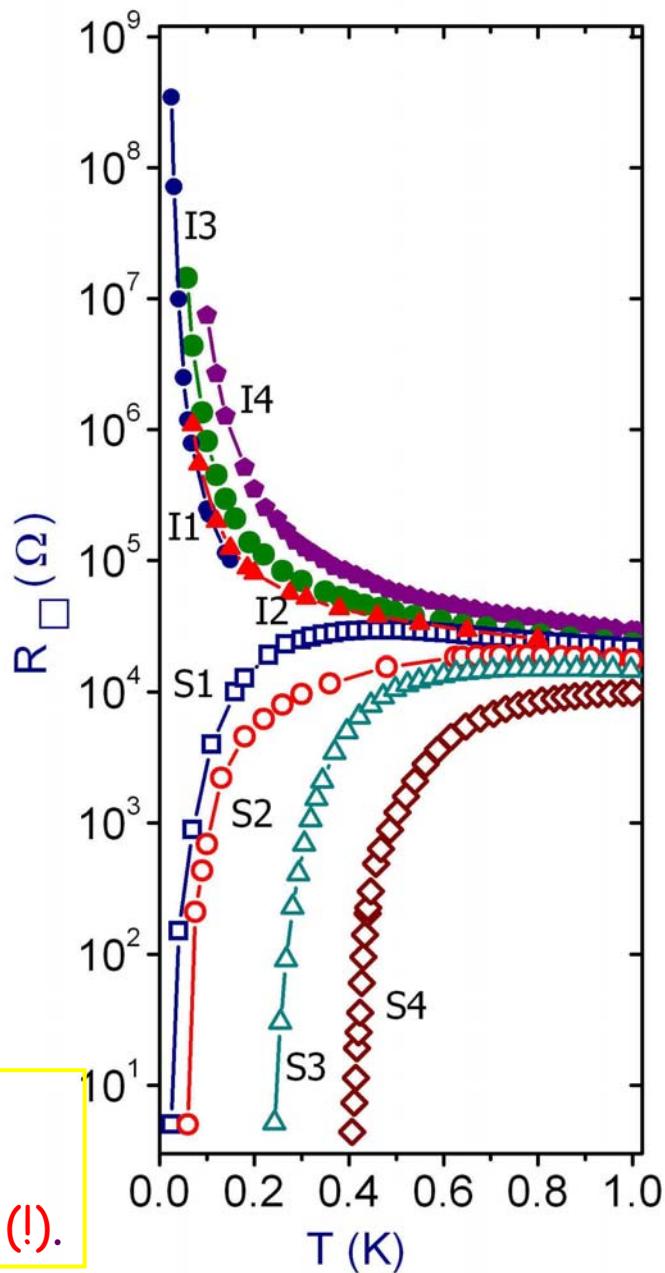
TiN films

Magnetoresistance

While the difference between the insulating and superconducting samples is significant at the zero magnetic field and at low temperatures, it vanishes at higher magnetic fields and temperatures



Relying on the high temperature data only
it is impossible to predict whether the film turns
superconductor or insulator at lowest temperatures (!).



PMR and activated behavior

TiN films

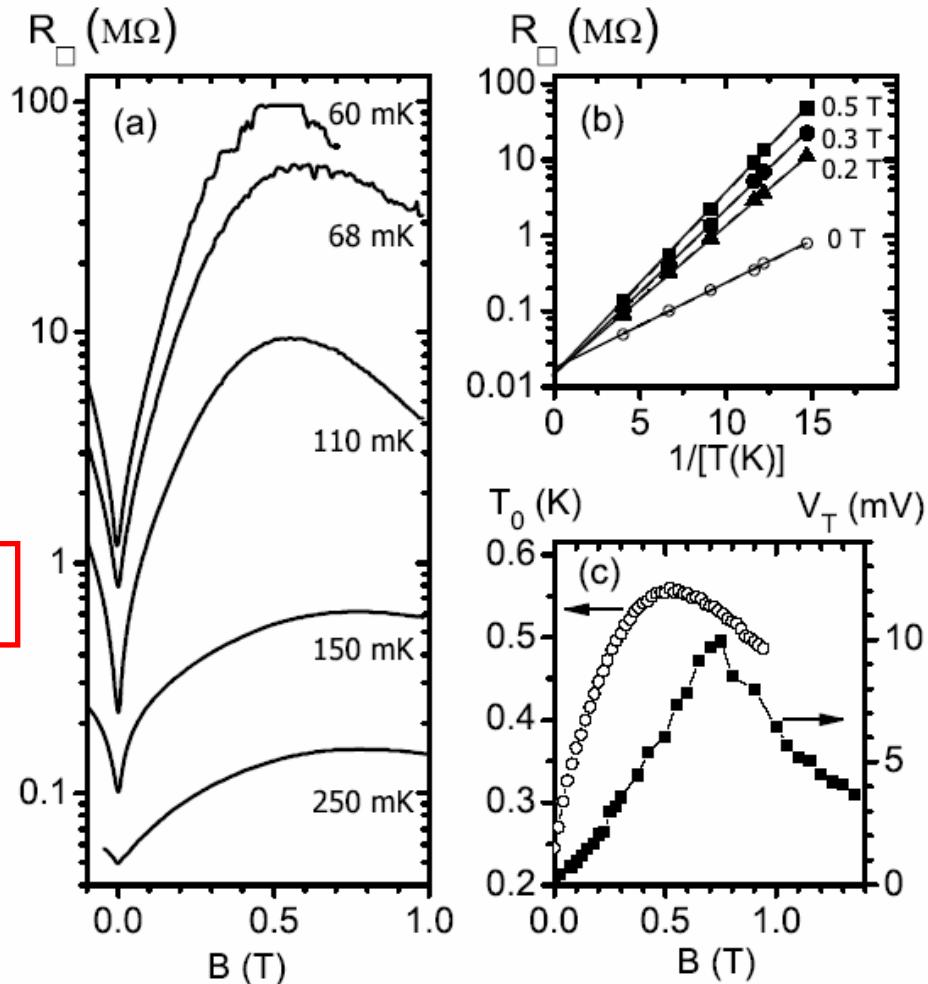
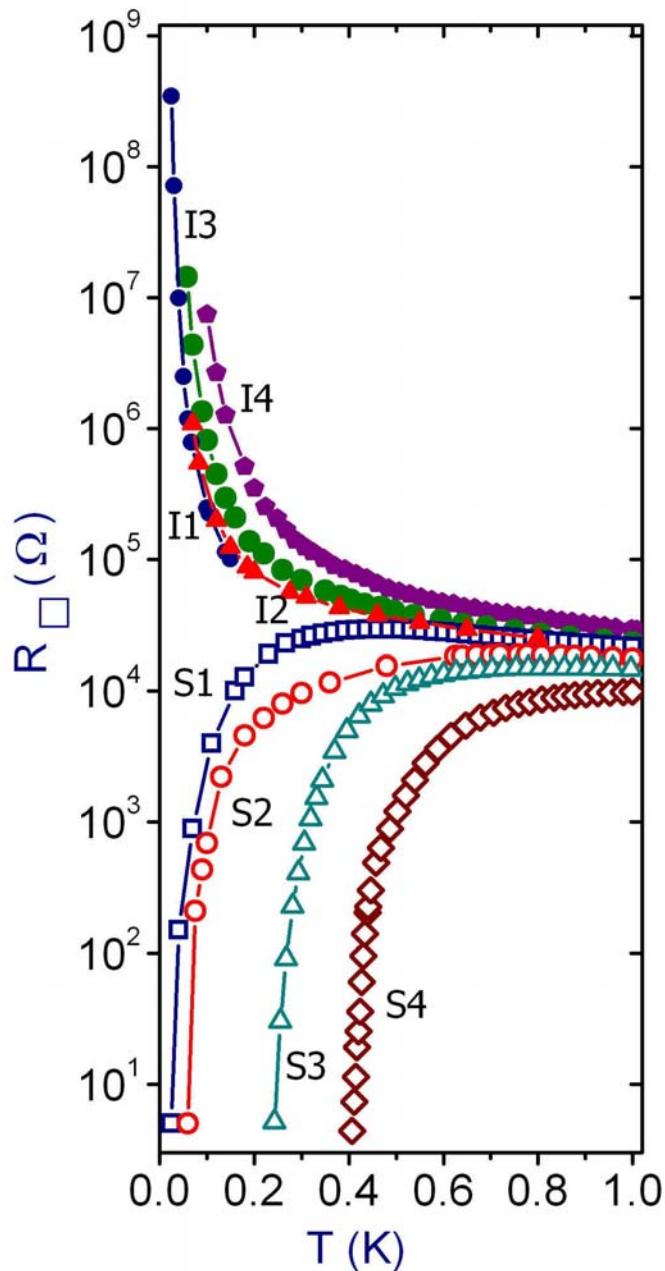
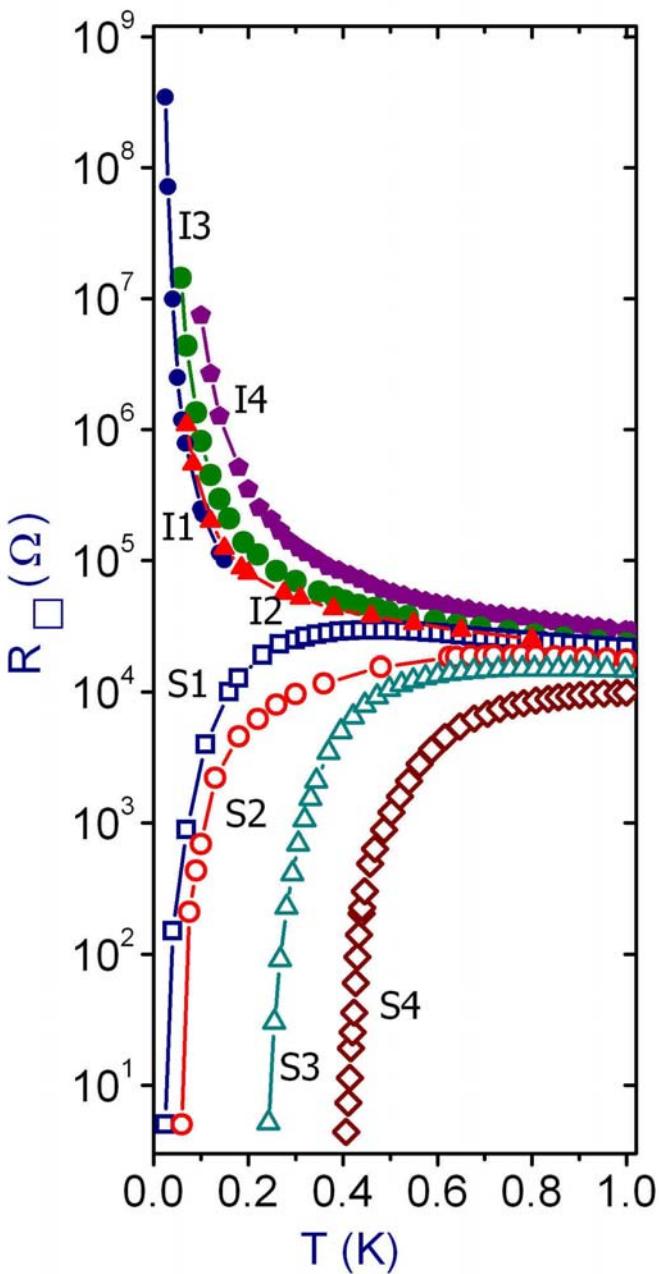
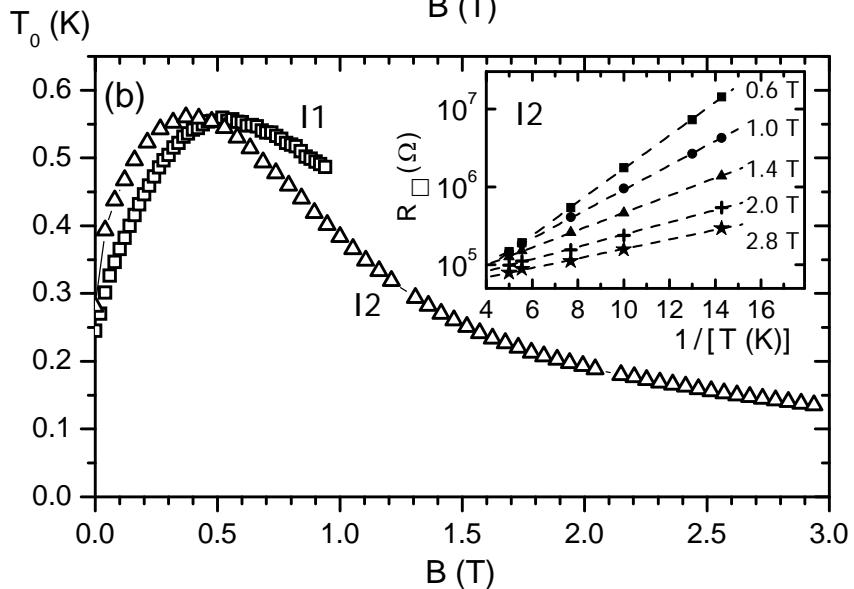
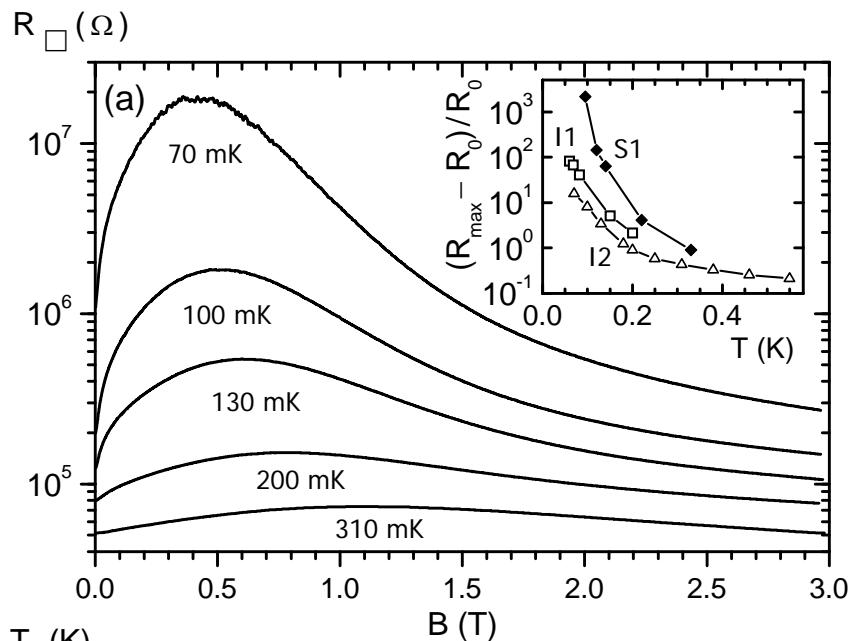


FIG. 3: (a) Sheet resistance of sample I1 as a function of the magnetic field at some temperatures listed. (b) R versus $1/T$ at $B = 0$ (open circles), 0.2 (triangles), 0.3 (filled circles), and 0.5 T (squares). The dashed lines are given by Eq. (1). (c) T_0 (left axis), calculated from fits to Eq. (1), and the threshold voltage V_T (right axis) as a function of B .



PMR and activated behavior

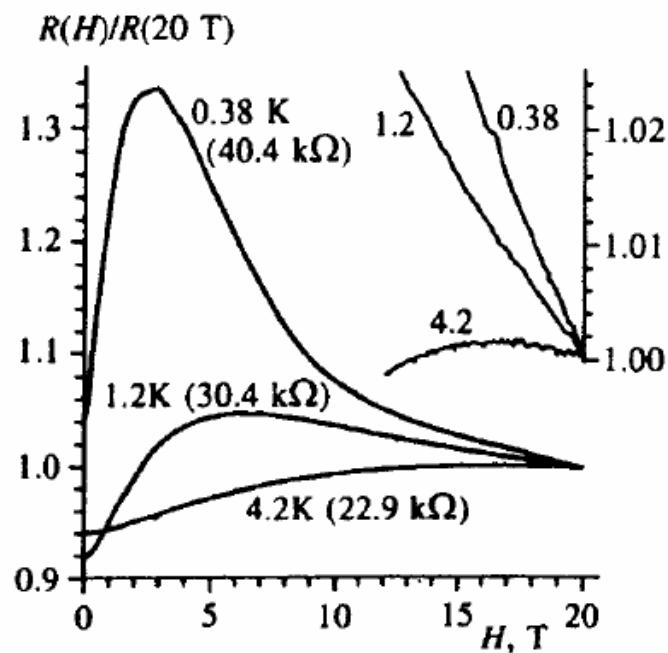
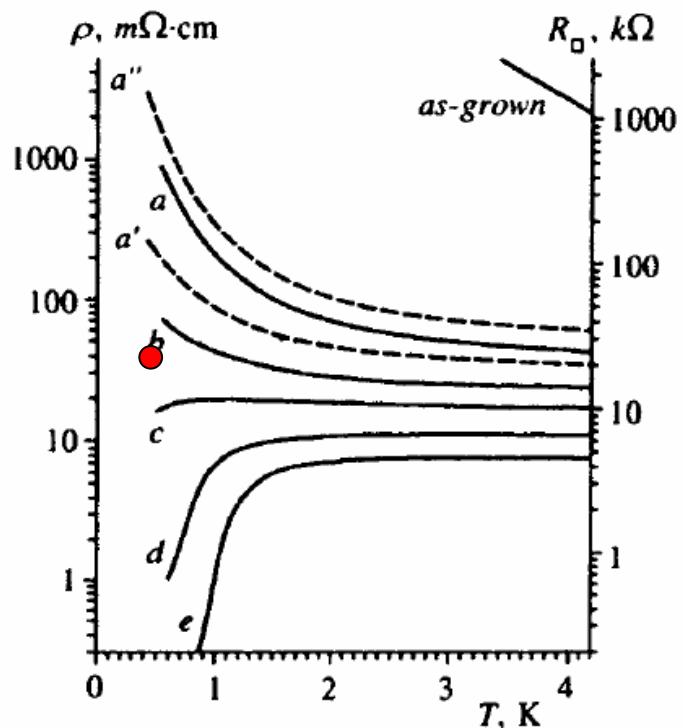
TiN films



Magnetoresistance

InO_x films

V.F. Gantmakher *et al.*,
JETP 82, 951 (1996).



Field dependence $R(H)$ normalized to $R(20 \text{ T})$ at three different temperatures. Inset: high-field part of the curves at ten times the vertical scale. Film No. 3, state b .

FIG. 2. Evolution of the temperature dependence of the resistance of α -In₂O_x films in zero magnetic field after different treatments. Film No. 1: states a (initial)— e , film No. 2: states a' (initial) and a'' . A part of the dependence $R(T)$ for the as-grown film from the inset of Fig. 1 is also plotted.

Magnetoresistance

Be films

E. Bielejec, J. Ruan, and W. Wu,
PRB 63, 100502(R) (2001).

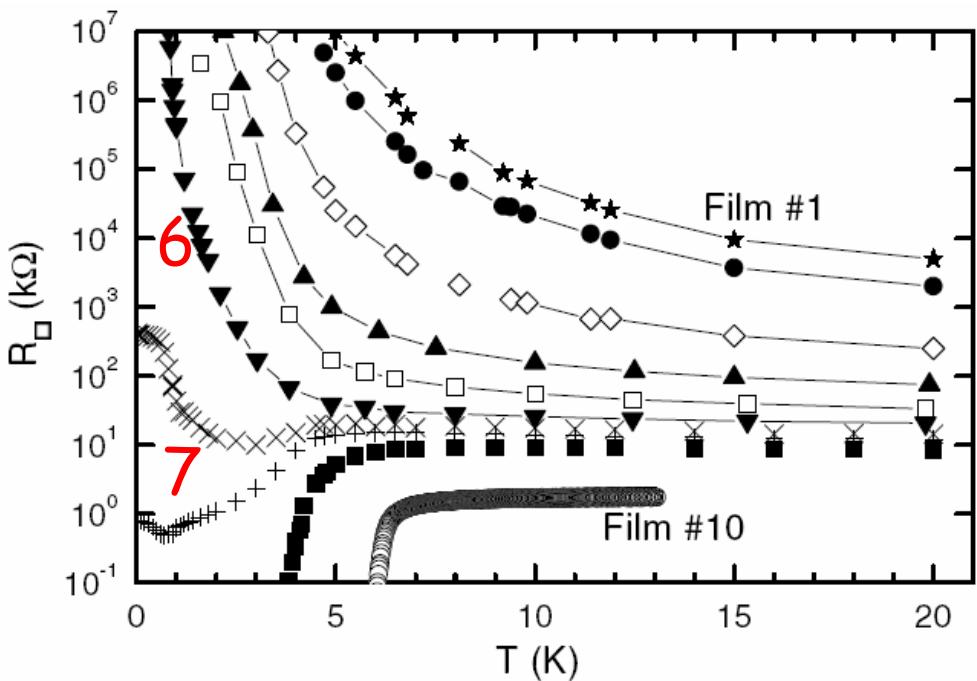
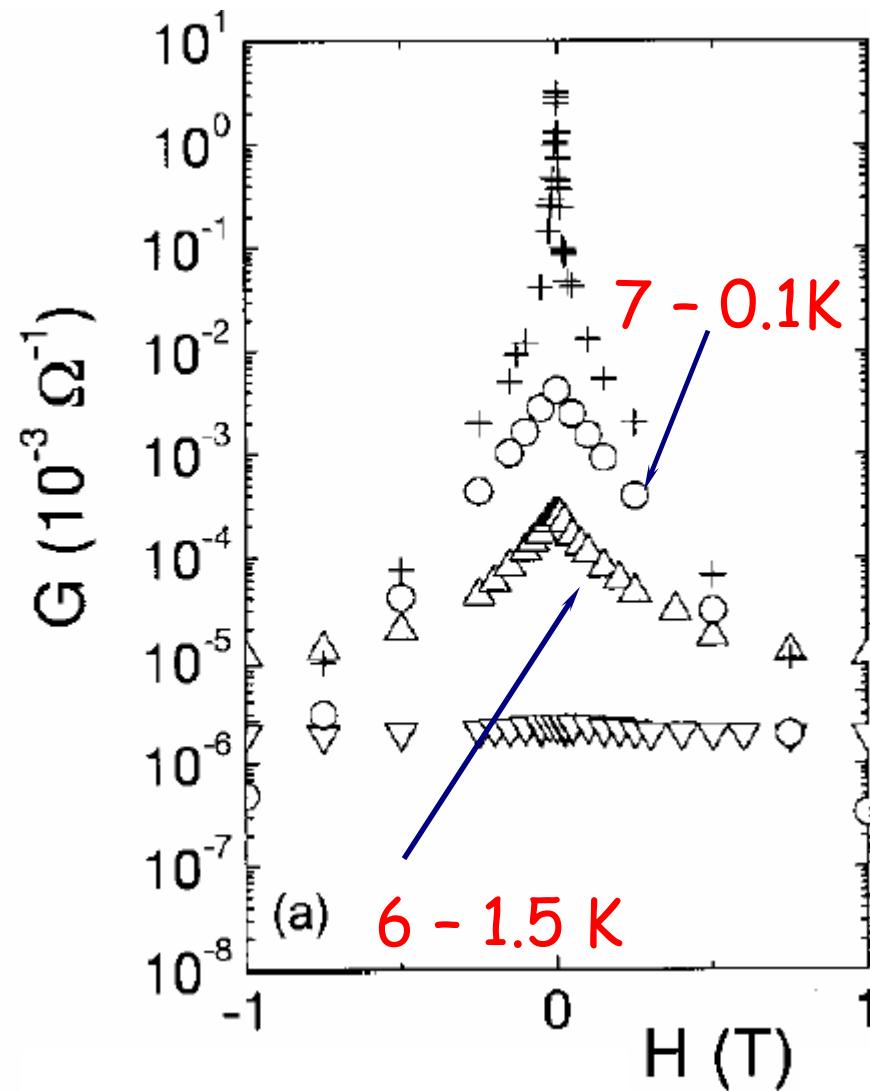
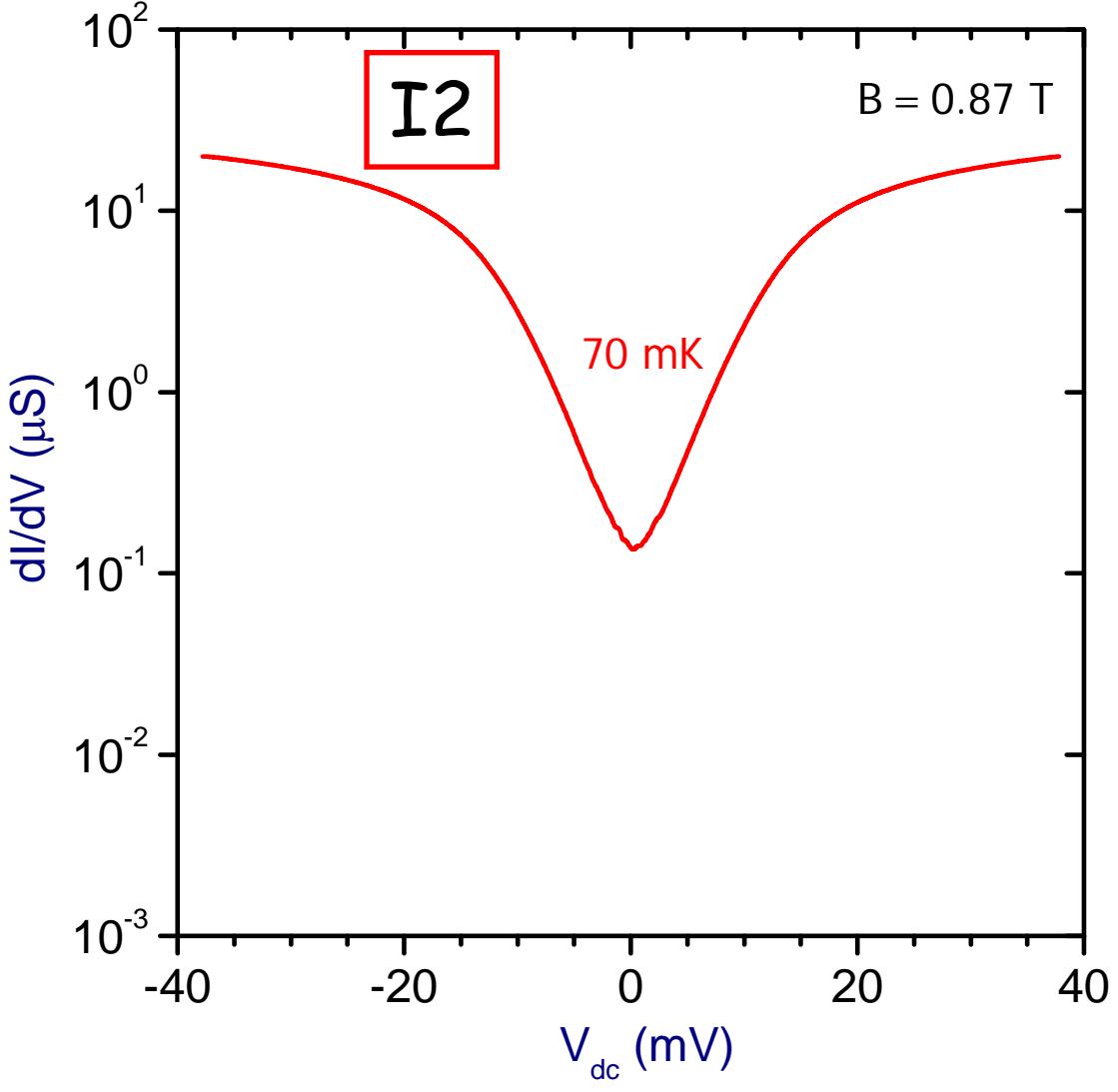


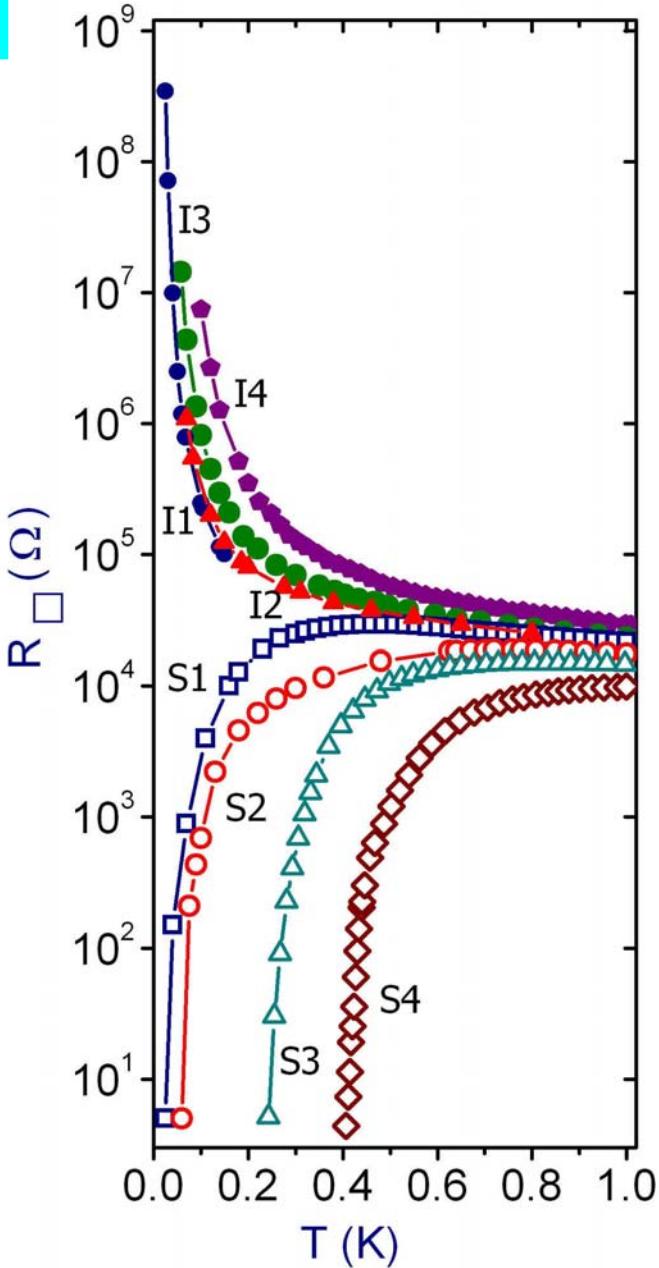
FIG. 1. Curves of film sheet resistance as a function of temperature measured on one film section following a series of deposition steps to increase film thickness. For curves from top to bottom, we label them as Film #1 to Film #10, respectively. The thickness for these films changed from 4.6 to 15.5 Å.



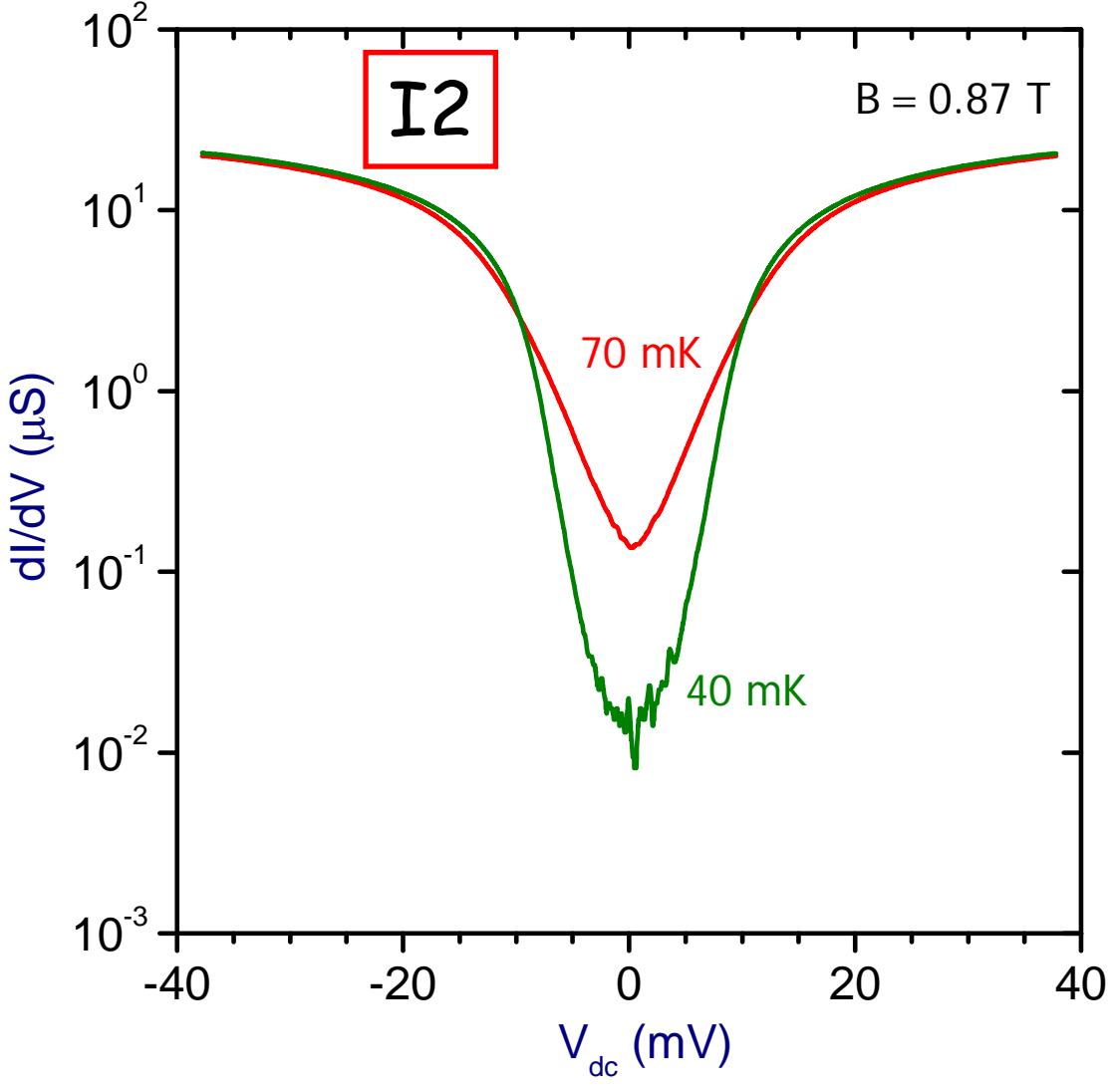
Collective insulating state: Threshold behavior of dI/dV vs V_{dc}



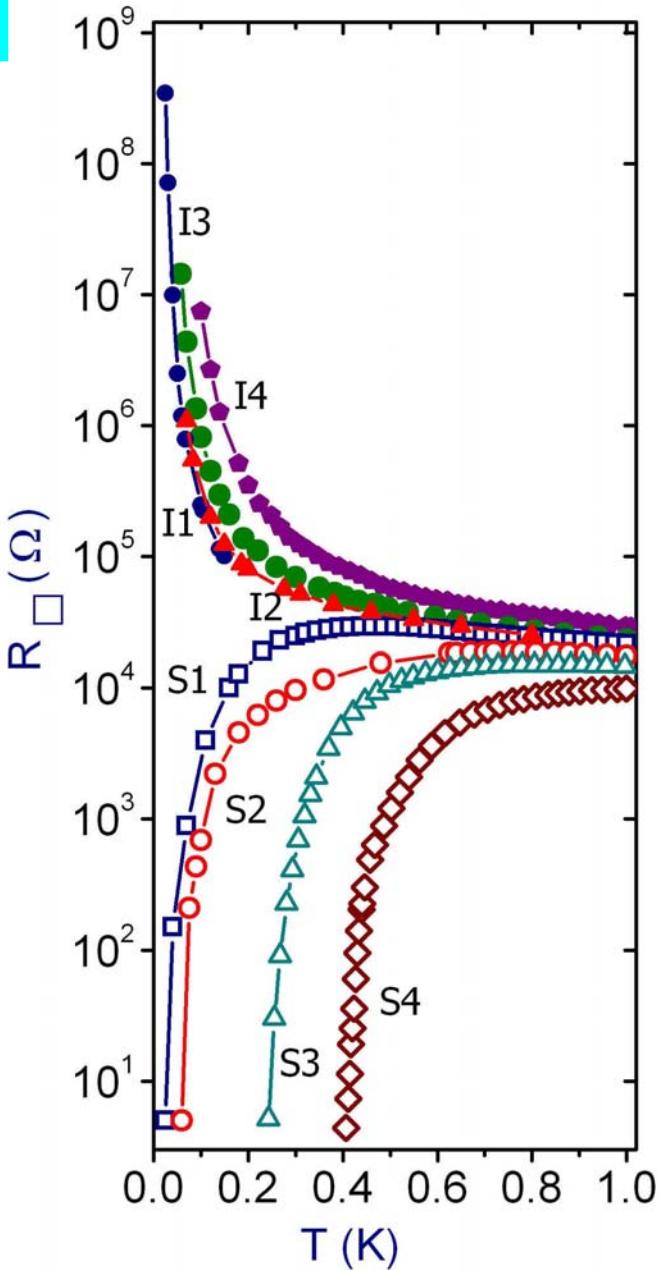
TiN films



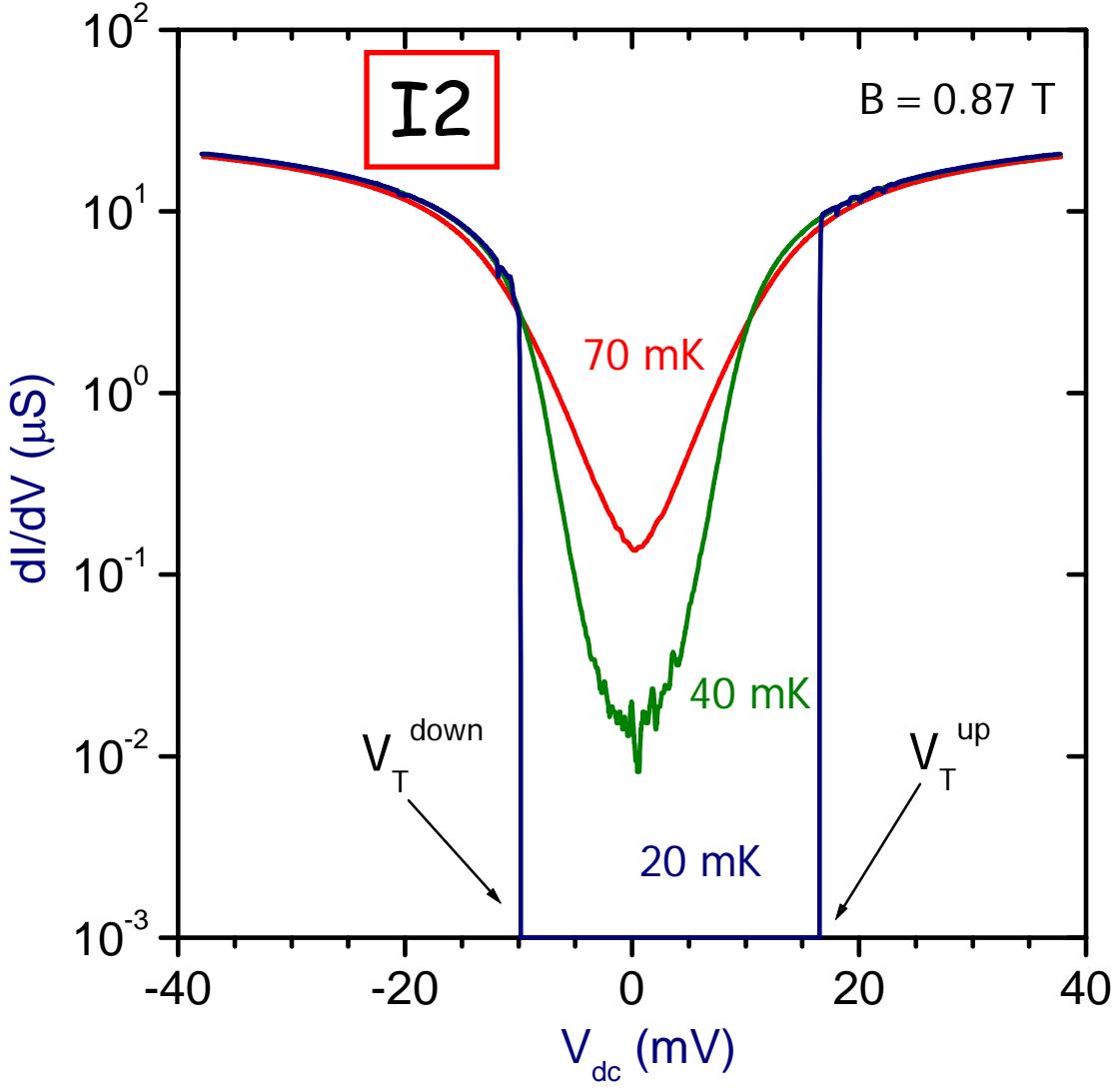
Collective insulating state:
Threshold behavior of dI/dV vs V_{dc}



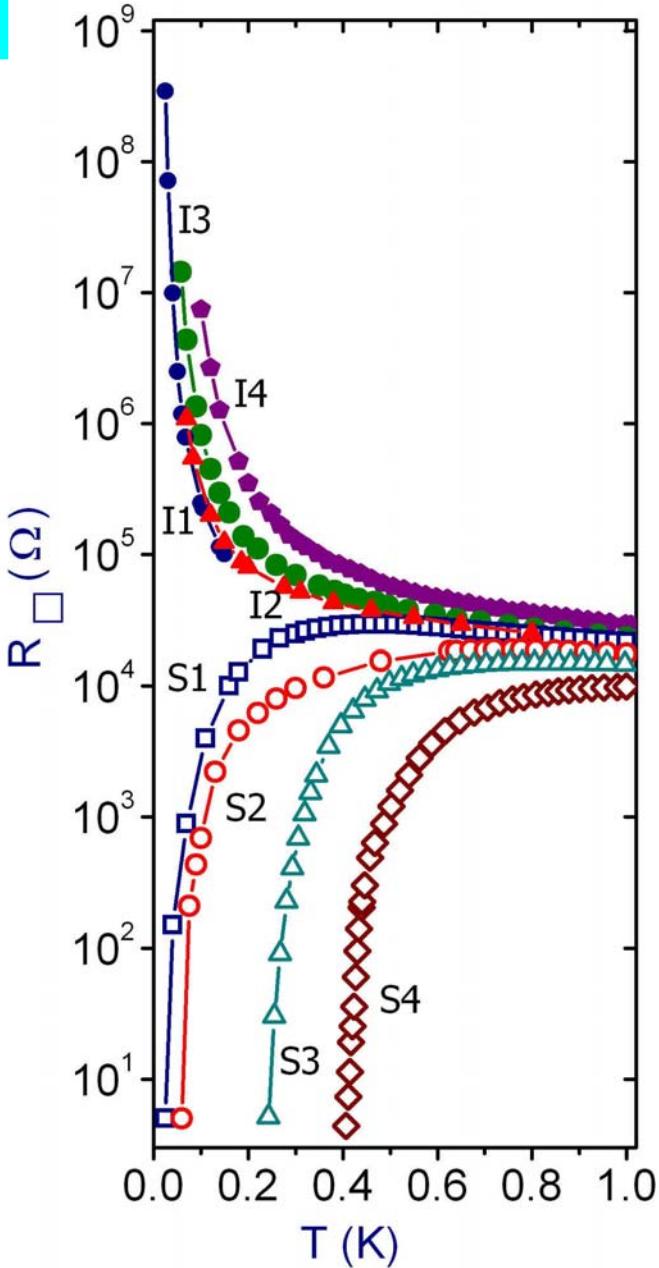
TiN films



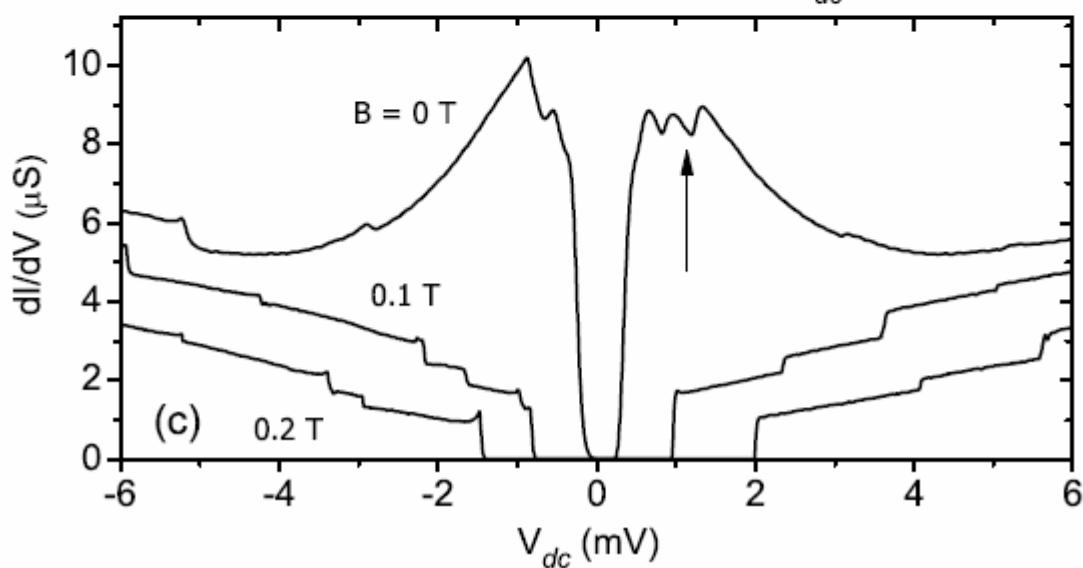
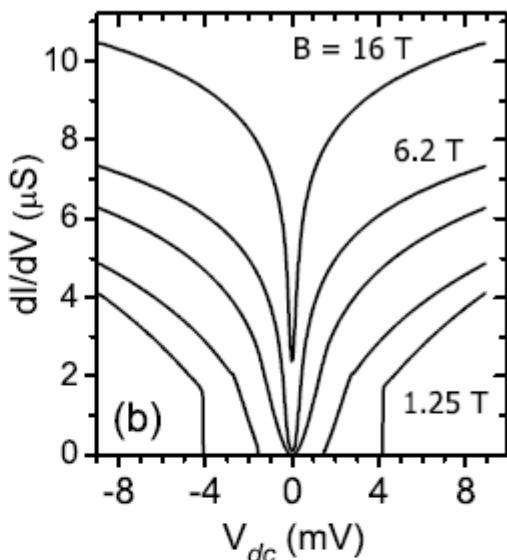
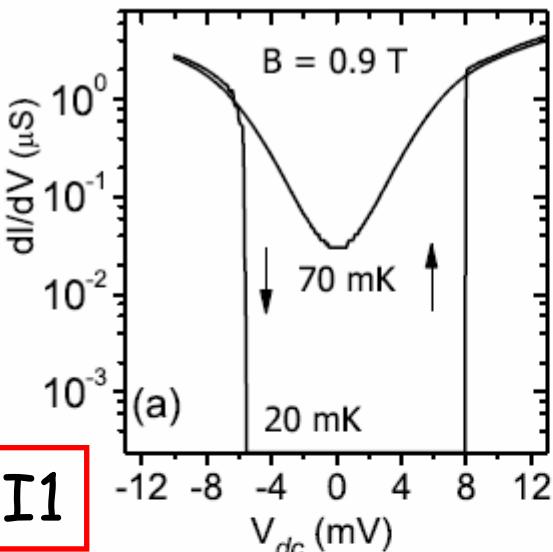
Collective insulating state:
Threshold behavior of dI/dV vs V_{dc}



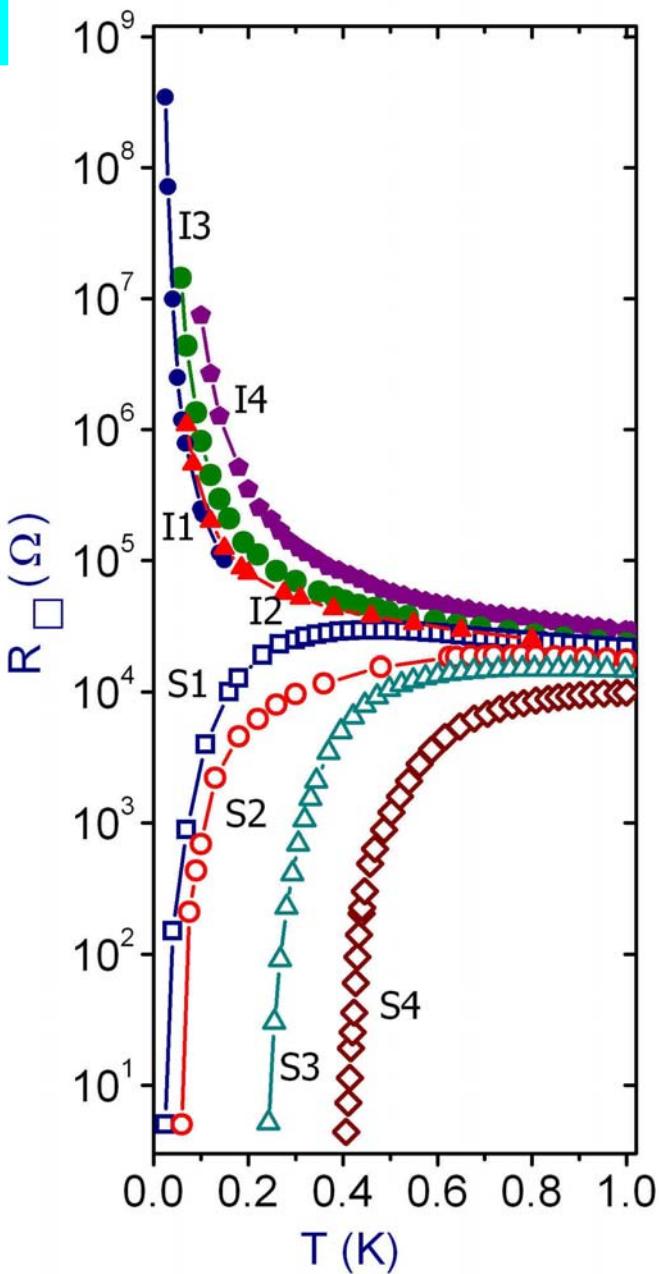
TiN films



Collective insulating state: Threshold behavior of dI/dV vs V_{dc}

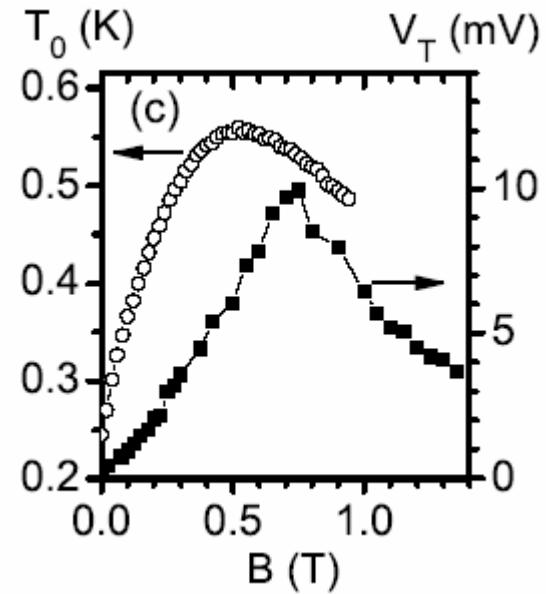
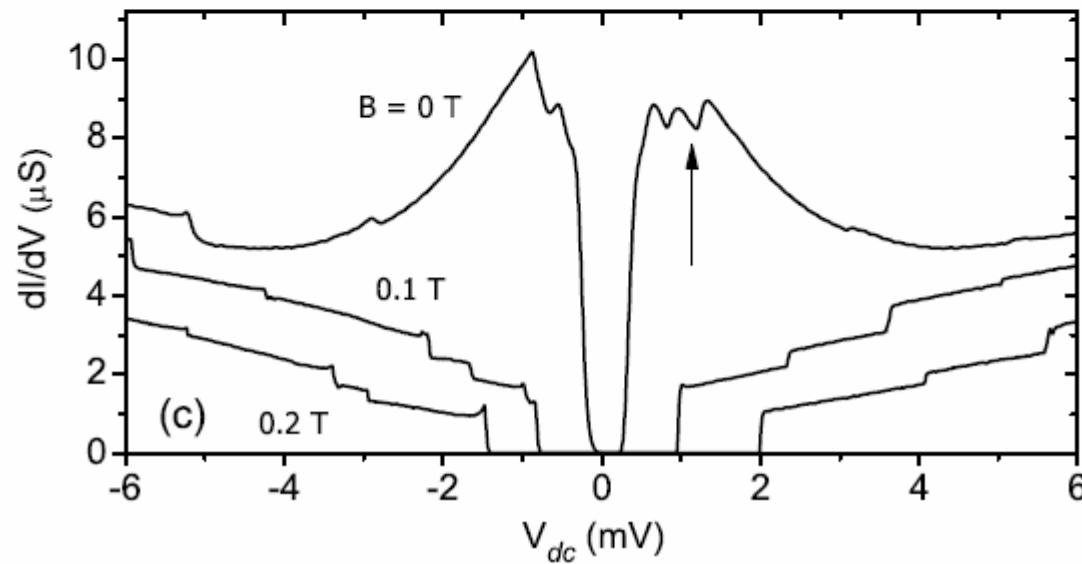
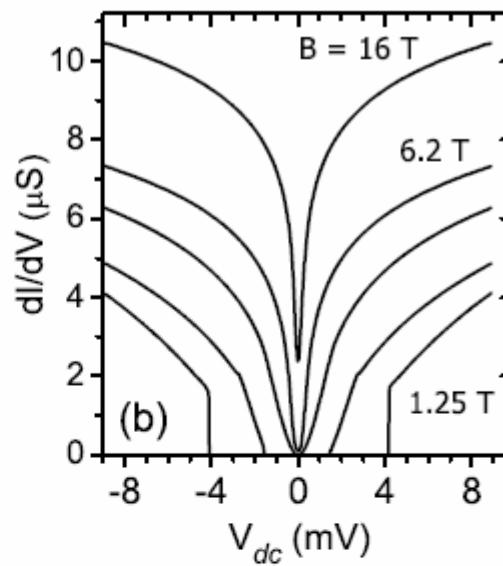
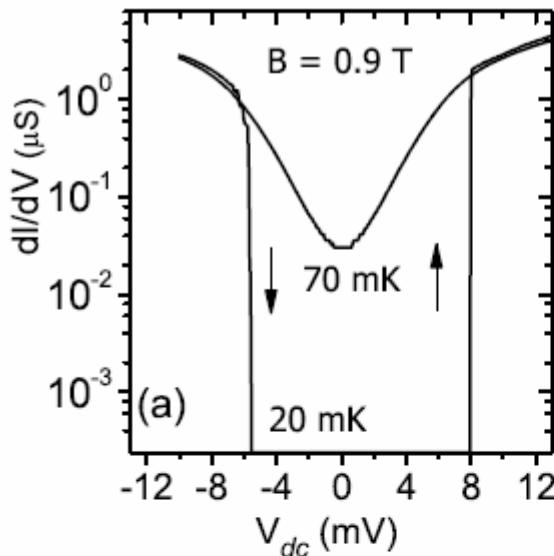


TiN films



Collective insulating state: Threshold behavior of dI/dV vs V_{dc}

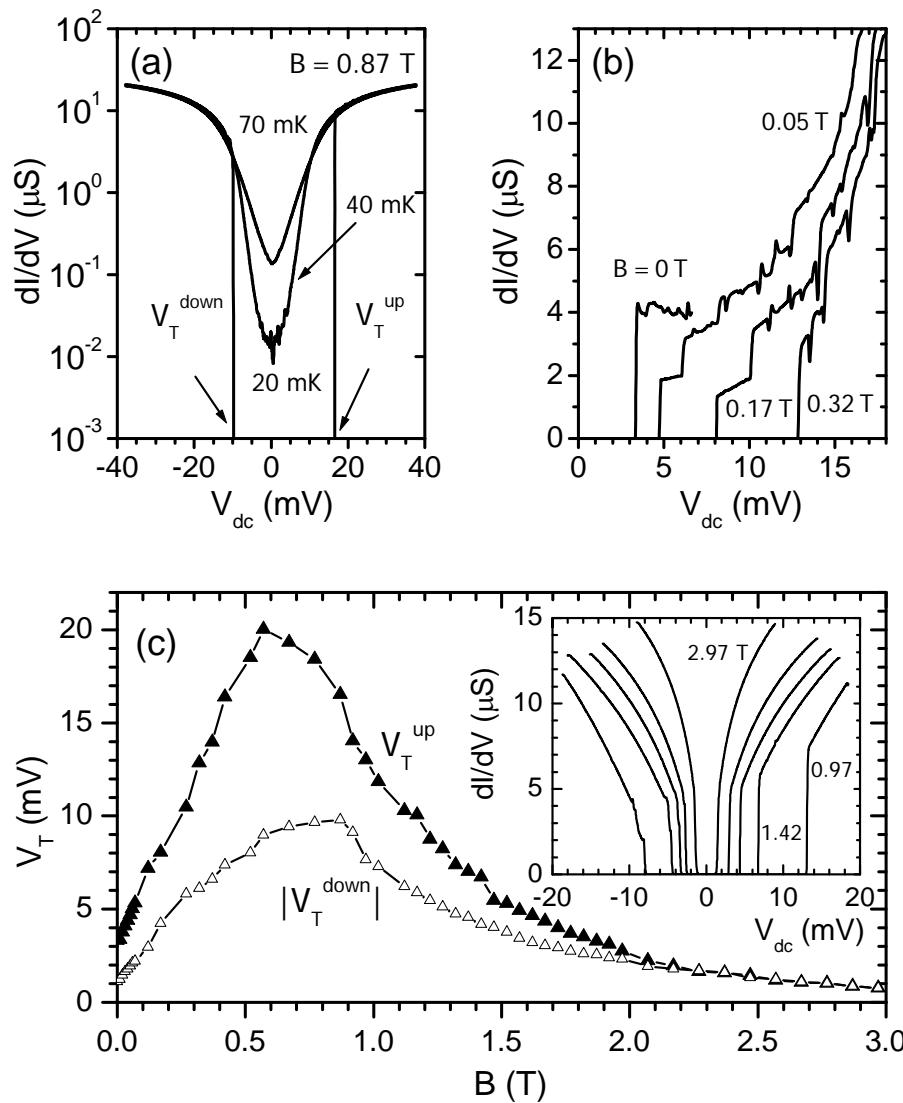
I1



The threshold voltage changes nonmonotonically upon magnetic field

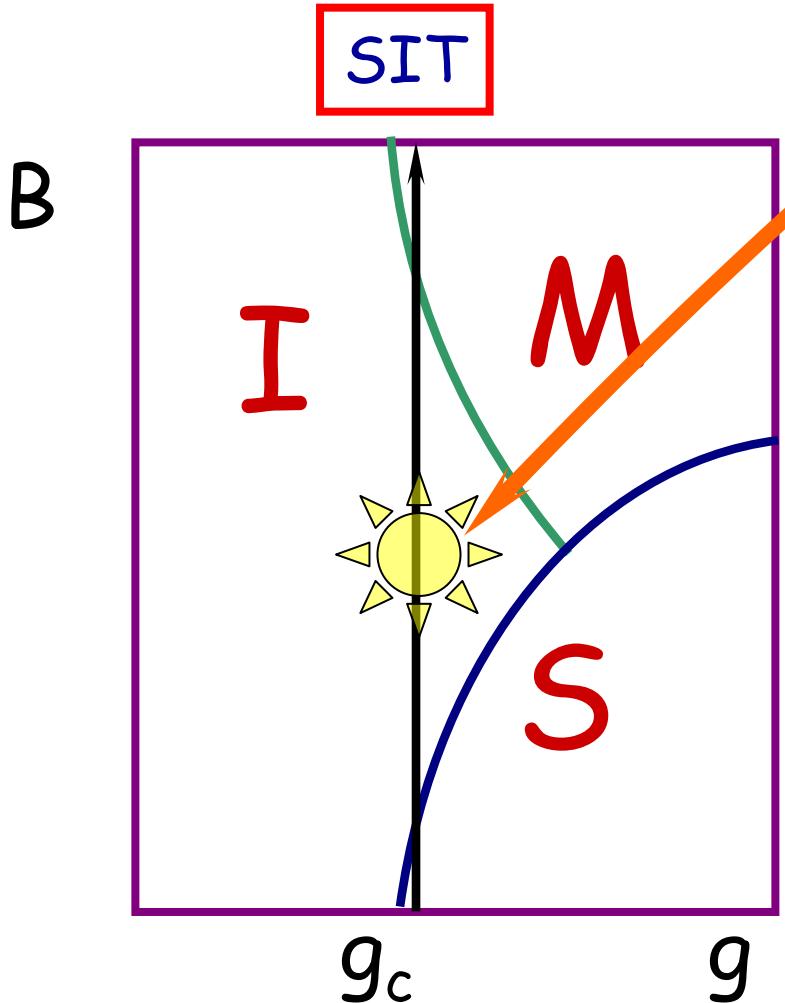
Collective insulating state: Threshold behavior of dI/dV vs V_{dc}

I2



The threshold voltage changes nonmonotonically upon magnetic field

schematic phase diagram

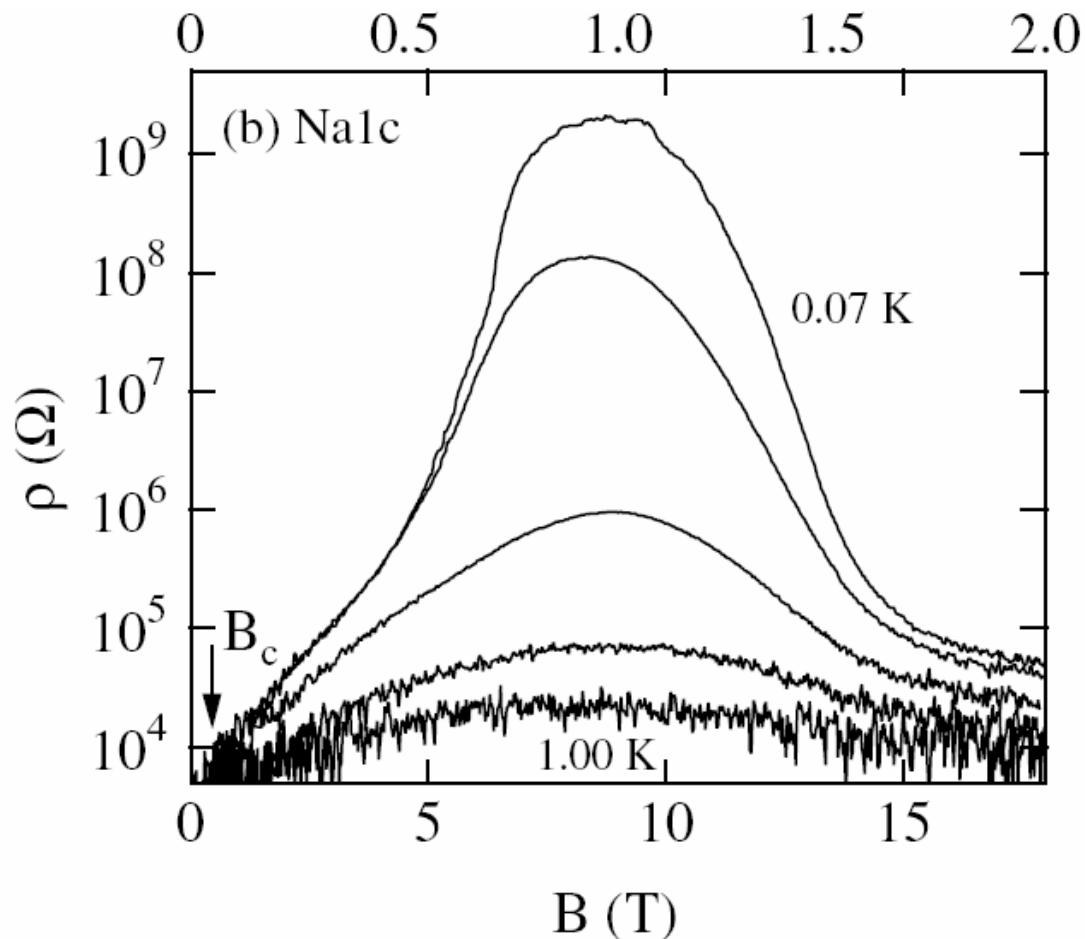


Magnetic-field-induced
insulating phase

InO_x films

Magnetic-field-induced insulating phase

InO_x films



G. Sambandamurthy,
L.W. Engel,
A. Johansson,
and D. Shahar,
PRL 92, 107005 (2004).

for sample Na1c at $T = 0.07, 0.16, 0.35, 0.62$, and 1.00 K.

Magnetic-field-induced insulating phase

InO_x films

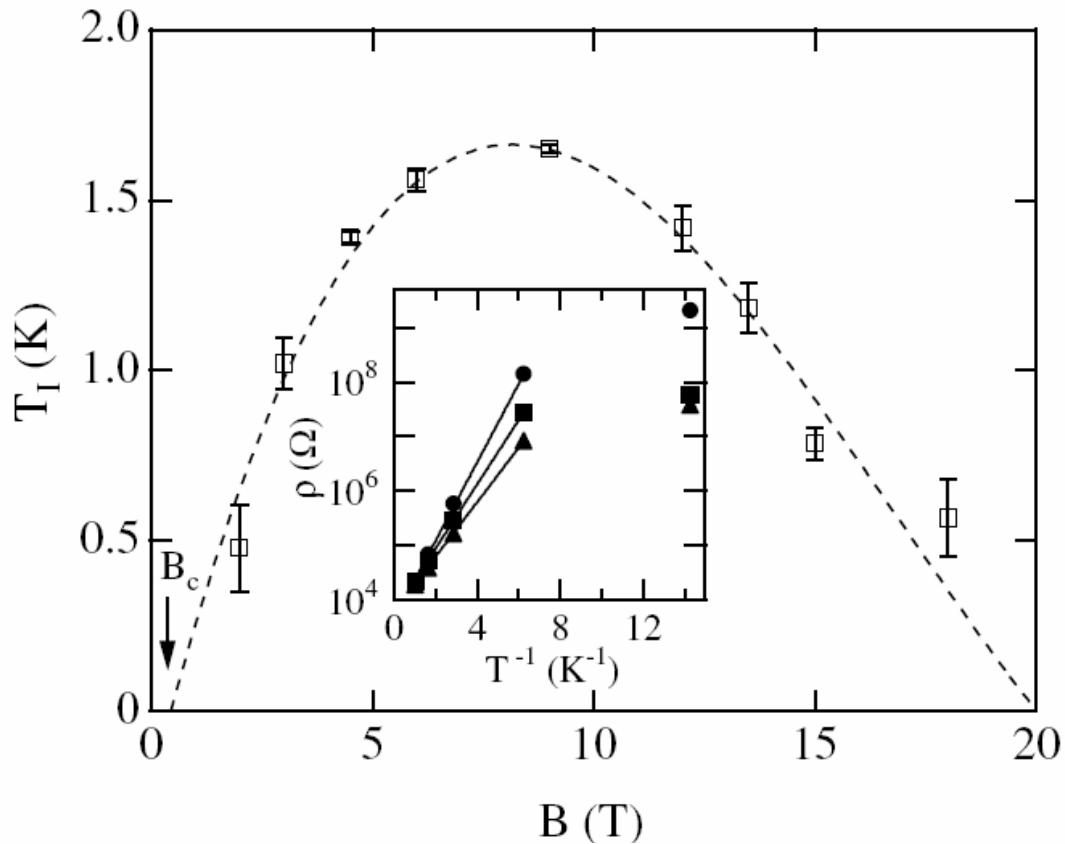
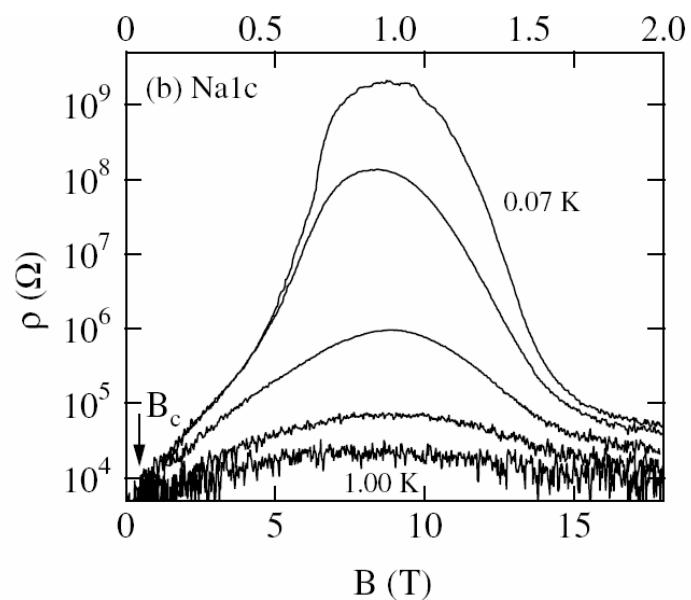


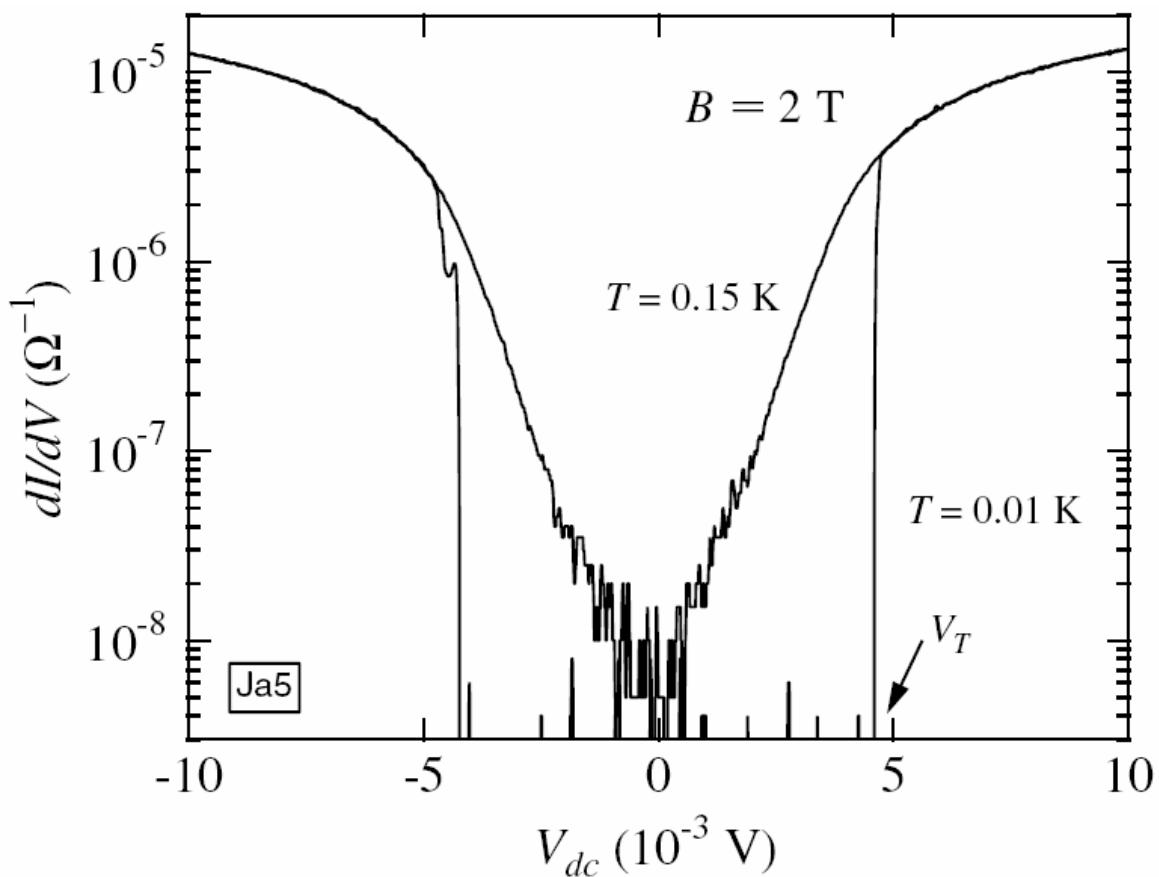
FIG. 3. Inset: ρ versus T^{-1} at $B = 6$ (squares), 9 (circles), and 12 T (triangles) for sample Na1c. The solid lines are fits to Eq. (1). The lowest T data points do not fit to the Arrhenius behavior. The main figure shows T_I , calculated from the fits to Eq. (1), as a function of B . T_I has a peak at 9 T. T_I estimates for $4 \text{ T} > B > 14 \text{ T}$ suffer from large errors since the low- T ρ value is not high enough to ensure activated behavior. The vertical arrow marks B_c ($= 0.45 \text{ T}$), where $T_I = 0$. The dashed line is a guide to the eye.

G. Sambandamurthy,
L.W. Engel,
A. Johansson,
and D. Shahar,
PRL 92, 107005 (2004).



Magnetic-field-induced insulating phase

InO_x films



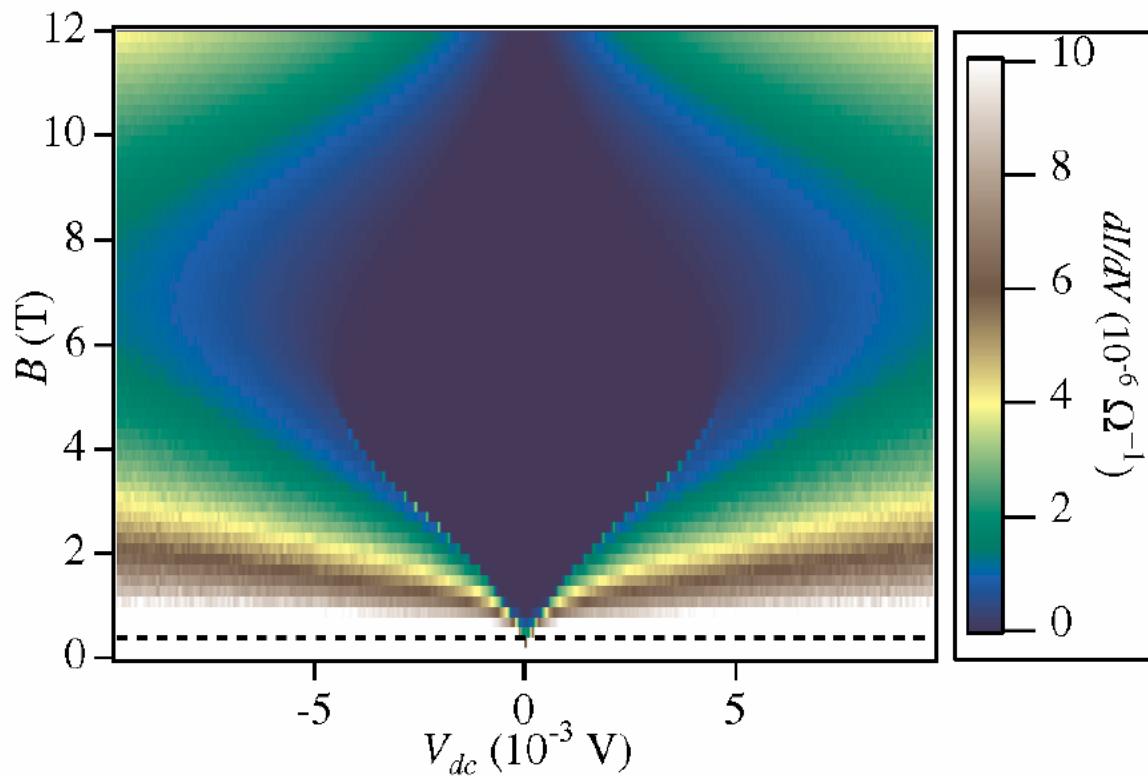
G. Sambandamurthy,
L.W. Engel,
A. Johansson,
E. Peled
and D. Shahar,
PRL 94, 017003 (2005).

Collective insulating state:
Threshold behavior
of dI/dV vs V_{dc}

FIG. 2. Comparison of the current-voltage characteristics of the B -driven insulating phase at two T 's (0.15 and 0.01 K). The traces show the two-terminal differential conductance measured at $B = 2$ T as a function of dc voltage. The ac excitation voltage applied is $10 \mu\text{V}$. The sample used is Ja5 with $B_c = 0.4$ T. V_T marks the threshold voltage for conduction at $T = 0.01$ K.

Magnetic-field-induced insulating phase

InO_x films



G. Sambandamurthy,
L.W. Engel,
A. Johansson,
E. Peled
and D. Shahar,
PRL 94, 017003 (2005).

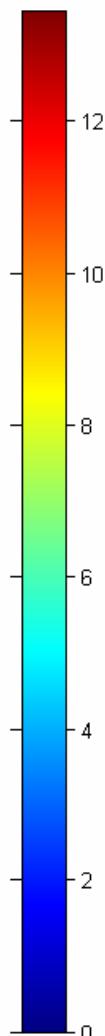
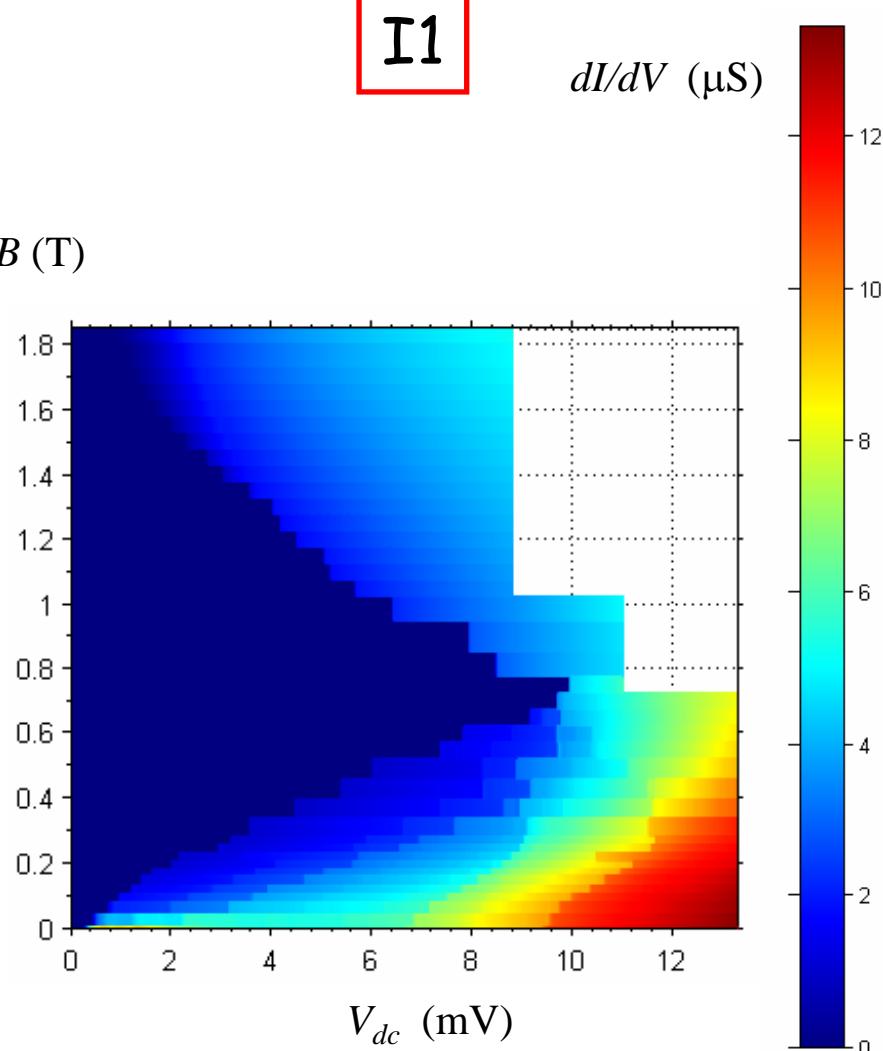
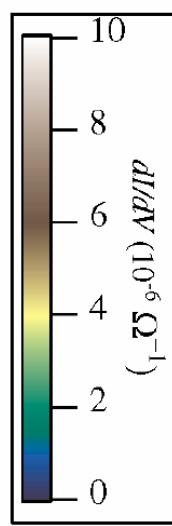
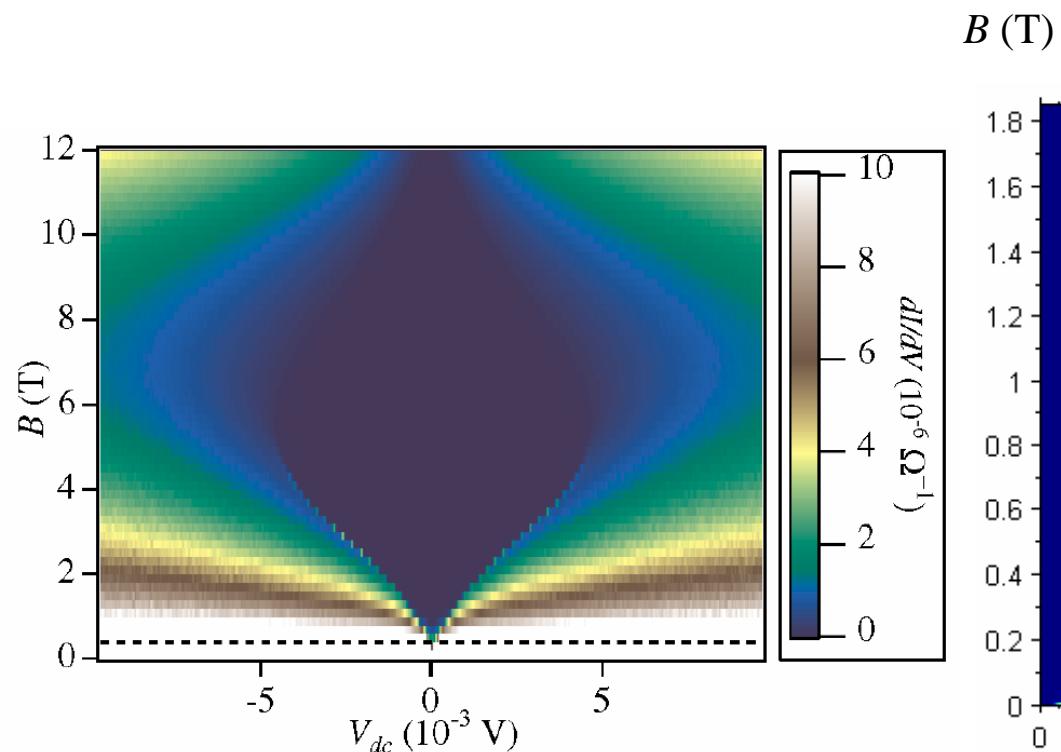
Collective insulating state:
Threshold behavior
of dI/dV vs V_{dc}

FIG. 4 (color). Two-dimensional map of the dI/dV values in the $B - V_{dc}$ plane. For the sample of Fig. 2 (Ja5), we have measured dI/dV traces as a function of V_{dc} at B intervals of 0.2 T and at $T = 0.01$ K. The color scale legend on the right-hand side shows the various colors used to represent the values of dI/dV . The horizontal dashed line denotes B_c ($= 0.4$ T) of this sample.

InO_x film
Sc at B=0

Collective insulating state:
Threshold behavior
of dI/dV vs V_{dc}

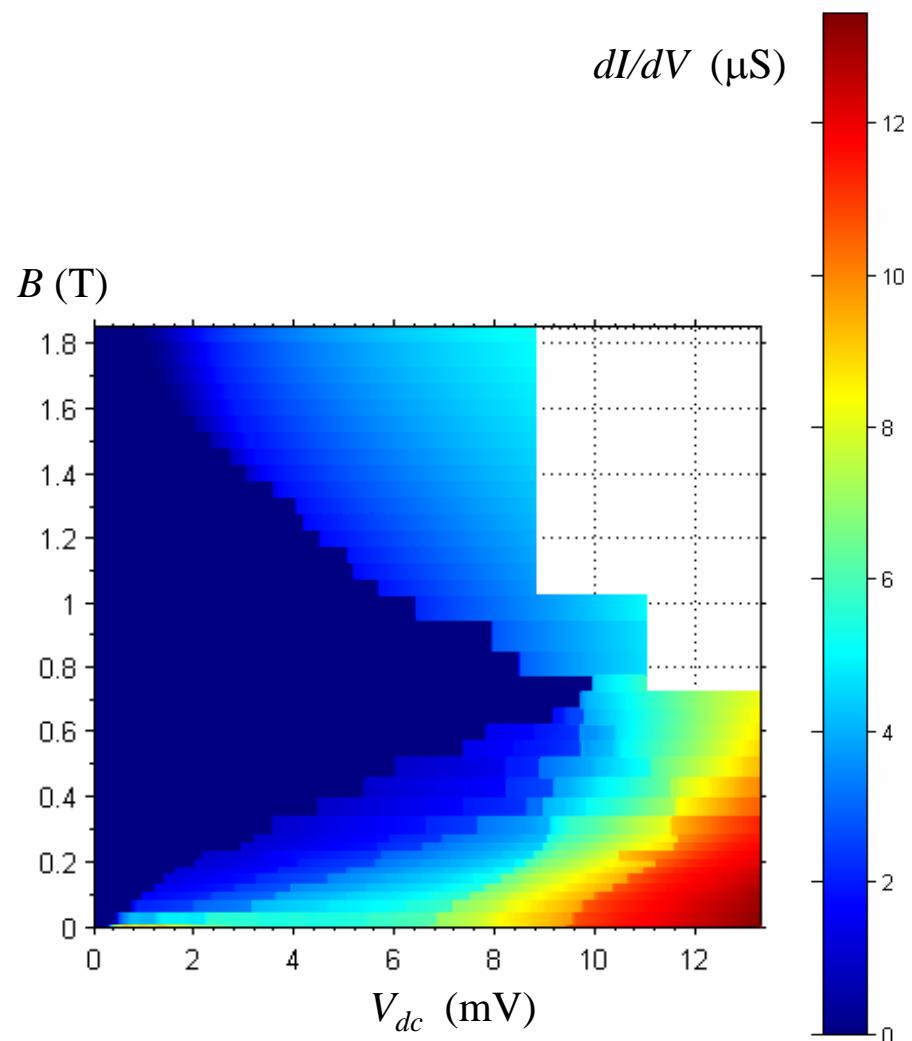
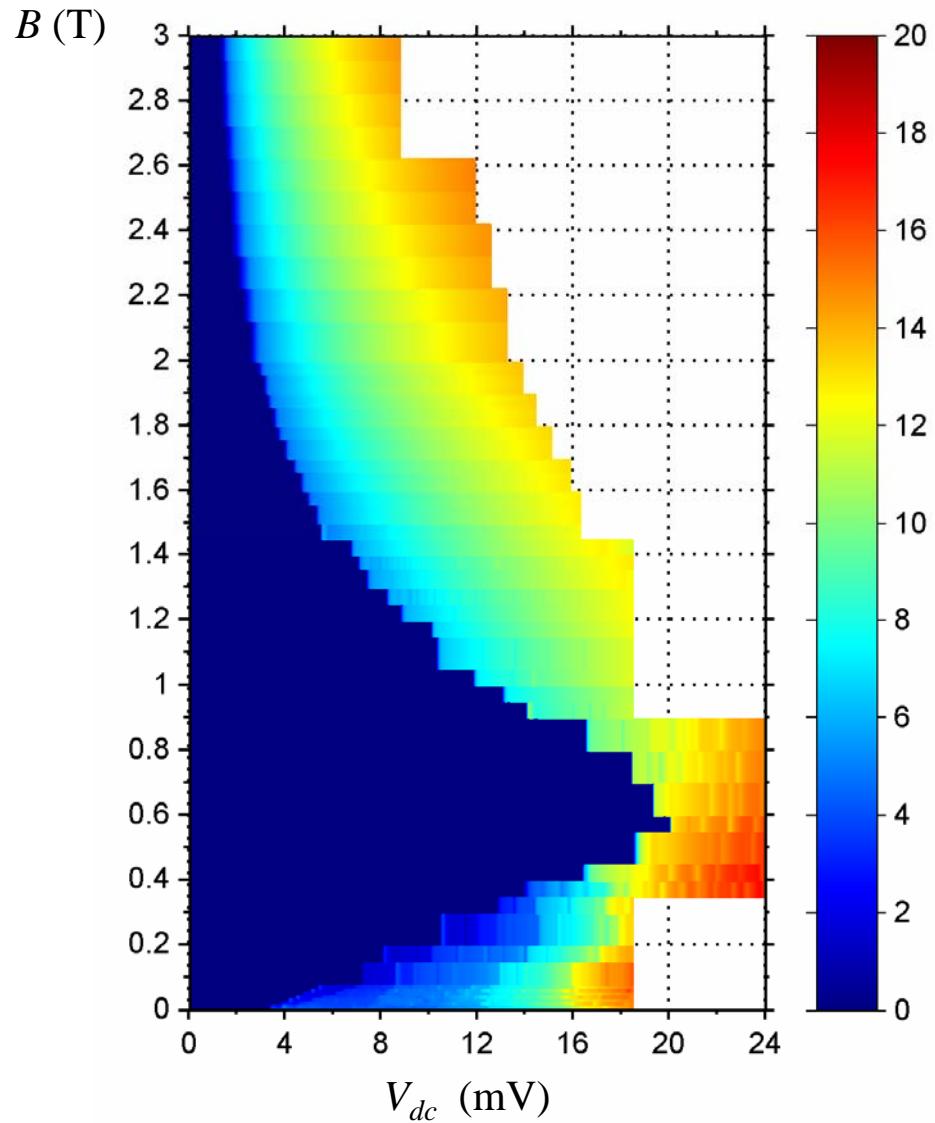
TiN film
Ins. at B=0



TiN film
I2

Collective insulating state:
Threshold behavior
of dI/dV vs V_{dc}

TiN film
I1



Critical Region of the Disorder-Driven Superconductor-Insulator quantum phase transition

Aggregate of Experimental Features

- ✓ thermally activated behavior of the conductivity
- ✓ positive magnetoresistance at low magnetic field
- ✓ negative magnetoresistance with a saturation near h/e^2 in high magnetic fields
- ✓ voltage threshold for conductivity

in the vicinity of the D-SIT,
the response to applied magnetic and/or electric fields, is
the same irrespectively of whether the underlying ground
state is superconducting or insulating

It looks like...

E. Chow, P. Delsing, D.B. Haviland, PRL 81, 204 (1998).

One-dimensional arrays of small-capacitance Josephson junctions
(255, 127, and 63 junctions)

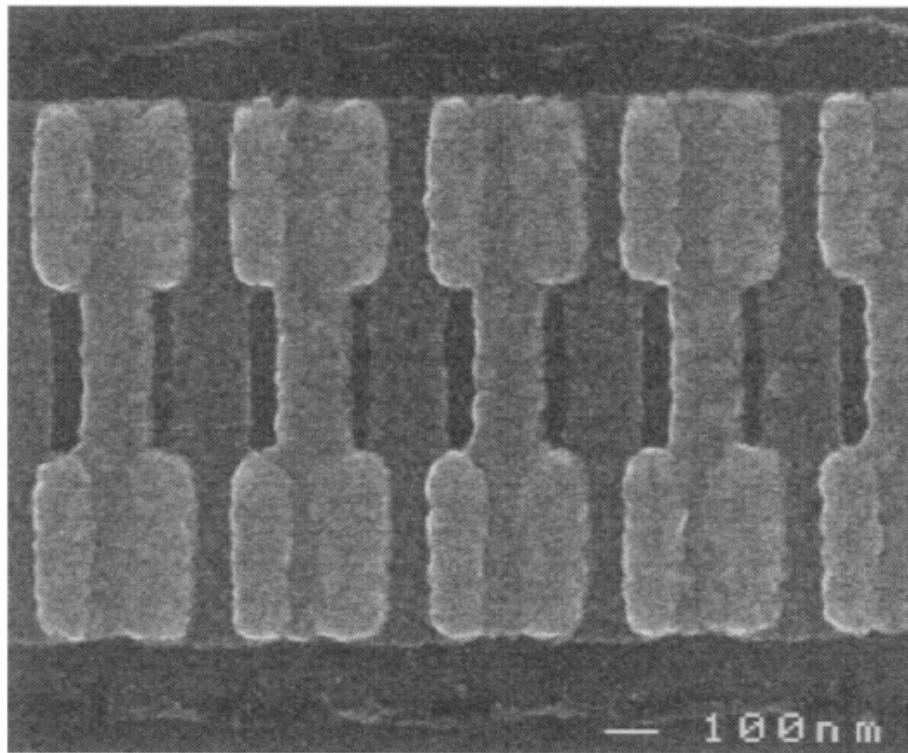


FIG. 1. A scanning electron micrograph of a section of the Josephson junction array. Tunnel junctions are formed at the overlap between the base electrode (darker gray) and the top electrode (lighter gray). The hole between neighboring electrodes forms the SQUID geometry.

Al/Al₂O₃/Al tunnel junctions

$A_{\text{loop}} = 0.12 \mu\text{m}^2$ is
the effective area of the SQUID loop.
 $A \simeq 0.039 \mu\text{m}^2$ is junction area

$$R_T = 4.9 \text{ k}\Omega \pm 6\%$$

$$C \simeq 3.5 \text{ fF}$$

electrostatic screening length

$$\Lambda \equiv (C/C_0)^{1/2} \simeq 10$$

$$E_{J0}/E_C \simeq 142 \text{ }\mu\text{eV}/23 \text{ }\mu\text{eV} = 6.1$$

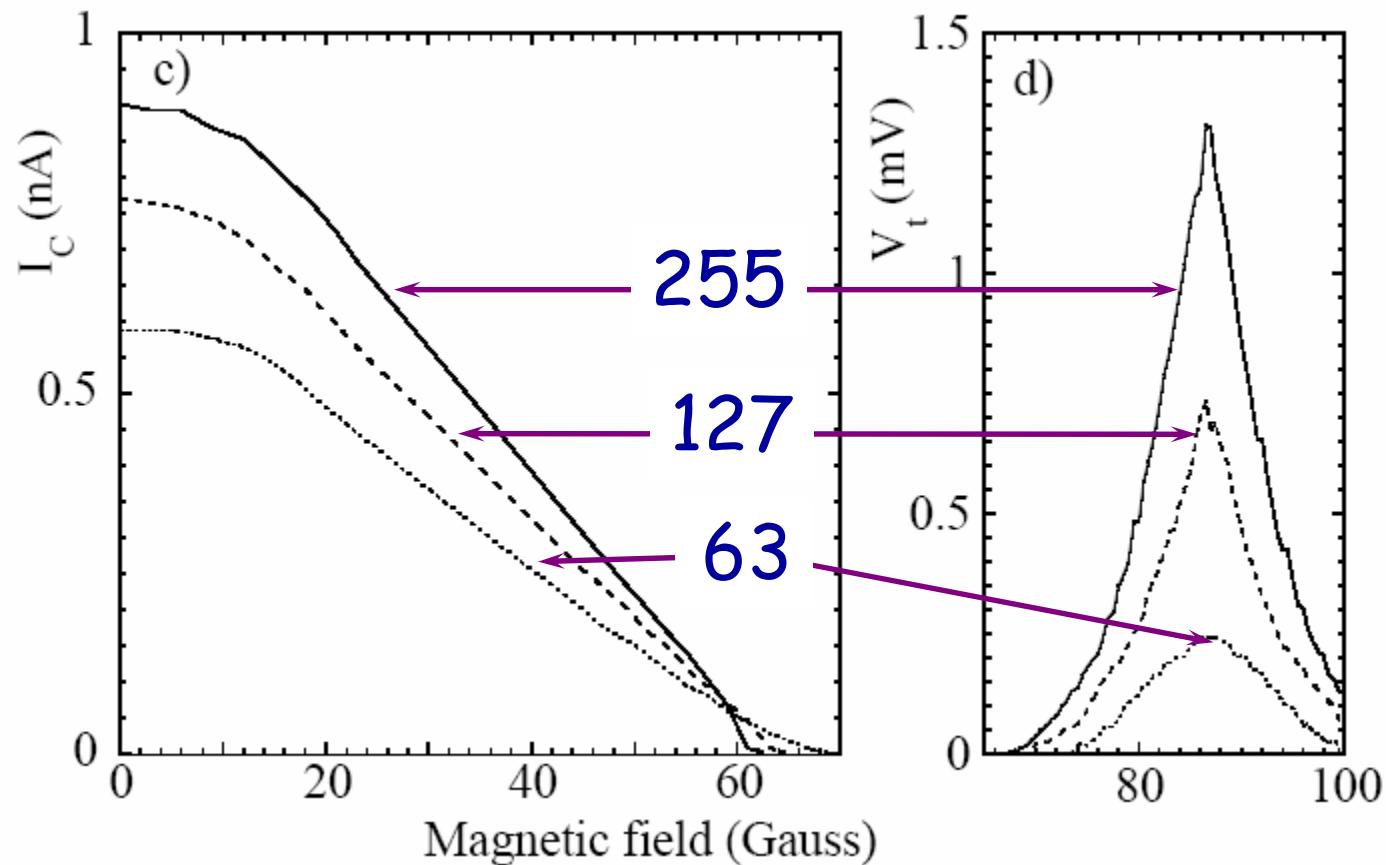
$$E_J = E_{J0} |\cos \pi B A_{\text{loop}} / \Phi_0|$$

It looks like...

E. Chow, P. Delsing, D.B. Haviland, PRL 81, 204 (1998).

One-dimensional arrays of small-capacitance Josephson junctions
(255, 127, and 63 junctions)

$T = 50 \text{ mK}$

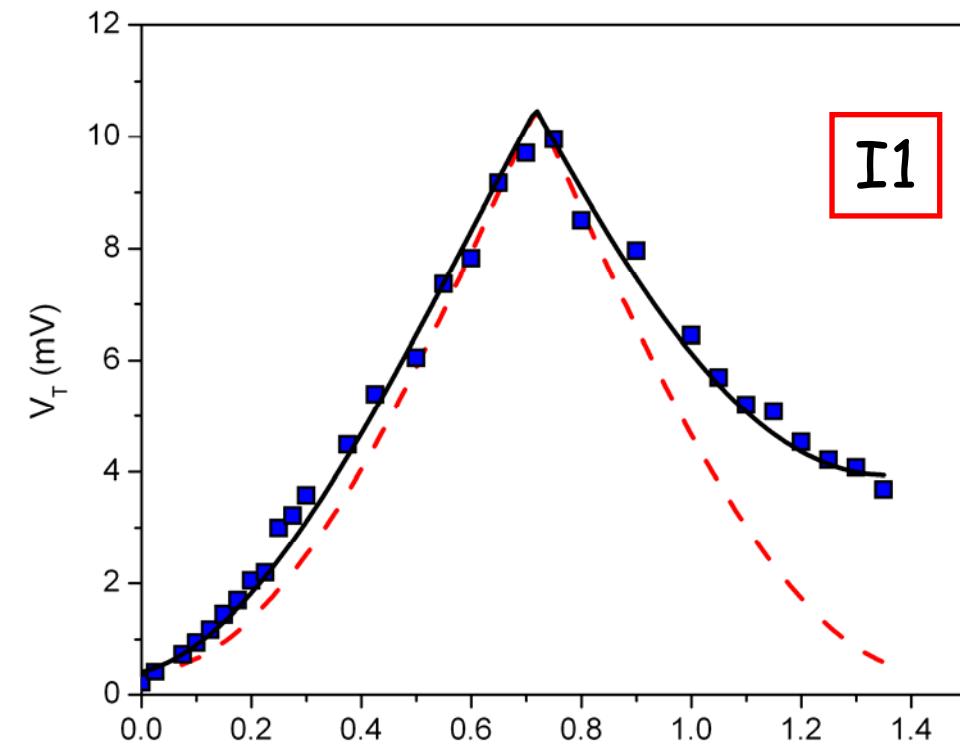


TiN film

Ins. at B=0

E. Chow, P. Delsing, D.B. Haviland,
PRL 81, 204 (1998).

One-dimensional arrays
of small-capacitance
Josephson junctions
(255, 127, and 63 junctions)



$$V_T(B) = V_0 \left(1 - \alpha E_J(B)/E_c\right), \quad E_J = E_{J0} |\cos \pi B A_{loop}/\Phi_0|$$

$$\alpha E_{J0}/E_c = 0.96 \text{ and } A_{loop} = 1.44 \cdot 10^{-3} \mu\text{m}^2$$

$$\underline{\alpha E_{J0}/E_c = 0.96 - 0.0024 \cdot B}$$

